Upgrading Ethereum

A technical handbook on Ethereum's move to proof of stake and beyond.

Ben Edgington



Capella Edition

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Preface

Upgrading Ethereum

Welcome to my book about upgrading Ethereum: Ethereum on proof of stake and beyond.

Work in progress!

I am writing this book backwards. Bottom up. Starting with the details and working towards the big picture.

The first pretty much complete part is Part 3: The Annotated Spec. These are the guts of the machine. Like the innards of a computer, all the components are showing and the wires are hanging out: everything is on display. But with the guts in place, everything else can be built around them with the messiness all neatly tucked away.

I'm now working on Part 2: Technical Overview which wraps a first, hopefully more accessible, layer around the Annotated Spec. Again, I'm writing this backwards, starting with the protocol's Building Blocks and its Incentive Mechanisms and working forwards towards a higher level narrative of how it all fits together. The current focus is on the Consensus chapter.

Warning: until Edition 1.0 is out, anything may change. I'll try not to change URLs and anchors in the Annotated Spec part, but no promises. Anything else, including entire chapters and sections, should be considered unstable.

What to expect

This is a book for those who want to understand Ethereum 2.0 – Ethereum on proof of stake – at a technical level. What does it do? How does it work? Why is it like this?

Who am I writing for? For people like me! People who enjoy understanding how things work. But more than that, who like to know why things are the way they are. This is not intended to be an academic work; I am more interested in insight than in rigour. But I try to link out to relevant academic papers and formal analyses where relevant.

Although I am an Ethereum staker and an Ethereum user, I am not writing primarily for stakers or users here. Some of the generic material on Staking may be relevant (once I have written it), but you will find better help in places like the excellent EthStaker community.

The scope of the book concerns (what I consider to be) the Ethereum 2.0 protocol. Ethereum 2.0 has become a less well-defined term recently. But for me, it broadly includes,

- all things proof of stake and the beacon chain,
- the process of The Merge by which Ethereum moved to proof of stake,
- in-protocol data sharding, and
- an array of potential future enhancements.

I will not be covering any of the historic Ethereum 1.0 protocol, except as it touches upon The Merge. The Mastering Ethereum book is an excellent resource, though rather out of date now. Although rollups and other so-called layer 2 solutions have rapidly become part of the overall Ethereum 2.0 system, they

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are by definition not in-protocol, and I will not be covering them here. I will not be discussing, DeFi, DAOs, NFTs, or any of the wonderful things that can be built on top of this amazing technology.

It's a chunky list of exclusions, but there's still plenty to talk about.

Versions

This edition covers the Capella version of the deployed Ethereum 2.0 consensus layer. The beacon chain went live with Phase 0 on December 1st, 2020. It was upgraded to Altair on October 27th, 2021, to Bellatrix on September 6th, 2022, and to Capella on April 12th, 2023.

Specifically, unless otherwise stated, any reference to the consensus specifications is to the version tagged v1.3.0 (the Gamlum release).

Historical and current versions of Upgrading Ethereum are available online:

- The old Altair spec version,
- The old Bellatrix spec version,
- The current Capella spec version, and
- The latest version, which is currently Capella.

My original annotated specification for the Phase 0 version is also available, though largely of historical interest and now subsumed into this book.

In defence of "Eth2"

When I started this writing project, Ethereum on proof of stake was universally known as Ethereum 2.0, Eth2 for short, as it had been since 2014. This reflects the fact that the Ethereum 2.0 vision diverged from the original Ethereum 1.0 implementation in many respects. The direction of travel was well-captured in the Ethereum.org 2.0 Mauve Paper in 2016. The details of our eventual implementation differ from what's presented there, but the elements were all in place even then. Eth2 was to deliver not only proof of stake, but new cryptography, new peer-to-peer networking, new cryptoeconomics, and new directions in scalability, among other things. This is what we achieved.

In 2022, the Ethereum Foundation declared that we must emphasise continuity over discontinuity by rebranding Ethereum 2.0 back to plain old Ethereum. With the way that the Merge was coming together, that made some sense from an Ethereum user's point of view. The user and developer experience was to be almost unchanged by the move to proof of stake.

However, I am not writing primarily as a user of Ethereum or as a developer on Ethereum. From the point of view of a *protocol engineer*, the Merge was a moment of profound discontinuity. Ethereum on proof of stake is utterly different from Ethereum on proof of work - the size and complexity of this book is ample evidence of that. With Ethereum's new architecture we have delivered a good chunk of what the Mauve Paper laid out all those years ago.

This is why I often continue to refer to Ethereum on proof of stake as Ethereum 2.0 or Eth2¹, and I make no apology for that. I am confident that you will understand what I mean, and that it will help clarify rather than confuse.

While we're here, another thing I won't be apologising for is using British English spelling, punctuation, and quaint idioms. It's a feature, not a bug.

Acknowledgements

Above all, I want to thank my employer, Consensys. Much of the writing has been done in my own time, but Consensys has been increasingly supportive of me working on this in the course of my day job. In particular, during Q2 2023, the company granted me three months of writing leave to work full-time on the book. They also allowed me to put a liberal licence on everything. All this is extremely cool of them,

¹That, and being a bloody-minded reactionary who dislikes being told what to do and say by a centralised authority. The EF's claim that, "As of late 2021, core developers stopped using the terminology" is laughably untrue.

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and I am deeply grateful. Consensys is a wonderful employer, a terrific force for good in the ecosystem, and an incredible place to work.

So much of what I do involves writing about other people's work, and pretty much everything in this book is other people's work. I deeply value the openness and generosity of the Ethereum community. For me, this is one of its defining characteristics. Many people's contributions are cited throughout this book, and I am indebted to all of you. Being part of the Eth2 dev community has been the best experience of my life.

Thank you to the many GitCoin grant supporters who donated in support of the original annotated specification and my regular What's New in Eth2 newsletter. And to generous crypto friends, anon and otherwise, for your kind gifts over the years. Your support has encouraged me hugely as I've wrestled with the minutiae of the spec. I bloody love this community.

Shout-out to the EthStaker community: you rock!

Finally, to circle back to Consensys: working daily with such brilliant, talented, generous, and knowledgeable people is a joy. The Protocols group, PegaSys, has been my home for the past five-plus years. It is where I helped establish the fabulous Protocols R&D team, and later kicked off the project that became Teku. Thank you for all your support and encouragement. I love working with all you wonderful people.

Part 1: Building

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Introduction

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TODO: Intro

The Beacon Chain

Introduction

TODO

Terminology

TODO

Design Overview

TODO

Architecture of a Node

TODO

Genesis

Consensus

Here's the opening sentence of a paper about attacks on the Ethereum 2.0 consensus protocol:

The Proof-of-Stake (PoS) Ethereum consensus protocol is constructed by applying the finality gadget Casper FFG on top of the fork choice rule LMD GHOST, a flavor of the Greedy Heaviest-Observed Sub-Tree (GHOST) rule which considers only each participant's most recent vote (Latest Message Driven, LMD).

If that makes perfect sense to you then feel free to skip this chapter entirely. Otherwise, read on!

Our aim is to understand that sentence in all its parts. There's a lot to unpack, but we'll take time over it. We'll begin with some preliminaries covering basics of consensus that are not particularly specific to Ethereum.

After a high-level overview of the how the whole consensus protocol fits together, we will dive down into its component parts, first LMD GHOST, then Casper FFG. In the Gasper section we will see how these two are combined together.

Enough subtleties and edge cases arise from the way that the LMD GHOST and Casper FFG protocols interoperate that I've dedicated the closing section of this chapter to discussing these issues.

Preliminaries

- Consensus is a way to build reliable distributed systems with unreliable components.
- Blockchain-based distributed systems aim to agree on a single history of transactions.
- Proof of work and proof of stake are not consensus protocols, but enable consensus protocols.
- Many blockchain consensus protocols are "forkful".
- Forkful chains use a fork choice rule, and sometimes undergo reorganisations.
- In a "safe" protocol, nothing bad ever happens.
- In a "live" protocol, something good always happens.
- No practical protocol can be always safe and always live.

Introduction

This section covers the basics of consensus, fork choice, and finality. Most of it is not specific to Ethereum and is for general background understanding.

The challenge a consensus protocol seeks to solve is that of building a reliable distributed system on top of unreliable infrastructure. Consensus protocol research goes back to the 1970s and beyond, but the scale of the challenges we seek to solve in Ethereum are orders of magnitude more ambitious.

Our goal in Ethereum's consensus layer is to enable tens of thousands of independent nodes around the world to proceed completely in lockstep with each other. Each node maintains a ledger containing the state of every account, and every ledger must match every other ledger. There must be no discrepancies; the nodes must agree, and they must come to agreement swiftly. This is what I mean by "a reliable distributed system".

These nodes often run on consumer grade hardware. They communicate over Internet connections that might be low bandwidth, or high latency, that lose packets, or drop out for indefinite periods of time.

Node operators sometimes misconfigure their software, or don't keep it up to date. And, to make it all the more exciting, there is the possibility of large numbers of bad actors running rogue nodes or tampering with communications for their own gain. This is what I mean by "unreliable infrastructure".

An explicit design goal for Ethereum is that it doesn't only run well when every node is running well and communicating well. We have done our best to design a system that will do its best to continue running even when the world beneath it is falling apart.

Coming to consensus

The Ethereum network comprises a large number of individual nodes. Each node acts independently, and nodes communicate over an unreliable, asynchronous network, the Internet. Any individual node might be honest – behaving correctly at all times – or faulty in any arbitrary way: simply down or non-communicative, following a different version of the protocol, actively trying to mislead other nodes, publishing contradictory messages, or any manner of other fault.

Users submit transactions to this network of nodes, and the goal of the consensus protocol is that all correct nodes eventually agree on a single, consistent view of the history of transactions. That is, the order in which transactions were processed and the outcome of that processing. So, if I have 1 ETH and I simultaneously tell the network that I am sending that 1 ETH to Alice and also to Bob, we expect that eventually the network will agree that either I sent it to Alice or I sent it to Bob. It would be a failure if both Alice and Bob received my Ether, or if neither received it.

A consensus protocol is the process by which this agreement on the ordering of transactions comes about.

Ethereum's consensus protocol actually "bolts together" two different consensus protocols. One is called LMD GHOST, the other Casper FFG. The combination has become known as Gasper. In subsequent sections we will be looking at these both separately and in combination.

Byzantine generals

In a 1982 paper Leslie Lamport described in rather whimsical terms the fundamental problem that consensus systems are trying to solve - building reliable distributed systems.

We imagine that several divisions of the Byzantine army are camped outside an enemy city, each division commanded by its own general. The generals can communicate with one another only by messenger. After observing the enemy they must decide on a common plan of action.

This formulation makes clear that there is no overall holistic view, no God-mode in which we can see the whole situation in one glance and make a decision. We are simply one of the generals, and our only source of information about the other generals is the messages that we receive - messages that may be correct, or lies, or mistakes based on limited information, or delayed, or modified in transit. We have only a very limited local view, yet we must come to a view about the state of the whole system.

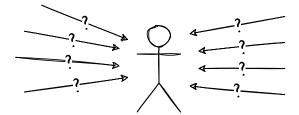
It is important to keep this in mind at all times. When we draw diagrams of block chains and block trees, it is easy to assume that this is somehow "the state" of the whole system. But these diagrams only ever represent the local view of a single participant in the system. My node's view of the system is likely to differ from your node's view of the system, if only temporarily, because we operate over an unreliable network. For example, you will see blocks at different times from when I see them, or in a different order, or even different blocks from those that I see.

Lamport captures the faultiness of the system in the following way.

However, some of the generals may be traitors, trying to prevent the loyal generals from reaching agreement.

These treacherous generals exhibit what we've come to call "Byzantine behaviour", or "Byzantine faults". They can act in any arbitrary way: delaying messages, reordering messages, outright lying, sending contradictory messages to different recipients, failing to respond at all, or any other behaviour we can think of.

The loyal generals need a method that reliably delivers an outcome on the following terms.



I receive a ton of messages from other nodes, but I have no idea which are accurate, what order they were sent in, or if any are missing or just delayed. Somehow, we need to reach agreement.

- A. All loyal generals decide upon the same plan of action [e.g. "attack" or "retreat"], and
- B. A small number of traitors cannot cause the loyal generals to adopt a bad plan.

Achieving consensus in such a Byzantine distributed system is not an easy problem to solve, but there have been several reasonably successful approaches over the years.

The first mainstream solution was the Practical Byzantine Fault Tolerance (PBFT) algorithm published by Liskov and Castro in 1999. This relies on a relatively small and limited set of known consensus participants (called *replicas*). PBFT is always "safe", in the terms discussed below and does not have forks.

Nakamoto consensus, invented by Satoshi Nakamoto for Bitcoin in 2008, takes a fundamentally different approach. Rather than limiting participants to a known set it uses proof of work to permissionlessly select a temporary leader for the consensus. Unlike PBFT, Nakamoto consensus allows forks and is not formally "safe".

Many, many variants of these and other novel alternatives, such as the Avalanche family of protocols, have since sprung up. Section 7, Related Work, of the Avalanche white paper provides a good survey of the zoo of different consensus protocols currently in use in the blockchain world.

Proof of Stake and Proof of Work

This is a good point at which to mention that neither proof of work nor proof of stake is a consensus protocol in itself. They are often (lazily) referred to as consensus protocols, but each is merely an enabler for consensus protocols.

For the most part, both proof of work and proof of stake are Sybil resistance mechanisms that place a cost on participating in the protocol. This prevents attackers from overwhelming the protocol at low or zero cost.²

Nevertheless, both proof of work and proof of stake are often fairly tightly coupled, via fork choice rules, to the consensus mechanisms that they support. They provide a useful way to assign a weight, or a score, to a chain of blocks: in proof of work, the total work done; in proof of stake, the amount of value that supports a particular chain.

Beyond these basic factors, both proof of work and proof of stake enable many kinds of different consensus protocols to be built on them, each with its own dynamics and trade-offs. Once again, the survey in section 7, Related Work, of the Avalanche white paper is instructive.

Block chains

The basic primitive that underlies blockchain technology is, of course, the block.

²In proof of work, the "proof" you bring is a number that makes the block hash a certain value. This proves that you did the work to calculate it. In proof of stake, your proof is a private key that is associated with a deposit of stake on the blockchain. Other proof mechanisms are available, such as proof of space and time.

A block comprises a set of transactions that a leader (the block proposer) has assembled. A block's contents (its payload) may vary according to the protocol.

- The payload of a block on Ethereum's execution chain is a list of user transactions.
- The payload of a block on the pre-Merge proof of stake beacon chain was (mostly) a set of attestations made by other validators.
- Post-Merge beacon chain blocks also contain the execution payload (the user transactions).
- As and when EIP-4844 is implemented on Ethereum, blocks will contain commitments to opaque blobs of data alongside the ordered list of user transactions.

Except for the special Genesis block, every block builds on and points to a parent block. Thus, we end up with a chain of blocks: a blockchain. Whatever the contents of blocks, the goal of the protocol is for all nodes on the network to agree on the same history of the blockchain.



A blockchain. Time moves from left to right and, except for the Genesis block, each block points to the parent block it builds on.

The chain grows as nodes add their blocks to its tip. This is accomplished by temporarily selecting a "leader", an individual node that has the right to extend the chain. In proof of work the leader is the miner that first solves the proof of work puzzle for its block. In Ethereum's proof of stake the leader is selected pseudo-randomly from the pool of active stakers.

The leader (usually known as the block proposer) adds a single block to the chain, and has full responsibility for selecting and ordering the contents of that block, though its block must be valid according to the protocol rules otherwise the rest of the network will simply ignore it.

The use of blocks is an optimisation. In principle we could add individual transactions to the chain one by one, but that would add a huge consensus overhead. So blocks are batches of transactions, and sometimes people argue about how big those blocks should be. In Bitcoin, the block size is limited by the number of bytes of data in the block. In Ethereum's execution chain, the block size is limited by the block gas limit (that is, the amount of work needed to run the transactions in the block). Beacon block sizes are limited by hard-coded constants.

Block trees

Our neat diagram of a nice linear chain will for the most part reflect what we see in practice, but not always. Sometimes, due perhaps to network delays, or a dishonest block proposer, or client bugs, any particular node might see something more like the following.

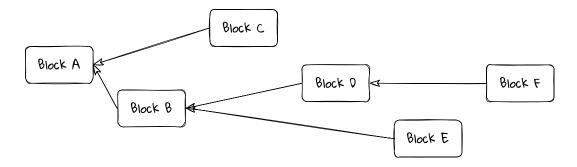
In real networks we can end up with something more like a block tree than a block chain. In this example very few blocks are built on their "obvious" parent.

Why did the proposer of block C build on A rather than B?

- It may be that the proposer of C had not received block B by the time it was ready to make its proposal.
- It may be that the proposer of C deliberately wanted to exclude block B from its chain, for example to steal its transactions, or to censor some transaction in B.
- It may be that the proposer of C thought that block B was invalid for some reason.

The first two reasons, at least, are indistinguishable to the wider network. All we know is that C built on A, and we can never know why for certain.

Similarly, why did the proposer of block D build on B rather than C? Any of the above reasons apply, and we can add another:



In general, we might end up with a block tree rather than a block chain. Again, time moves from left to right and each block points to the parent block it builds on.

• The proposer of D may have decided on some basis that there was more chance of the wider network eventually including B than C. Thus, building D on B gives it more chance of making it into the eventual block chain, than building D on C.

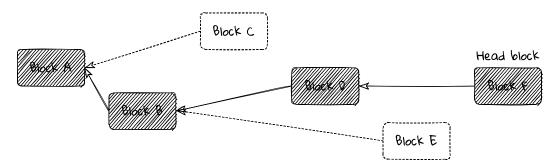
The various branches in the block tree are called "forks". Forks happen naturally as a consequence of network and processing delays. But they can also occur due to client faults, malicious client behaviour, or protocol upgrades that change the rules, making old blocks invalid with respect to the new rules. The last of these is often called a "hard fork".

The existence of forking in a consensus protocol is a consequence of prioritising liveness over safety, in the terms discussed below: if you were to consult nodes that are following different forks they would give you different answers regarding the state of the system. Non-forking consensus protocols exist, such as PBFT in the classical consensus world and Tendermint in the blockchain world. These protocols always produce a single linear chain and are thus formally "safe". However, they sacrifice liveness on asynchronous networks such as the Internet: rather than forking, they just stop entirely.

Fork choice rules

As we've seen, for all sorts of reasons – network delays, network outages, messages received out of order, malicious behaviour by peers – nodes across the network end up with different views of the network's state. Eventually, we want every correct node on the network to agree on an identical linear view of history and hence a common view of the state of the system. It is the role of the protocol's *fork choice rule* to bring about this agreement.

Given a block tree and some decision criteria based on a node's local view of the network, the fork choice rule is designed to select, from all the available branches, the one that is most likely to eventually end up in the final linear, canonical chain. That is, it will choose the branch least likely to be later pruned out of the block tree as nodes attempt to converge on a canonical view.



The fork choice rule selects a head block from among the candidates. The head block identifies a unique linear block chain running back to the Genesis block.

The fork choice rule selects a branch implicitly by choosing a block at the tip of a branch, called the head block.

For any correct node, the first criterion for any fork choice rule is that the block it chooses must be valid according to the protocol's rules, and all its ancestors must be valid. Any invalid block is ignored, and any blocks built on an invalid block are themselves invalid.

Given that, there are many examples of different fork choice rules.

- The proof of work protocols in Ethereum and Bitcoin use a "heaviest chain rule" (sometimes called "longest chain", though that's not strictly accurate). The head block is the tip of the chain that represents the most cumulative "work" done under proof of work.
- The fork choice rule in Ethereum's proof of stake Casper FFG protocol is "follow the chain containing the justified checkpoint of the greatest height", and to never revert a finalised block.
- The fork choice rule in Ethereum's proof of stake LMD GHOST protocol is specified in its name: take the "Greediest Heaviest Observed SubTree". It involves counting accumulated votes from validators for blocks and their descendent blocks. It also applies the same rule as Casper FFG.

We will properly unpack the second and third of these later in their respective sections.

You can perhaps see that each of these fork choice rules is a way to assign a numeric score to a block. The winning block, the head block, has the highest score. The idea is that all correct nodes, when they eventually see a certain block, will unambiguously agree that it is the head and choose to follow its branch whatever else is going on in their own views of the network. Thus, all correct nodes will eventually agree on a common view of a single canonical chain going back to genesis.

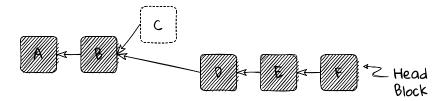
Reorgs and reversions

As a node receives new blocks (and, under proof of stake, new votes for blocks) it will re-evaluate the fork choice rule in the light of the new information. Most commonly, a new block will be a child of the block that the node currently views as the head block, and the new block will become the head block.

However, sometimes the new block might be a descendent of some other block in the block tree. (Note that, if the node doesn't already have the parent block of the new block, it will need to ask its peers for it, and so on for any blocks it knows that it is missing.)

In any case, running the fork choice rule on the updated block tree might indicate a head block that is on a different branch from the previous head block. When this happens, the node must perform a reorg (short for reorganisation), also known as a reversion. It will kick out (revert) blocks that it had previously included in its chain, and will adopt the blocks on the new head's branch.

In the following diagram, the node has evaluated block F to be the head block, hence its chain comprises blocks A, B, D, E, and F. The node knows about block C, but it does not appear in its view of the chain; it is on a side branch.



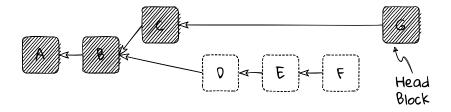
At this point, the node believes that block F is the best head, and therefore its chain is blocks $[A \leftarrow B \leftarrow D \leftarrow E \leftarrow F]$.

³Contrary to popular belief, Ethereum's proof of work protocol did not use any form of GHOST in its fork choice. This misconception is very persistent, probably due to the Ethereum Whitepaper. I eventually asked Vitalik about it, and he confirmed to me that although GHOST had been planned under PoW it was never implemented due to concerns about some unspecified attacks. The heaviest chain rule was simpler and well tested. It served us well.

Some time later the node receives block G which is not built on its current head block F, but on block C on a different branch. Depending on the details of the fork choice rule, the node might still evaluate F to be a better head than G and therefore ignore G. But in this case we will assume that the fork choice rule indicates that G is the better head block.

Blocks D, E, and F are not ancestors of G, so they need to be removed from the node's canonical chain. Any transactions or information those blocks contain will be reverted, as if they were never received. The node must perform a full rewind to the state that it was in after processing block B.

After rewinding to B, the node can add blocks C and G to its chain and process them accordingly. Once done, the node will have completed the reorganisation of its chain.



Now the node believes that block G is the best head, and therefore its chain must change to the blocks $[A \leftarrow B \leftarrow C \leftarrow G]$.

Later, perhaps, a block H might appear that builds on F. If the fork choice rule indicates that H ought to be the new head, then the node will perform a reorg once again, reverting blocks back to B and replaying the blocks on H's branch.

Short reorgs of one or two blocks in both proof of work and Ethereum's proof of stake protocol are not uncommon due to network delays in block propagation. Much longer reorgs ought to be exceedingly rare, unless the chain is under attack, or there is a bug in the formulation of - or the clients' implementations of - the fork choice rule.

Safety and Liveness

Two important concepts that crop up frequently when discussing consensus mechanisms are *safety* and *liveness*.

Safety

Informally, an algorithm is said to be safe if "nothing bad ever happens".

Examples of bad things that might happen in the blockchain context could be the double-spend of a coin, or the finalising of two conflicting checkpoints.

An important facet of safety in a distributed system is "consistency". That is, if we were to ask different (honest) nodes about the state of the chain at some point in its progress, such as the balance of an account at a particular block height, then we should always get the same answer, no matter which node we ask. In a safe system, every node has an identical view of the history of the chain that never changes.

Effectively, safety means that our distributed system "behaves like a centralized implementation that executes operations atomically one at a time." (to quote Castro and Liskov). A safe system is, in Vitalik's taxonomy of centralisation, logically centralised.

Liveness

Again informally, an algorithm is said to be live if "something good eventually happens".

⁴The helpful, intuitive definitions of safety and liveness I've quoted appear in short form in Lamport's 1977 paper, Proving the Correctness of Multiprocess Programs, and as stated here in Gilbert and Lynch's 2012 paper, Perspectives on the CAP Theorem.

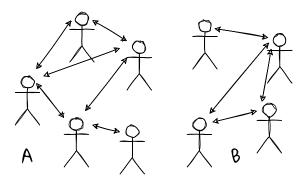
In a blockchain context we generally understand this to mean that the chain can always add a new block; it will never get into a deadlock situation in which it will not produce a new block with transactions in it.

"Availability" is another way of looking at this. I want the chain to be available, meaning that if I send a valid transaction to an honest node it will eventually be included in a block that extends the chain.

You can't have both!

The CAP theorem is a famous result in distributed systems' theory that states that no distributed system can provide all three of (1) consistency, (2) availability, and (3) partition tolerance. Partition tolerance is the ability to function when communication between nodes is not reliable. For example, a network fault might split the nodes into two or more groups that can't communicate with each other.

It is easy to demonstrate the CAP theorem in our blockchain context. Imagine that Amazon Web Services goes offline, such that all the AWS hosted nodes can communicate with each other, but none can talk to the outside world. Or that a country firewalls all connections in and out so that no gossip traffic can pass. Either of these scenarios divide the nodes into two disjoint groups, A and B.



The network is partitioned: the nodes in A can talk among themselves, but cannot talk to any node in B, and vice versa.

Let's say that somebody connected to the network of group A sends a transaction. If the nodes in A process that transaction then they will end up with a state that is different from the nodes in group B, which didn't see the transaction. So, overall, we have lost consistency between all the nodes, and therefore safety. The only way to avoid this is for the nodes in group A to refuse to process the transaction, in which case we have lost availability, and therefore liveness.

In summary, the CAP theorem means that we cannot hope to design a consensus protocol that is both safe and live under all circumstances, since we have no option but to operate across an unreliable network, the Internet.⁵

Ethereum prioritises liveness

The Ethereum consensus protocol offers both safety and liveness in good network conditions, but prioritises liveness when things are not running so smoothly. In the case of a network partition the nodes on each side of the partition will continue to produce blocks. However, finality (a safety property) will no longer occur on both sides of the partition. Depending on the proportion of stake managed by each side, either one side or neither side will continue to finalise.

Eventually, unless the partition is resolved, both sides will regain finality due to the novel inactivity leak mechanism. But this results in the ultimate safety failure. Each chain will finalise a different history and the two chains will become irreconcilable and independent forever.

⁵The CAP theorem is related to another famous result described by Fisher, Lynch and Paterson in their 1985 paper, Impossibility of Distributed Consensus with One Faulty Process, usually called the FLP theorem. This proves that, even in a reliable asynchronous network (that is, with no bound on how long messages can take to be received), just one faulty node can prevent the system from coming to consensus. That is, even this unpartitioned system cannot be both live and safe. Gilbert and Lynch's paper discusses the FLP theorem in section 3.2.

Finality

We're going to be discussing finality a good deal over the following sections, which is a safety property of the chain.

Finality is the idea that there are blocks that will never be reverted. When a block has been finalised, all the honest nodes on the network have agreed that the block will forever remain part of the chain's history, and therefore that all of its ancestors will remain in the chain's history. Finality makes your payment for pizza as irrevocable as if you'd handed over cash. It is the ultimate protection against double-spending.⁶

Some consensus protocols, like classical PBFT, or Tendermint, finalise every round (every block). As soon as a round's worth of transactions has been included on the chain, all the nodes agree that it will be there forever. On the one hand, these protocols are very "safe": once a transaction has been included on-chain, it will never be reverted. On the other hand, they are vulnerable to liveness failures: if the nodes cannot come to agreement – for example, if more than one third of them are down or unavailable – then no transactions can be added to the chain and it will stop dead.

Other consensus protocols, such as Bitcoin's Nakamoto consensus, do not have any finality mechanism at all. There is always the possibility that someone will reveal an alternative, heavier chain. When this happens, all honest nodes must reorg their chains accordingly, reverting whatever transactions they previously processed. Heuristics such as how many confirmations your block has are only approximations to finality, they are not guarantees.⁷

Ethereum's consensus layer prioritises liveness, but also strives to offer a safety guarantee in the form of finality when circumstances are favourable. This is an attempt to gain the best of both worlds. Vitalik has defended this as follows.⁸

The general principle is that you want to give users "as much consensus as possible": if there's > 2/3 then we get regular consensus, but if there's < 2/3 then there's no excuse to just stall and offer nothing, when clearly it's still possible for the chain to keep growing albeit at a temporarily lower level of security for the new blocks. If an individual application is unhappy with that lower level of security, it's free to ignore those blocks until they get finalized.

Finality in Ethereum's consensus layer is delivered by the Casper FFG mechanism that we'll be exploring soon. The idea is that, periodically, all honest validators agree on fairly recent checkpoint blocks that they will never revert. That block and all its ancestor blocks are then "final" - they will never change, and if you consult any honest node in the network about them or their ancestors you will always get the same answer.

Ethereum's finality is "economic finality". It is theoretically possible for the protocol to finalise two conflicting checkpoints, that is, two contradictory views of the chain's history. However, it is possible only at enormous and quantifiable cost. For all but the most extreme attack or failure scenarios, final means final.

The section on Casper FFG dives into the detail of how this finality mechanism works.

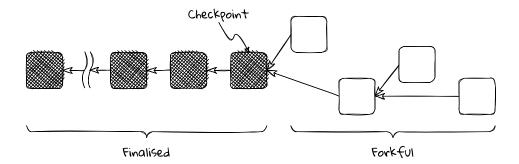
See also

It's always worth reading anything that Leslie Lamport has had a hand in, and the original 1982 paper by Lamport, Shostak, and Pease on The Byzantine Generals Problem contains many insights. While the algorithm they propose is hopelessly inefficient in modern terms, the paper is a good introduction

⁶It's worth noting that finality is never absolute. Whatever any protocol claims, if a supermajority of nodes agrees (for example via a software upgrade) to revert a bunch of finalised blocks, then that's going to happen. Ultimately, as in all things, the concept of finality is subservient to social consensus. See On Settlement Finality for further discussion.

⁷At the time of writing, at least one exchange requires 40000 confirmations for deposits from the Ethereum Classic network. That means that forty thousand blocks must be built on top of a block containing the deposit transaction before the exchange will process it, which takes about six days. The requirement reflects concern about the vulnerability of ETC's low hash rate proof of work chain to 51% attacks - it is relatively easy for an attacker to revert blocks at will. The reality is that, in the face of a well-crafted 51% attack, no number of confirmations is truly safe.

⁸The value of this was evident when the beacon chain stopped finalising for around an hour on the 12th of May, 2023. Participation in consensus dropped from over 99% of validators to around 40% for the duration. Ordinary Ethereum users and applications, however, would have barely noticed. Blocks continued to be produced (albeit fewer than normal) and transactions continued to be executed.



The honest nodes have agreed that the checkpoint and all its ancestor blocks are "final" and will never be reverted. There are therefore no forks before the checkpoint. The chain descending from the checkpoint remains liable to forking.

to reasoning about consensus protocols in general. The same is true of Castro and Liskov's seminal 1999 paper Practical Byzantine Fault Tolerance which significantly influenced the design of Ethereum's Casper FFG protocol. However, you might like to contrast these "classical" approaches with the elegant simplicity of proof of work, as described by Satoshi Nakamoto in the 2008 Bitcoin white paper. If proof of work has just one thing in its favour, it is its simplicity.

We've referred above to Gilbert and Lynch's 2012 paper, Perspectives on the CAP Theorem. It is a very readable exploration of the concepts of consistency and availability (or safety and liveness in our context).

The Ethereum beacon chain underwent a seven block reorg in May 2022 due to differences between client implementations of the fork choice rule. These differences were known at the time and thought to be harmless. That proved to be not so. Barnabé Monnot's write-up of the incident is very instructive.

Vitalik's blog post On Settlement Finality provides a deeper and more nuanced exploration of the concept of finality.

Our ideal for the systems we are building is that they are *politically* decentralised (for permissionlessness and censorship resistance), *architecturally* decentralised (for resilience, with no single point of failure), but *logically* centralised (so that they give consistent results). These criteria strongly influence how we design our consensus protocols. Vitalik explores these issues in his article, The Meaning of Decentralization.

Overview

- Nodes and validators are the actors of the consensus system.
- Slots and epochs regulate consensus time.
- Blocks and attestations are the currency of consensus.
- $\bullet\,$ Ethereum's consensus protocol combines two separate consensus protocols.
- "LMD GHOST" essentially provides liveness.
- "Casper FFG" provides finality.
- Together they are sometimes known as "Gasper".

Introduction

The last section gave a broad view of blockchain consensus; in this section we will tighten the focus to Ethereum's proof of stake consensus. I've tried to follow a path that gives enough information to make sense of things, without wandering off into the detailed technical weeds on either side. All those weeds are well explored in the annotated specification and other chapters, and I've included some links for those who want to branch off and go exploring.

The first thing we must cover is the Ethereum-specific terminology that we will be using throughout.

Nodes and Validators

The main participants in the Ethereum network are *nodes*. A node's role is to validate consensus and form the communication backbone with other nodes.

Consensus is formed by *validators*, which (in true Ethereum style) are horribly misnamed, as they don't really validate anything - that's done by the nodes. Each validator represents an initial 32 ETH stake. It has its own secret key, and the related public key that is its identity in the protocol. Validators are attached to nodes, and a single node can host anything from zero to hundreds or thousands of validators. Validators attached to the same node do not act independently, they share the same view of the world.⁹

A interesting feature of proof of stake that sets it apart from proof of work is that, under PoS, we know our validator set. We have a complete list of all the public keys that we expect to be active at any time. Knowing our validator set enables us to achieve finality, as we can identify when we have achieved a majority vote of participants.¹⁰

Slots and Epochs

Time is strictly regimented in Ethereum's proof of stake consensus, which is a major change from proof of work, which only had casual relationship with time - PoW makes some attempt to keep block intervals constant on average, but that's all.

The two most important intervals are the *slot*, which is 12 seconds exactly, and the *epoch*, which is 32 slots, or 6.4 minutes. Slots and epochs progress regularly and relentlessly, whatever else may be happening on the network.

Blocks and Attestations

Every slot, exactly one validator is selected to propose a *block*. The block contains updates to the beacon state, including attestations that the proposer knows about, as well as the execution payload containing Ethereum user transactions. The proposer shares its block with the whole network via a gossip protocol.

A slot can be empty: a block proposer might be offline, or propose an invalid block, or have its block subsequently reorged out of the chain. These things should not happen often in a well-running beacon chain, but the protocol is intended to be robust when empty slots occur.

Every epoch, every validator gets to share its view of the world exactly once, in the form of an *attestation*. An attestation contains votes for the *head* of the chain that will be used by the LMD GHOST protocol, and votes for *checkpoints* that will be used by the Casper FFG protocol. Attestations are also gossiped to the whole network. Like blocks, attestations can be missing for all sorts of reasons, and the protocol can tolerate this to various extents - crudely, the quality of consensus will decrease as the participation rate of attesters decreases.¹¹

The function of the epoch is to spread out the workload of handling all those attestations. By attesting, every validator is informing every other validator of its view of the world, which could amount to an

⁹It would serve us well to be mindful of this when making claims about the decentralisation of Ethereum. Having, say, 600,000 validators active on the network is a long way from having 600,000 independent actors. Looking at the number of nodes, and the distribution of validators across nodes, will give more useful metrics for Ethereum's decentralisation.

¹⁰In consensus jargon, we can have "accountable safety".

¹¹The Beaconcha.in site shows attestation participation rate (also called Voting Participation) on a per epoch basis. It is a good measure of network health. The rate often exceeds 99%, which is an outstanding level of performance for a massively distributed consensus protocol.

immense amount of network traffic and processing load if it were all done at once. Spreading the attestation workload across all 32 slots of an epoch keeps resource usage low. In each slot, committees comprising only $\frac{1}{32}$ of the validators make attestations.

The protocol incentivises block and attestation production and accuracy via a system of rewards and penalties for validators. We don't need to go into these now; there is a whole separate chapter on all of that.

Slashing

In proof of work, producing a block is expensive. This is a strong incentive for miners to behave well, in line with the protocol's goals, to ensure that their blocks are included.

In proof of stake, creating blocks and attestations is almost free¹². We need a way to prevent attackers from exploiting this to disrupt the network. This is the role of *slashing*. Validators that equivocate over blocks or attestations are subject to being slashed, which means that they are ejected from the validator set and fined some portion of their stake. Simply put, equivocation means saying two contradictory things. It might be proposing two different blocks for the same slot, or making two attestations that are inconsistent with each other, that no validator honestly following the protocol would have made.

The Ghosts in the Machine

With some terminology behind us we can begin to outline Ethereum's actual consensus mechanism.

Ethereum's proof of stake consensus protocol is actually a combination of two separate consensus protocols, known individually as LMD GHOST¹³, and Casper FFG¹⁴. These two have been "bolted together" to form the consensus protocol we have implemented for Eth2 - the combined protocol is sometimes known by the portmanteau "Gasper".

Combining the two in Gasper is an attempt to get the best of both worlds in terms of liveness and safety. In essence, LMD GHOST provides slot-by-slot liveness (it keeps the chain running), while Casper FFG provides safety (it protects the chain from long reversions). LMD GHOST allows us to keep churning out blocks on top of one-another, but is forkful and therefore not formally safe. Casper FFG modifies the LMD GHOST fork choice rule to periodically bless the chain with finality. Nevertheless, as previously discussed, Ethereum prioritises liveness. Therefore, in situations in which Casper FFG is unable to confer finality, the chain still continues to grow via the LMD GHOST mechanism.

This bolted-together consensus mechanism is not always pretty. We can sometimes see the joins, and the interaction between the two has led to subtle issues that we will discuss later. However, in the spirit of Ethereum, it is a workable engineering solution that serves us well in practice.

History

The detailed history of Gasper is bound up with the development of the individual components, LMD GHOST and Casper FFG, which we will review in their respective sections. But we note here that Casper FFG was never designed to be a standalone consensus mechanism.

As stated in the Casper FFG paper,

Casper the Friendly Finality Gadget is an overlay atop a *proposal mechanism* – a mechanism which proposes blocks.

So, there is an underlying block proposal mechanism – which implies an underlying consensus mechanism – that Casper FFG sits on top of, delivering a kind of meta-consensus that confers finality on the blockchain.

The original plan was to apply Casper FFG as a proof of stake overlay on top of Ethereum's proof of work consensus. Casper FFG would confer finality – a property that proof of work chains lack – on

 $^{^{12}\}mathrm{This}$ is sometimes called the "nothing at stake problem".

¹³"Latest Message Driven, Greedy Heaviest Observed Subtree". I will unpack the naming in the specific LMD GHOST chapter.

^{14&}quot;Casper the Friendly Finality Gadget". Again, I will unpack this slightly curious naming when we get to the specific Casper FFG chapter.

the chain on a periodic basis, say, every 100 blocks. This was intended to be the first step in weaning Ethereum off proof of work. With the finality guarantee, we could have reduced the proof of work block reward, and thereby reduced the overall hash power as an interim step towards replacing mining with full proof of stake at some future date.

By the end of 2017, this plan had become quite advanced. EIP-1011, Hybrid Casper FFG, describes the architecture in detail, and there was even a testnet that went live on the 31st of December, 2017.

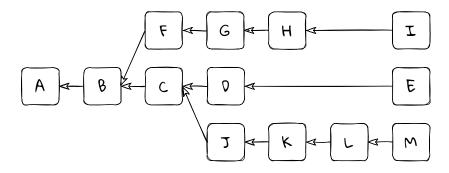
In early 2018, however, that plan was superseded. The limited bandwidth of the Ethereum Virtual Machine constrained the size of the validator set that EIP-1011 could support, in turn leading to a minimum stake of 1500 ETH, which was seen as undesirable. Around the same time, paths towards a full, much more scalable proof of stake protocol became clearer, and we began working on the design that became Ethereum 2.0.

Due to its generic nature, Casper FFG was able to survive the redesign and was adopted into Ethereum 2.0, not as an overlay on proof of work, but as an overlay on a new proof of stake protocol called LMD GHOST.

A finality gadget

When we say that Casper FFG overlays an existing block proposal mechanism, we mean that it takes an existing block tree and prunes it in a specific way. Casper FFG modifies the fork choice of the underlying block tree by making some of its branches inaccessible.

Consider this block tree produced by some underlying consensus mechanism, whether it be proof of work, or LMD GHOST in proof of stake.



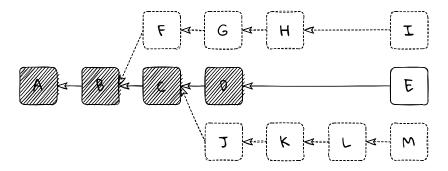
An arbitrary block tree with three forks (branches). Any of blocks I, E, or M could be the tip of the chain. (The block labels are for convenience and do not imply a particular ordering.)

In this situation, I have three candidate head blocks, I, E, and M. Under proof of work's longest chain rule, the choice of head block is obvious: I must choose M since it has the greatest block height, or (almost) equivalently the greatest amount of work done. Under LMD GHOST we can't choose a head block from this information alone, we'd need to see the votes from the other validators in order to make a choice.

The challenge is that the chain from blocks J to M might be from an attacker. The attacker might have mined that chain in secret and revealed it later in a so-called 51% attack. Proof of work nodes would have no choice but to reorg to make M the head, thereby favouring the attacker's chain and potentially becoming vulnerable to double-spends.

The value that Casper FFG brings is that it confers finality. Let's say that block D is marked as final by Casper FFG (which automatically finalises blocks A, B, and C). Finalisation modifies the fork choice rule of the underlying protocol so that any branch with blocks that competes with block D – that is, any block not descended from D – is excluded. Equivalently, branches are pruned so that there are no forks prior to the finalised block.

When block D is finalised, the fork choice must ignore the branches that begin with blocks F and J. We end up with a single candidate head block, E.



We have the same block tree as above, but now block D has been finalised. The Casper FFG fork choice says that any chain not including block D is ignored, so our head block is now unambiguously E.

Essentially, the finality delivered by Casper FFG prevents long reorganisations (reversions). No finalised block, or ancestor of a finalised block, will ever be reverted. In Ethereum's Casper FFG implementation we must qualify "ever", with, "without burning at least 1/3 of the entire amount of staked Ether". This is the economic finality that the proof of stake chain provides.

Conclusion

As a reminder, this is the sentence we are trying to understand in all its parts.

The Proof-of-Stake (PoS) Ethereum consensus protocol is constructed by applying the finality gadget Casper FFG on top of the fork choice rule LMD GHOST, a flavor of the Greedy Heaviest-Observed Sub-Tree (GHOST) rule which considers only each participant's most recent vote (Latest Message Driven, LMD).

We've spent some time on what a consensus protocol is and does, and touched a little on proof of stake. We talked about finality, and at a high level I've illustrated how Casper FFG forms a "finality gadget" applied on top of LMD GHOST as a block proposal mechanism.

Much work remains, however. In the next sections we will take deeper dives into LMD GHOST, Casper FFG, and how they combine to form the Gasper protocol.

See also

On the history of how everything came together, Vitalik made a terrific tweet storm. Consolidated versions are available here and here. He discusses weak subjectivity a little, which we will deal with later.

The Proof of Stake FAQ remains an excellent primer on many of the topics we'll be covering.

Joachim Neu's presentation, The Why and How of PoS Ethereum's Consensus Problem (at ETHconomics, Devconnect 2022), is a very accessible insight into the availability–finality trade-off, and how Ethereum seeks to manage it. We'll pick up again on the idea of "nested ledgers" when we get to the Gasper protocol.

LMD Ghost

- LMD GHOST is a fork choice rule used by nodes to determine the best chain.
- It assigns weights to branches based on votes from all active validators.
- LMD GHOST does not provide finality, but does support a confirmation

rule.

• Slashing is used to solve the "nothing at stake" problem.

Introduction

In this section we will consider LMD GHOST in isolation, ignoring completely the Casper FFG finality overlay¹⁵. LMD GHOST is the essence of a consensus mechanism in itself – it is a fork choice rule, just as the heaviest chain rule in Nakamoto consensus is – and has its own sets of properties and trade-offs.

For now, we will be considering only the "how it works" part of the story - the happy flow. We will look at the "how it can go wrong" part later, in the Issues and Fixes section.

Naming

The name LMD GHOST comprises two acronyms, for "Latest Message Driven", and "Greedy Heaviest-Observed Sub-Tree". We'll unpack GHOST first, then LMD.

GHOST

The GHOST protocol comes from a 2013 paper by Sompolinsky and Zohar about how to safely improve transaction throughput on Bitcoin. Increasing the block size, or decreasing the interval between blocks, makes the chain more susceptible to forking in a network that has uncontrolled latency (delays), like the Internet. Chains that fork have more reorgs, and reorgs are bad for transaction security. Replacing Bitcoin's longest chain fork choice rule with the GHOST fork choice was shown to be more stable in the presence of latency, allowing block production to be more frequent.

The name GHOST stands for "Greedy Heaviest-Observed Sub-Tree", which describes how the algorithm works. We will expand on that below. In short, GHOST's fork choice doesn't follow the heaviest chain, but the heaviest subtree. It recognises that a vote for a block is not only for that block, but implicitly a vote for each of its ancestors as well, so whole subtrees have an associated weight.

Bitcoin never adopted GHOST, and (despite that paper stating otherwise) neither did Ethereum under proof of work, although it had originally been planned, and the old proof of work "uncle" rewards were related to it.

LMD

The GHOST protocol that we are using in Ethereum's proof of stake has been extended to be able to handle attestations. In proof of work, the voters are the block proposers. They vote for a branch by building their own block on top of it. In our proof of stake protocol, all validators are voters, and each casts a vote for its view of the network once every 6.4 minutes on average by publishing an attestation. So, under PoS, we have a lot more information available about participants' views of the network.

This is what it means to be "message driven", giving us the MD in LMD. The fork choice is driven not by blocks added by proposers, but by messages (attestations, votes) published by all validators.

The "L" stands for "latest": LMD GHOST takes into account only the *latest* message from each validator, that is, the most recent attestation that we have received from that validator. All a validator's earlier messages are discarded, but its latest vote is retained and has weight indefinitely.

As a side note, other versions of message-driven GHOST are available. Vitalik initially favoured IMD, "Immediate Message Driven", GHOST. As far as I can tell¹⁶, this retains all attestations indefinitely, and the fork choice chooses based on whatever attestation was current at the time. Then there's FMD, "Fresh Message Driven", GHOST, which considers attestations only from the current and previous epochs. And

 $^{^{15}}$ The next section covers Casper FFG, and the one after that the combination of the two into Gasper.

¹⁶I've yet to find a lucid exposition of IMD GHOST. Looking back through the history on the original mini-spec gives some information, but it's hard to understand what was really happening. It was first known as "recursive proximity to justification", since it was bound up with Casper FFG in a way that LMD GHOST is not.

RLMD, "Recent Latest Message Driven", GHOST which remembers validators' latest attestations only for a parameterisable number of epochs.

How it works

LMD GHOST, above all, is a fork choice rule. Given a tree of blocks and a collection of votes, LMD GHOST will tell me which block I should consider to be the best head, thereby giving me a linear view of history from that head all the way back to genesis. The decision is based on my local view of the chain, based on the messages (blocks and attestations) that my node has received - remember, there is no "God's eye view", my local view is all that I have to work with, and it may well differ from other nodes' local views. The idea is that honest validators will build their blocks on the best head that they see, and will in turn cast their votes according the best head block they see.

Some things that a good fork choice rule will deliver are as follows.¹⁷

- Majority honest progress: if over 50% of nodes build blocks by following the fork choice rule, the chain progresses and is (exponentially) unlikely to revert older blocks.
- Stability: the fork choice is a good prediction of the future fork choice.
- Manipulation resistance: even if an attacker captures a temporary supermajority of some small set of participants, the attacker is unlikely to be able to revert blocks.

All these points are interrelated. Stability, in particular, is important for block proposers. When I propose a block, I want to be as sure as I possibly can be that the block will remain in the chain forever. Equivalently, that it will not be reorged out. Finding the head block means finding the block that most likely will make my new block the head in the views of other nodes when I build on it.

We'll divide our exploration of how LMD GHOST works in two. We'll look first at the LMD part, latest messages, and then at the GHOST part, finding the head.

Latest messages

Messages, in this context, are the head block votes found in attestations.

Votes in LMD GHOST

In an attestation's data, the head vote is the beacon_block_root field:

class AttestationData(Container):

slot: Slot
index: CommitteeIndex
LMD GHOST vote
beacon_block_root: Root
FFG vote

source: Checkpoint target: Checkpoint

Every honest validator makes an attestation exactly once per epoch, containing its vote for the best head block in its view at the moment that it attests. Within each epoch, the validator set is split up so that only 1/32 of the validators are attesting at each slot. (The index field in this structure relates to the attesting validators being further divided into up to 64 committees at each slot for operational reasons, but this is not relevant to the mechanics of LMD GHOST and we shall ignore it.)

Nodes receive attestations both directly, via attestation gossip, and indirectly, contained in blocks. In principle, a node could receive attestations through other means - I could type an attestation in at the keyboard if I wished - but in practice votes propagate only via attestation gossip and within blocks.

¹⁷I've adapted this from an old post of Vitalik's, PoS fork choice rule desiderata. I'm postponing his finality point for now. I am not aware of much formal analysis of LMD GHOST with respect to properties like these; in fact, our implementation of LMD GHOST may not do too well in some respects. But these goals are worth bearing in mind as we explore how the mechanism works.

Storing latest messages

On receiving an attestation, by whatever means, the node calls the fork choice's on_attestation() handler. Before proceeding, the on_attestation() handler performs some basic validity checks on the attestation:

- Is it too old?
 - It must be from the current or previous epoch. See Attestation consideration delay.
- Is it too new?
 - It must be from no later than the previous slot. See Attestation recency.
- Do we know about the block that it is voting for, the beacon_block_root?
 - We must have received that block already. If not we might try to fetch it from a peer.
- Is its signature correct?
 - Validators sign attestations and are accountable for them.
- Is the attestation slashable?
 - We must ignore attestations that conflict with other attestations. See Attestation equivocation.

After passing these and some other checks, the attestation is considered for insertion into the node's Store, which is its repository of information about the state of the chain: its view. This is done in update_latest_messages(). If we don't already have a head block vote for the validator, then this one is stored for it. If we have a head block vote for the validator, then this one replaces it if it is more recent.

Over time, then, a node's Store builds up a list containing a single latest vote for each validator that it has heard from.

Note that a vote can be inserted in the store only if we heard about it in the same epoch or the epoch after it was made. However, once it is in the store it remains there indefinitely, and continues to contribute to the fork choice until it is updated with a more recent vote. This is a key difference between LMD GHOST and, say, the Goldfish protocol, or RLMD GHOST.

Finding the head block

In essence, the LMD GHOST fork choice rule is a function $GetHead(Store) \rightarrow HeadBlock$. As we've seen, a node's Store is its view of the world: all the relevant information it has received that could affect the fork choice. For the pure LMD GHOST algorithm we are looking at here, the relevant parts of the Store are the following.

- The block tree, which is just a list of blocks. The blocks' parent links join them logically into a tree
- The list of latest messages (votes) from validators.
- The validators' effective balances (based on some state) as these provide the weights used in the algorithm.

The goal of the GHOST algorithm is to select a single leaf block from the given block tree, where a leaf is a block without any descendants. This will be our chosen head block.

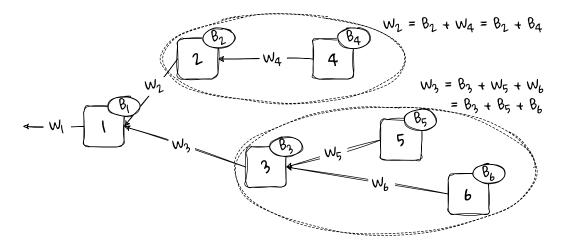
We are going to assume that all the blocks in our block tree descend from a single root block. In a pure GHOST algorithm, that would be the genesis block: by definition, all blocks must descend from genesis. In our full consensus implementation, that root block will be the last justified checkpoint block. For our present purposes, all we need to know is that the GHOST algorithm starts from a given block, and ignores all blocks not descended from that block.

Get weight

The first thing we do is calculate the "weight" of each branch in the tree. A branch's weight is its score, in some sense.

The weight of a vote is the effective balance of the validator that made the vote. This will usually be 32 ETH, the maximum effective balance, but could be less. A vote, recall, is the latest message we have from that validator.

The weight of a branch is the weight of the votes for the block that roots it, plus the weights of that block's child branches. By including the weights of child branches, we are acknowledging that a vote for a block is also a vote for each of the ancestors of that block. The weight of a branch consisting of only a leaf block will be just the weight of the votes for that block.



 B_N is the sum of the effective balances of the validators whose most recent head vote was for block N, and W_N is the weight of the branch rooted at block N.

Some obvious relationships apply between the weights, W_x , of branches, and B_x , the weights of the votes for blocks.

- For a branch comprising only a leaf block, $L, W_L = B_L$.
- The weight of a branch is the weight of the votes for the block at its root plus the sum of the weights of all branches below it. So, in the diagram, $W_1 = B_1 + W_2 + W_3$.
- The weight of a branch is the sum of the weights of all votes for blocks in the subtree that forms the branch.

Since votes always carry a positive weight, no block will have a greater weight than the root block, and the root block's weight is the sum of the weights of all the votes for blocks in the tree. Every validator has at most one latest message – that is, one vote –, so that weight is bounded above by the total effective balance of all active validators.¹⁸

Get head

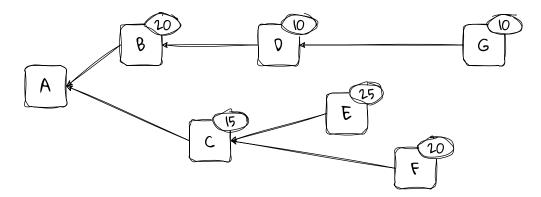
Once we have the weight of each branch or subtree, the algorithm proceeds recursively. Given a block, we select the heaviest branch descending from it. We then repeat the process with the block at that branch's root. If a block has only one child, then the choice is obvious and there is no work to do. If two or more branches have equal weight, we arbitrarily choose the branch rooted at the child block with the highest block hash value. Eventually we will reach a block with no children. This is a leaf block and will be the output of the algorithm.

Unpacking the GHOST name, we see that the algorithm: is Greedy, meaning that it takes the Heaviest-Observed branch immediately, without looking further; and deals with Sub-Trees, the weight of a branch being the sum of all the weights of votes for blocks in the subtree.

Here's a simple example. In the diagrams, I've distinguished between (1) the weight of the votes for a particular block, which are the numbers attached to each block, and (2) the weights of branches, which I've added to the lines joining the blocks to their parents.

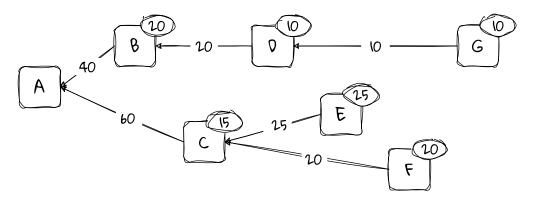
¹⁸Ignoring proposer boost, which we shall deal with later.

First, from the latest messages in the Store, we calculate the weight of votes for each block in the tree.



 $get_head()$ starts from the root block, A, of a block tree. The numbers show the weights of the votes for each block.

Second, from the weights of votes for each block, we can calculate the weight of each branch or subtree.



The get_weight() function when applied to a block returns the total weight of the subtree of the block and all its descendants. These weights are shown on the lines between child and parent blocks.

Third, we move recursively through the blocks at the roots of the subtrees, always choosing the branch or subtree with the highest weight. Eventually, we will reach a leaf, which is our chosen head block.

If, say, the subtrees rooted at B and C had equal weight, we would choose according to which of blocks B and C had the greatest block hash - this is a completely arbitrary tie-break mechanism.

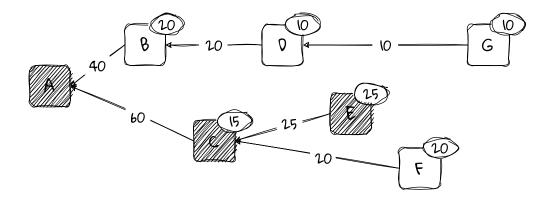
The specification

The code that implements all this in the specification is get_head(), which walks up through the tree from the root, taking the heaviest branch at each fork. The code for calculating the weight of a subtree is get_weight().

If you look at the <code>get_weight()</code>, you'll find that it is more complex than what we've covered here, due to something called "proposer boost". We shall discuss proposer boost in detail in the Issues and Fixes section.

Intuition

Having seen how the GHOST protocol works, it's perhaps easier to gain some intuition for why we prefer it to a longest chain rule. The occurrence of forks suggests that block propagation time has become of



At block A, branch C is heavier. At C, branch E is heavier. Block E is a leaf block, so it is GHOST's choice for the head of the chain. Our blockchain is $[A \leftarrow C \leftarrow E]$. A "longest chain" rule would have chosen block G, although that branch has minority support from validators.

similar order to, or exceeds, block production intervals (slots). In short, not all validators are seeing all the blocks in time to attest to them or to build on them.¹⁹

In these circumstances, we want to take advantage of the maximum amount of information available. Votes for two different children of the same parent block should be taken as confirmation that all those validators favour the parent block's branch, even if there is disagreement about the child blocks. GHOST achieves this simply by allowing a vote for a child block to add weight to all of its ancestors. Thus, when faced with a choice, we favour the branch with the greatest total support from validators. I've illustrated this in the diagram above: branch C is favoured over branch B, even though block B has more direct votes than block C, since more validators overall made latest votes for branch C.

The longest chain rule discards all this information, and can allow a branch to win even if only a minority of validators has been working on it.

Confirmation rule

In proof of work, the only data available for input into the fork choice comes from block production, which represents the view of a single miner at the time of publishing the block.

In Ethereum's proof of stake protocol, we have vastly more information available to us, in the form of head block votes from $\frac{1}{32}$ of the validator set every 12 seconds, in addition to the block proposer's view.

In principle, all this extra information ought to allow us to be very sure, very quickly, about whether blocks will remain canonical or are in danger of being reverted. Proof of work chains tend to use a heuristic around the number of confirmations that a block has received. That is, blocks are assumed to be exponentially less likely to be reverted the more blocks have been built on top of them. This is generally true, but can fail badly in high-latency environments (such as an attacker making a longer chain in secret).

Proof of stake's ultimate answer to this is finality, which we shall look at in the next section. LMD GHOST on its own does not provide finality. However, it's interesting to consider whether there is some heuristic analogous to proof of work's confirmations rule that we can use, and it turns out that there is. In fact, it improves on the PoW confirmation rule by giving a "yes/no" statement about the safety of a block, rather than a probability.

The details of the confirmation rule are described by Aditya Asgaonkar in a blog post and an accompanying paper. The general idea is that, for a block b, we calculate two values q and q_{\min} . When $q > q_{\min}$, and the network remains close to synchronous, then that block is confirmed as "safe". We can be fully confident that it will not be reorged.

¹⁹See Vitalik's Toward a 12-second block time for a fascinating analysis of this in a proof of work context. However, not much of it carries over to our PoS implementation, except that GHOST helps to make sense of a forkful network.

The quantity q_b^n is defined as the weight of the subtree rooted at b at slot n divided by the total weight of votes cast since b was produced. Simply put, if, in the slots since b was proposed, 80% of validators voted for b or a descendant of b, then q_b^n would be 0.8.

 q_{\min} is defined as $\frac{1}{2} + \beta$, where β is the fraction of stake we believe is controlled by an adversary. This fraction is unknown, but is assumed to be less than one third, otherwise we have big problems.

Now, if $q_{b'}^n > q_{\min}$ for b and all its (non-finalised) ancestors, b', then b is considered to be confirmed, or "safe".

The idea is that, once a branch up to block b has accumulated a simple majority of the available voting weight, then all honest validators will continue to vote for that branch, so it will maintain its majority indefinitely. One way this can fail is if dishonest validators swap their votes to another branch, giving that branch a majority instead. That's why we add a fraction β to the basic majority safety parameter of $\frac{1}{2}$, so that, even if all the dishonest validators swap branches, our branch maintains a majority. The other way this can fail is if the network begins to suffer delays or partitions (loses synchrony), so that some honest validators cannot see other honest validators' votes, hence the reliance on the network remaining sufficiently synchronous.

While this seems very intuitive, there are some important subtleties and complications related to the integration with Casper FFG that modify the confirmation rule, so anyone dealing with this should consult the full paper (which remains a draft). In addition, proposer boost makes it easier for an adversarial block proposer to reorg a block, so we need to account for that as well.

The table below summarises the differences between the confirmation rule and finality for a block.

	Confirmation	Finality
Time	One slot in ideal circumstances, less than a minute more generally.	At least two epochs / 13 minutes.
Assumptions	Network remains synchronous until finality.	No synchrony assumption.
Breakage	A confirmed block can be reorged if the network does not remain synchronous.	A conflicting block can be finalized if more than $\frac{1}{3}$ of the validators commit a slashable action.

The confirmation rule is not yet implemented in client software as I write, but should be available in due course via the safe block specification.

Incentives in LMD GHOST

One of the ways cryptoeconomic systems secure themselves is by rewarding good behaviour and penalising bad behaviour. In our implementation of LMD GHOST, both proposers and attesters are rewarded in different ways for accurately finding the head of the chain.

The incentive for a block proposer to build on the best head is clear. If it doesn't, then there's a good chance that its block will not be included in the eventual canonical chain – it will be orphaned – in which case the proposer will not receive any of its block rewards. This is an implicit incentive rather than explicit; miners in proof of work are in a similar situation.

By contrast, validators are directly rewarded for voting accurately. When a validator makes an accurate head vote, and its attestation is included in a block in the very next slot, it receives a micro reward. A perfectly performing validator will gain about 22% of its total protocol rewards from making accurate head votes. Proposers, in turn, are incentivised to include such attestations in blocks as they receive a proportionate micro, micro reward for each one they manage to get in.

A vote is accurate if it matches what ends up in the canonical chain. So if the validator voted for a block at the previous slot, and the canonical chain has a matching block there, then it receives its reward. If it voted for a block from a previous slot, indicating a skipped slot, and the canonical chain has skipped slots between that block and the present, then it will also receive its reward.

There is no penalty if a validator makes an inaccurate head vote, or their head vote is not included on chain within one slot. Getting the head vote right is difficult when the beacon chain is under stress, and there are late and missing blocks. This is often no fault of the validator itself, and it was felt unfair to penalise them in such circumstances.²⁰

Slashing in LMD GHOST

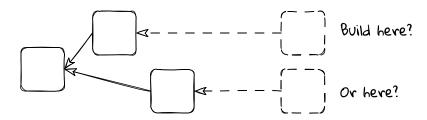
One of the big breakthroughs in proof of stake design was the adoption of slashing as a way around the "nothing at stake" problem. The problem, in essence, is that under proof of stake it is almost costless for a validator to equivocate by publishing multiple contradictory messages.

The solution turns out to be rather elegant. We detect when a validator has equivocated and punish it. The punishment is called "slashing", and entails removing a proportion of the validator's stake, and ejecting the validator from the protocol. Since validators digitally sign their messages, finding two contradictory signed messages is absolute proof of misbehaviour, so we can slash with confidence.

The name "slashing" comes from Vitalik's Slasher algorithm from early 2014. That was a very early proposal for solving the nothing at stake problem. Our current design doesn't look much like Slasher, but some things have carried over, not least the name.

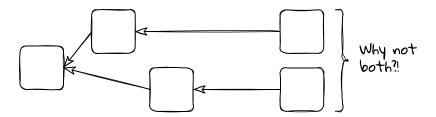
Proposer slashing

When it is a validator's turn to produce a block in a particular slot, the validator is supposed to run the fork choice rule in order to decide which existing block it will build its own block on. Its goal is to identify the fork that is most likely, based on the evidence it has, to be the one that eventually becomes canonical. That is, the one that the whole set of correct validators will converge on.



The proposer of a block needs to choose which block to build on. The best strategy is to build on the block least likely to be reorged, as indicated by the fork choice rule.

However, why choose? Under proof of stake – unlike under proof of work – it is almost costless for validators to produce blocks. Therefore, a good strategy would seem to be to propose multiple blocks, one built on each possible head, then at least one of my blocks is guaranteed to become part of the eventual canonical chain.



In the absence of punishment, a lazy or dishonest proposer might choose to extend both sides of the fork.

²⁰The original Phase 0 specification did have a penalty for a missed head vote. This was removed in the Altair upgrade's accounting reforms.

This is undesirable because it prolongs any fork and prevents the network from converging on a linear history. Users of the chain may not be able to work out which fork is correct, and that makes them vulnerable to double spend attacks, the very thing we wish to avoid.

This illustrates the nothing at stake problem. As outlined above, the solution is to detect the two contradictory blocks and slash the validator that proposed them.

Proposer equivocation is not detected in-protocol, but relies on a third-party constructing a proof of equivocation in the form of a ProposerSlashing object. The proof comprises just two signed beacon block headers: that's enough to prove that the proposer signed off on two blocks in the same slot. A subsequent block proposer will include the proof in a block (and be well rewarded for it), and the protocol will slash the offending validator's balance and eject it from the active validator set.

Attester slashing

Similarly, when it is a validator's turn to publish an attestation, it is supposed to run its fork choice rule and vote for the head block that it thinks is best. The issue here is that an attacker could make multiple contradictory attestations in order to provoke or prolong forks and prevent the network from converging on a single chain. Even a mostly-honest validator might be tempted to make two attestations for a borderline late block: one voting for the block, one voting for an empty slot. If it weren't punishable behaviour, this would hedge the chance of voting the wrong way and missing out on a reward.

The remedy is the same: detect and punish contradictory attestations. That is, attestations made in by the same validator in the same slot for different head blocks.

History

The LMD GHOST fork choice in Ethereum has its origin's in Vlad Zamfir's work on the Casper CBC protocol (then known as Casper TFG, and not to be confused with Casper FFG, which is something quite different²¹). The initial announcement of Casper TFG was in 2015, and in his 2017 Casper the Friendly Ghost paper, Zamfir describes combining Sompolinsky and Zohar's GHOST protocol with a "latest message" construction.

In August 2018, Vitalik still favoured a fork choice called IMD GHOST (formerly known as Recursive Proximity to Justification), that was more aware of finalisation and justification than the pure LMD GHOST that we have today. As the Eth2 consensus mini-spec evolved, IMD GHOST was changed to LMD GHOST in November 2018²². This was due to concerns about the stability properties of IMD GHOST.

That November 2018 description of LMD GHOST in the mini-spec is essentially what we are using today.

See also

Bear in mind that this section has covered only the pure form of LMD GHOST. In Ethereum's full consensus protocol, LMD GHOST is modified by being integrated with Casper FFG, as we shall see in the Gasper section. It is also modified by proposer boost, which we shall also discuss later.

The fork choice document in the consensus specs repo contains the relevant specifications. They are covered in my annotated specification in the following places.

- get_head() is the entry point to the fork choice when we want to get an opinion on the best current head block.
- get_weight() is where the LMD GHOST algorithm is implemented.
- The on_attestation() handler is where the fork choice learns about LMD GHOST votes.
 - Validating those votes is mostly taken care of in validate_on_attestation().
 - update latest messages() takes care of the record keeping around latest messages.

 $^{^{21}\}mbox{Welcome}$ to the joy of naming things in Ethereum.

 $^{^{22}}$ You can view the history of changes to the mini-spec by clicking on the pencil icon near the title.

The introduction to Vitalik's annotated fork choice is an excellent overview (though some of the details in the spec itself are now outdated). The LMD GHOST part of Vitalik's CBC Casper tutorial has a nice explainer. Ignore the later stuff about finality in Casper CBC - that does not concern us.

Some weaknesses of LMD GHOST as it is currently implemented in Ethereum are reviewed in the RLMD GHOST paper. For example, LMD GHOST does not handle dynamic participation securely – that is, when large numbers of validators go offline – among other things. We will consider some of the issues later, but the introduction to that paper is a good read if you want to get a head start.

Casper FFG

- Casper FFG adds finality to the Eth2 consensus protocol.
- It acts as an overlay on LMD GHOST consensus that modifies its fork choice rule.
- Casper FFG is classically safe under asynchrony when less than $\frac{1}{3}$ of validators are faulty or adversarial.
- Moreover, slashing allows Casper FFG to provide accountable safety, also known as economic finality, when more than $\frac{1}{3}$ are adversarial.

Introduction

Many articles have been written to explain the basic mechanics of Casper FFG – how it works – but there is very little about why it works. I hope that by the end of this section you will feel that you have some insight into why Casper FFG is effective.

The mechanics of Casper FFG are not very complicated. Even so, as you read on, bear in mind that the effectiveness of Casper FFG really comes down to two big ideas. First, the two-phase commit (justification and finalisation) and, second, accountable safety.

The two-phase commit gives Casper FFG classical consensus safety. It makes it possible to declare blocks final, being certain that no honest validator will ever revert them. But that's enforceable only when over two-thirds of the stake is controlled by honest validators, something we cannot always assume.

On top of this, Casper FFG offers an extra guarantee called accountable safety for situations when over one-third of the validators are dishonest. If the chain ever suffers from conflicting finality, at least one-third of the total amount of staked Ether will be burnt. This is enforced by slashing validators that break either of the two Casper commandments.

Overview

Casper FFG is a kind of meta-consensus protocol. It is an overlay that can be run on top of an underlying consensus protocol in order to add finality to it. Recall that finality is the property that there are blocks in the chain that are guaranteed never to be reverted: they will be part of the chain forever. In Ethereum's proof of stake consensus, the underlying protocol is LMD GHOST which does not provide finality - there is always a chance that validators might decide to build a competing chain, and there is no real penalty for doing so. Casper FFG functions as a "finality gadget", and we use it to add finality to LMD GHOST.

Casper FFG takes advantage of the fact that, as a proof of stake protocol, we know who our participants are: the validators that manage the staked Ether. This means that we can use vote counting to judge when we have seen a majority of the votes of honest validators. More precisely, votes from validators managing a majority of the stake - in everything that follows, every validator's vote is weighted by the value of the stake that it manages, but for simplicity we won't spell it out every time.

We operate on an asynchronous network, the Internet, which means that we can tolerate at most $\frac{1}{3}$ of the validators being adversarial (or faulty) if we want to achieve both safety and liveness. This is a

well-known result in consensus theory²³, and the reasoning goes as follows.

- We have a total of n validators, of which a number, f, may be faulty or adversarial in some way.
- To preserve liveness, we need to be able to make a decision after hearing from only n-f validators, since the f faulty ones might withhold their votes.
- But this is an asynchronous environment, so the f non-responders may simply be delayed, and not faulty at all.
- Therefore we must account for up to f of the n-f responses we have received being from faulty or adversarial validators.
- To guarantee that we can always achieve a simple majority of honest validators after hearing from n-f validators, we require that (n-f)/2 > f. That is, n > 3f.

To summarise, like all classical Byzantine fault tolerant (BFT) protocols, Casper FFG is able to provide finality when less than one-third of the total validator set is faulty or adversarial. When sufficient honest validators have declared a block finalised, all honest validators will follow, and that block will not be reverted. However, as we shall see, unlike classical BFT protocols, Casper FFG is also able to provide economic finality (accountable safety) even when more than one-third of the validator set is faulty or adversarial.

In this section, we will consider Casper FFG on its own terms, without spending much time on how it is integrated with LMD GHOST. This is in the spirit of the Casper FFG paper which has very little to say about the underlying blockchain consensus mechanism. We will look at how the two are combined into Gasper in the next section.

Naming

Once again, the name Casper FFG comprises two parts, and it's worth looking at them both.

Casper

The Casper part of the name seems to be due to Vlad Zamfir. He explains in Part 5 of his History of Casper as follows.

In this chapter I recount the story of Casper's birth as an application of the principles of Aviv Zohar and Jonatan Sompolinsky's GHOST to proof-of-stake.

I called it "the friendly ghost" because of incentives designed to guarantee censorship resistance against the oligopolists: incentives that force the cartel to be friendly to non-cartel validators.

The GHOST protocol he mentions is the same as we looked at in the previous section. It helps to make sense of all this if you share the cultural context that Casper the Friendly Ghost is a cartoon character that's been around since the 1940s.

Zamfir's protocol was initially called Casper TFG (The Friendly Ghost), and later renamed Casper CBC (Correct By Construction). Vitalik's Casper FFG grew up alongside Zamfir's Casper TFG/CBC – which presumably explains the naming synergy – but has very little in common with it. Indeed, Casper FFG doesn't even use the GHOST protocol. 24

FFG

The FFG part stands for the "Friendly Finality Gadget", as in the title of the Casper FFG paper.

This is clearly a play on Zamfir's TFG name, but also indicates that Casper FFG is not a fully self-contained blockchain protocol, but a "gadget" than can add finality to an underlying consensus protocol.

²³See, for example, the paper Asynchronous consensus and broadcast protocols (1985) by Bracha and Toueg. The earlier work Reaching Agreement in the Presence of Faults (1980) by Pease, Shostak and Lamport gives the same bound, but is based on synchronous communications in a system where validators can forge messages. Our environment is asynchronous with unforgeable messages, so Bracha and Toueg's analysis is the relevant one.

²⁴This is, of course, quite confusing. But it's very far from being the most confusing thing in Ethereum naming, so we just live with it.

Terminology

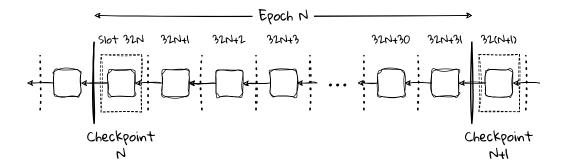
As ever, the jargon that we use is the way into understanding how the protocol is constructed.

Epochs and checkpoints

In order to come to a decision about finality, the Casper FFG mechanism needs to process votes from at least $\frac{2}{3}$ of the validator set. In Ethereum, the validator set is potentially very large, and it is infeasible for votes from several hundred thousand validators to be broadcast, gossiped, and processed simultaneously.

To work around this, voting is spread out through the duration of an epoch²⁵, which, in Eth2, is 32 slots of 12 seconds each. At each slot, $\frac{1}{32}$ of the total validator set is scheduled to broadcast a vote, so each validator is scheduled to cast a vote exactly once per epoch. For efficiency, we bundle each validator's Casper FFG vote with its LMD GHOST vote, although that's by no means necessary.

To ensure that validators voting at different times during the epoch have something in common to vote for, we make them vote for a checkpoint, which is the first slot of an epoch. The checkpoint in epoch N is at slot number 32N (remembering that slots and epochs are numbered from zero).



An epoch is divided into 32 slots, each of which usually contains a block. The first slot of an epoch is its checkpoint. Time increases from left to right.

As an aside, people often talk lazily of finalising epochs, but that's not correct. Casper FFG finalises checkpoints, the first slots of epochs. When we have finalised the checkpoint in epoch N, we have finalised everything up to and including slot 32N. This includes all of epoch N-1 and the first slot of epoch N. But we have not yet finalised epoch N - it still has 31 unfinalised slots in it.

For the time-being we will assume that every slot has a block in it. This is because the original Casper FFG's checkpoints are based on block heights rather than slot numbers. We will relax this assumption to allow empty slots and checkpoints when we look at Gasper.

Within the protocol, a Checkpoint object simply contains the epoch number of the checkpoint, and the hash tree root of the head block in the epoch's first slot (root):

class Checkpoint(Container):

epoch: Epoch
root: Root

Justification and finalisation

Like classical BFT consensus protocols, Casper FFG achieves finality through a two-round process.

In the first round, I broadcast my view of the current epoch's checkpoint (X, say) to rest of the network, and I hear from the rest of the network what their view is. If a supermajority tells me that they also support X, that allows me to justify it. Justification is local to my network view: at this stage, I believe that the majority of the network believes that X is favourable for finalisation. But I don't yet know that the rest of the network has come to the same conclusion. Under adversarial conditions, it is possible that

 $^{^{25}}$ The Casper FFG paper generally uses the word "dynasty" for epoch, with a few exceptions. It's the same thing.

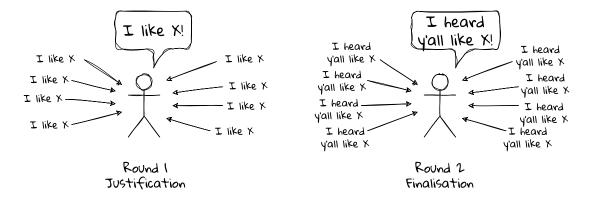
a sufficient majority of the other validators failed to come to a decision on X. We shall look at such a scenario later.

In the second round, I broadcast the fact that I've heard from a supermajority of validators that they support X (that is, that I've justified X) and I hear from the rest of the network whether they believe that a supermajority of validators supports X (that is, that they have justified X). If I hear that a supermajority of validators agrees with me that X is justified, then I will finalise X. Finalisation is a global property: once a checkpoint is finalised, I know that no honest validator will ever revert it. Even if they haven't yet marked the checkpoint as finalised in their view, I know that they've at least marked it justified, and that there is no (non-slashable) behaviour that will be able to revert that justification.

To summarise, for me to be absolutely certain that the whole network agrees that a block will not be reverted requires the following steps.²⁶

- 1. Round 1 (ideally leading to justification):
 - 1. I tell the network what I think is the best checkpoint.
 - 2. I hear from the network what all the other validators think is the best checkpoint.
 - 3. If I hear that $\frac{2}{3}$ of the validators agree with me, I justify the checkpoint.
- 2. Round 2 (ideally leading to finalisation):
 - 1. I tell the network my justified checkpoint, the collective view I gained from round 1.
 - 2. I hear from the network what all the other validators think the collective view is, their justified checkpoints.
 - 3. If I hear that $\frac{2}{3}$ of the validators agree with me, I finalise the checkpoint.

In short, when I justify a checkpoint I make a commitment never to revert it. When I finalise a checkpoint I know that all honest validators are committed to never reverting it.



In Round 1, I broadcast my best checkpoint and hear from all the others their best checkpoint. Ideally this leads to justification. In Round 2, I broadcast what I heard everyone's best checkpoint to be and hear their views. Ideally this leads to finalisation.

Under ideal conditions, each round lasts an epoch, so it takes an epoch to justify a checkpoint and a further epoch to finalise a checkpoint. At the start of epoch N we are aiming to have justified checkpoint N-1 and to have finalised checkpoint N-2.

Quantifying that, it takes 12.8 minutes, two epochs, to finalise a checkpoint in-protocol. In Casper FFG, the two rounds are overlapped and pipelined, so that, although it takes 12.8 minutes from end to end to finalise a checkpoint, we can finalise a checkpoint every 6.4 minutes, once per epoch.

 $^{^{26}}$ The two rounds map roughly onto the PREPARE and COMMIT phases of classical PBFT consensus. The PRE-PREPARE phase of PBFT more or less corresponds to a checkpoint block being broadcast in Casper FFG.

Note that it can be possible from outside the protocol to see that a checkpoint is likely to be finalised a little earlier than the full 12.8 minutes, assuming that there is no long chain reorg. Specifically, it is possible to have collected enough votes by $\frac{2}{3}$ of the way through the second round, that is after about 11 minutes. However, in-protocol justification and finalisation is done only during end of epoch processing.

An aside on the nomenclature: the terms "finalised" and "justified" do not appear in the classical consensus literature. It's easy to see where "finalised" comes from, but perhaps not so for "justified", which is frankly a peculiar term to be using here. As far as I can tell, its origins are in Vlad Zamfir's Casper TFG protocol. In that work, messages contain a "justification" to support the vote being made. The paper doesn't use the word "justified" anywhere, but I suspect that's where we got it from. In Casper FFG, my "justification" is having seen evidence that $\frac{2}{3}$ of validators like the same checkpoint as I do.

Sources and targets, links and conflicts

A vote in Casper FFG has two parts: a *source* checkpoint vote and a *target* checkpoint vote. These are the source and target fields in an attestation's data:

class AttestationData(Container):

slot: Slot

index: CommitteeIndex
LMD GHOST vote
beacon_block_root: Root

FFG vote

source: Checkpoint
target: Checkpoint

Source and target votes are made simultaneously in the form of a $link \ s \to t$, where s is the source checkpoint and t is the target checkpoint.

The role of my target vote is to broadcast my view of what the I think should be the next checkpoint to be justified. In the terms above, it is my round 1 vote. My target vote is a soft (conditional) commitment not to revert that checkpoint as long as I hear from $\frac{2}{3}$ of validators that they also commit to that checkpoint.

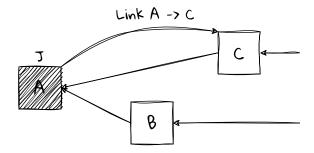
The role of my source vote is to broadcast that I've seen support from $\frac{2}{3}$ of the network for checkpoint s, and that it is the most recent such checkpoint that I know about. In the terms above, it is my round 2 vote announcing the collective view that I've heard. By making this source vote I am upgrading my previous soft commitment not to revert the checkpoint to a hard (unconditional) commitment never to revert it.



Casper FFG combines the source and target votes into a single message: a vote for a link $s \to t$.

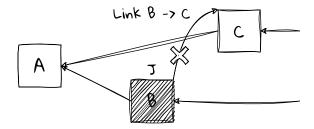
An honest validator's source vote will always be the highest justified checkpoint in its view of the chain. Its target vote will be the checkpoint of the current epoch that descends from the source checkpoint. The source and the target checkpoints do not need to be consecutive; it is permissible to jump checkpoints. But when the beacon chain is running smoothly, the target vote of one epoch will be the source vote of the next epoch.

In a valid link, the source checkpoint will always be an ancestor of the target checkpoint. If it weren't so, I'd be contradicting myself: the source vote announces my commitment never to revert checkpoint s; if the target checkpoint t is not descended from s then that would be a vote to revert s. However, it is



A link from a justified checkpoint to a checkpoint on a chain that descends from it is valid. Only checkpoints are shown here; the intermediate blocks have been omitted for clarity.

not a slashable offence to publish such an invalid $link^{27}$.



A link from a justified checkpoint to a checkpoint on a chain that does not descend from it is invalid. The two checkpoints are said to be conflicting as neither descends from the other.

There are some specific criteria around timeliness that valid Casper FFG votes must satisfy in the Eth2 implementation. We'll discuss these more in the Gasper section as they don't apply to the abstract Casper FFG protocol that we're considering here.

When weighing Casper FFG votes, only votes that have been received in blocks are considered. Unlike with LMD GHOST's fork choice, we do not consider any Casper FFG votes received solely via gossip, by carrier pigeon, or by any other means. This is because we must always have a common record of our decision making around finality, and the block history provides that common record. So, when I said above, "I tell the network", it's shorthand for saying that I broadcast an attestation that will be picked up by a block proposer and included in a block. And when I said, "I hear from the network", it's shorthand for saying that I processed the attestations included in a block.

Also, allow me to reiterate that votes in Casper FFG are weighted according to validators' effective balances. A vote from a validator with a 24 ETH effective balance carries 75% of the weight of a vote from a validator with a 32 ETH effective balance. I will frequently say things like, "the votes of two-thirds of the validators"; you should understand this as, "the votes of validators managing two-thirds of the stake".

Supermajority links

As described above, a link is a Casper FFG vote pair that links the source and target checkpoints, $s \to t$.

A link $s \to t$ is a supermajority link when over $\frac{2}{3}$ of the validators (weighted by stake) have published the same link (and had their votes included in blocks in a timely way).

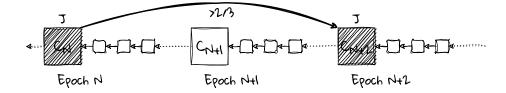
²⁷It was a slashable offence to link conflicting checkpoints in earlier versions of Casper FFG, but this was simplified in the Casper FFG design we use today, as per footnote 4 of the Casper FFG paper.

The mechanics of Casper FFG

With (most of) the terminology and key concepts behind us, we can now look at how Casper FFG operates in detail. It is fairly straightforward.

Justification

When a node sees a supermajority link from justified checkpoint c_1 to checkpoint c_2 , then it considers checkpoint c_2 to be *justified*.



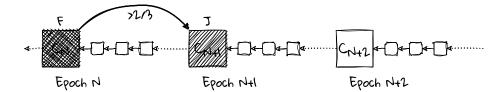
My node has seen a supermajority link $C_N \to C_{N+2}$, therefore I mark C_{N+2} as justified. Justified checkpoints are hatched and marked with "J".

Justification means that I have seen commitments from over $\frac{2}{3}$ of the validator set that they will not revert checkpoint c_2 as long as they get confirmation from at least $\frac{2}{3}$ of validators that also will not revert c_2 .

Finalisation

When a node sees a supermajority link from justified checkpoint c_1 to checkpoint c_2 , and checkpoint c_2 is a direct child checkpoint of c_1 , then it considers checkpoint c_1 to be *finalised*.

In other words, a finalised checkpoint is a justified checkpoint whose direct child is justified.



My node has seen a supermajority link $C_N \to C_{N+1}$, therefore I mark C_{N+1} as justified. Since C_{N+1} is a direct child of C_N in the checkpoint tree, I also make C_N as finalised. Finalised checkpoints are cross-hatched and marked with "F".

Finalisation means that I have seen confirmation from over $\frac{2}{3}$ of the validators that they have seen commitments from over $\frac{2}{3}$ of the validators that they will not revert checkpoint c_1 . Checkpoint c_1 cannot now be reverted without at least $\frac{1}{3}$ of validators provably changing their minds, and therefore getting slashed.

The above rule for finalising a checkpoint is the one described in the original Casper FFG paper. In practice we can use a slight generalisation of this rule, without affecting the safety proof. The generalisation is called k-finality and we will look at it a little later.

The Casper commandments

In the Casper FFG paper, each checkpoint has a defined height: if c is a checkpoint, then h(c) is the height of that checkpoint. Checkpoint heights increase monotonically with distance from the genesis block.

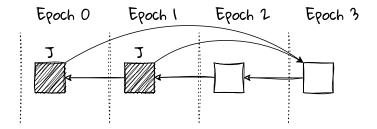
In the Eth2 implementation of Casper FFG, the checkpoint height is the checkpoint's epoch number: h(c) = c.epoch. Recall that a checkpoint comprises both a block hash and an epoch number. If either of these differs then the checkpoints are different.

Casper FFG's proof of accountable safety relies on any validator that violates either of the following two rules, or "commandments", being slashed.

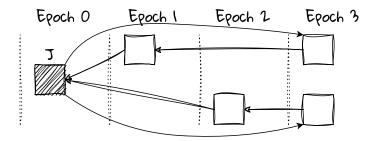
No double vote

Commandment 1: a validator must not publish distinct votes $s_1 \to t_1$ and $s_2 \to t_2$ such that $h(t_1) = h(t_2)$.

Simply put, a validator must make at most one vote for any target epoch.



One way to violate the no double vote rule: voting for the same target checkpoint from different source checkpoints: $0 \to 3$ and $1 \to 3$.



Another way to violate the no double vote rule: voting for different target checkpoints in the same epoch: $0 \to 3$ and $0 \to 3'$.

No surround vote

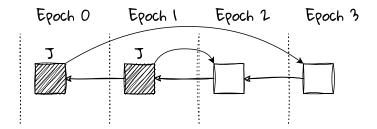
Commandment 2: a validator must not publish distinct votes $s_1 \to t_1$ and $s_2 \to t_2$ such that $h(s_1) < h(s_2) < h(t_2) < h(t_1)$.

That is, a validator must not make a vote such that its link either surrounds, or is surrounded by, a previous link it voted for.

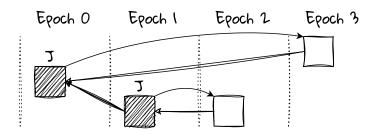
Slashing

Any validator that violates either of the Casper commandments is liable to being slashed. This means that some or all of its stake is removed and it is ejected from the validator set.

Slashing underpins the accountable safety guarantee of Casper by putting a price on bad behaviour specifically, behaviour that could lead to conflicting checkpoints being finalised. Slashing also features in LMD GHOST, and the Incentive Layer chapter has more information on the detailed mechanics of slashing.



One way to violate the no surround vote rule: the link $0 \rightarrow 3$ surrounds the link $1 \rightarrow 2$.



Another way to violate the no surround vote rule: again, the link $0 \to 3$ surrounds the link $1 \to 2$, albeit on different branches.

Violations of the commandments are potentially difficult to detect in-protocol. In particular, detection of surround votes might require searching a substantial history of validators' previous votes²⁸. For this reason, we rely on external slashing detection services²⁹ to detect slashing condition violations and submit the evidence to block proposers. There needs to be only one such service on the network, as long as it is reliable. In practice we have more, but it is certainly not necessary for every node operator to run a slashing detector.

Once evidence of breaking one of the commandments has been found, it is easy to prove on chain that the validator broke the rules. Validators sign every attestation they publish, so, given two conflicting attestations, it is a simple matter to verify their signatures and show that the validator broke the rules in publishing them.

The protocol as it is presented in the Casper FFG paper assumes that, on proof of having violated a slashing condition, "the validator's entire deposit is taken away". We have implemented a variation of this for Eth2 that scales the proportion of a validator's stake that is forfeit in proportion to total amount of stake slashed in a given period. If $\frac{1}{3}$ of all stake violated slashing conditions within a 36 day window, then the whole stake would be forfeit, as in the classic Casper FFG protocol. But if there were very few other slashings in the window, then almost no stake would be forfeit. This nicety does not change the Casper FFG guarantees in practice, at least since the Bellatrix upgrade to the beacon chain gave the PROPORTIONAL SLASHING MULTIPLIER constant its final value.

Fork choice rule

Casper FFG's fork choice rule takes the form of a modification to the underlying consensus mechanism's fork choice rule. From the Casper FFG paper, the underlying consensus mechanism must,

follow the chain containing the justified checkpoint of the greatest height.

The pure LMD GHOST protocol always begins its search for the head block from the root of the chain, the genesis block. When modified by Casper FFG's fork choice rule, LMD GHOST will start its search

²⁸See Protolambda's eth2-surround GitHub repo for some analysis of the challenges of finding surround votes.

 $^{^{29}}$ Slashing detection software has been created by the Lighthouse team and the Prysm team.

for the head block from the highest justified checkpoint it knows about, and will ignore potential head blocks that do not descend from the highest justified checkpoint. We will discuss this more when we get to Gasper.

This modification to the underlying consensus protocol's fork choice rule is what confers finality. When a node has justified a checkpoint in its local view, it is committed to never reverting it. Therefore, the underlying chain must always include that checkpoint; all branches that do not include that checkpoint must be ignored.

Note that this fork choice rule is compatible with the plausible liveness guarantee of Casper FFG.

The guarantees of Casper FFG

The Casper FFG consensus protocol makes two guarantees that are analogous to, but different from, the concepts safety and liveness in classical consensus: accountable safety, and plausible liveness.

Accountable safety

Classical PBFT consensus can guarantee safety only when less than one-third of validators are adversarial (faulty). If more than one-third are adversarial then it makes no promises at all.

Casper FFG comes with essentially the same safety guarantee when validators controlling less than one-third of the stake are adversarial: finalised checkpoints will never be reverted. In addition, it provides the further guarantee that, if conflicting checkpoints are ever finalised, validators representing at least one-third of the staked Ether will be slashed. This is called "accountable safety". It is accountable in that we can identify exactly which validators behaved badly and punish them directly.

The extra safety this guarantee provides is not safety in the usual consensus protocol sense of the word, but it is safety of a specifically cryptoeconomic nature: bad behaviour is heavily disincentivised by the protocol. It is often referred to as "economic finality".

Proof of accountable safety

The proof of Casper FFG's accountable safety is reasonably intuitive. I will sketch out the proof below more-or-less as it is presented in the Casper FFG paper, but modified for epochs rather than the more abstract "checkpoint height" that the paper uses.

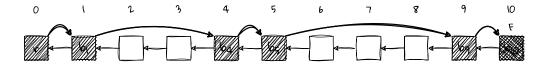
We will prove that, if fewer than $\frac{1}{3}$ of validators (weighted by stake) violate a Casper commandment, two conflicting checkpoints cannot both be finalised. We will do this by showing that the only way a conflicting checkpoint could be finalised is for there to be a supermajority link that is surrounded by another supermajority link, which contradicts the assumption at start of this paragraph, since surround votes violate the second commandment.

The first handy observation we'll need is that, under this assumption, at most one checkpoint can be justified in any epoch (in the views of honest nodes). This follows directly from the no double vote commandment.

Let us take two conflicting finalised checkpoints a_m and b_n in epochs m and n respectively. Since the checkpoints conflict, neither is a descendent of the other. From the previous observation, we know that $m \neq n$. Without loss of generality, we will take m < n, so that b_n is the higher finalised checkpoint.

Now, there must be a continuous series of justified checkpoints leading from the root checkpoint to b_n with supermajority links between them. That is, there is a set of k supermajority links $\{r \to b_{i_1}, b_{i_1} \to b_{i_2}, b_{i_2} \to b_{i_3}, \dots, b_{i_{k-1}} \to b_{i_k}\}$, with $i_k = n$. This follows from the definition of justification. The set of justified checkpoints leading to b_n is thus, $\mathcal{B} = \{r, b_{i_1}, b_{i_2}, b_{i_3}, \dots, b_{i_{k-1}}, b_{i_k}\}$. We can imagine bouncing along supermajority links from the root, landing on each of these checkpoints before jumping to the next.

Now consider conflicting finalised checkpoint a_m . From the definition of finalisation, there must be a supermajority link $a_m \to a_{m+1}$ from a_m to a_{m+1} in the next epoch. Clearly neither a_m nor a_{m+1} is in the set \mathcal{B} , since that would make a_m an ancestor of b_n and not conflicting. Also, set \mathcal{B} contains no checkpoint b_m or b_{m+1} since we may have only one justified checkpoint in an epoch.

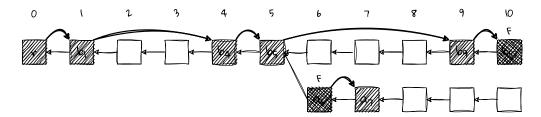


For any finalised checkpoint, such as b_{10} , there is a contiguous chain of supermajority links leading to it from the root, r. The chain of links here justifies the set of checkpoints $\mathcal{B} = \{r, b_1, b_4, b_5, b_9, b_{10}\}$. Shaded checkpoints are justified (and maybe finalised); cross-hatched checkpoints are finalised (also marked with "F").

Given these observations, it is inevitable that the pair of checkpoints (a_m, a_{m+1}) falls between the epochs of two consecutive elements of \mathcal{B} , say $b_{i_{j-1}}$ and b_{i_j} . That is, there is a j such that $i_{j-1} < m < m+1 < i_j$.

Finally, we can see that there must be a supermajority link $b_{i_{j-1}} \to b_{i_j}$ that *surrounds* the supermajority link $a_m \to a_{m+1}$. Either the surrounding or surrounded link cannot exist unless at least $\frac{1}{3}$ of validators have violated the second Casper commandment, which we have assumed they did not.

Therefore, we have proved (by contradiction) that two conflicting checkpoints cannot both be finalised if fewer than $\frac{1}{3}$ of validators (by weight) violate a Casper commandment.



Suppose an earlier, conflicting checkpoint a_6 is finalised. Finalisation means that there must be a supermajority link $a_6 \to a_7$. One of the supermajority links on the b chain – in this case, $b_5 \to b_9$ – must span $a_6 \to a_7$.

In this proof, we have relied on the definition of finalisation being that there is a supermajority link from the checkpoint being finalised to the checkpoint in the very next epoch. It turns out that we can relax that definition a little and calculate finality in the form of k-finality. We will discuss this below.

Economic finality

The proof of accountable safety rested on there being,

- 1. no two supermajority links that target distinct checkpoints at the same height, and
- 2. no two supermajority links such that one surrounds the other.

These conditions are enforced by the two Casper commandments. Since a supermajority link requires support from $\frac{2}{3}$ of the validators (by stake), if there are two supermajority links that break one of these rules, then at least $\frac{1}{3}$ of the validators must have voted for both of the links. That is, at least $\frac{1}{3}$ of validators made a double vote or a surround vote.

As we have seen already, any validator that breaks a commandment is liable to being slashed, that is, having all or part of its stake removed, and being ejected from the validator set. Therefore, in the event of a conflicting finalisation, we have the guarantee that at least $\frac{1}{3}$ of the staked Ether will be slashed.

In this way, slashing puts a price on attacking the chain, and a huge (and calculable) cost on successfully attacking the chain³⁰. As Vitalik puts it,

 $^{^{30}\}mathrm{As}$ I write (in July 2023), there is 21.6 million ETH staked on the beacon chain, so a finality reversion would result in

Basically, if a block is finalized, then that block is part of the chain, and it is very, very expensive to cause that to change.

We call this "economic finality". It is not finality enforced by software; it is finality enforced by the cost of an attack. Validators' stakes are a "good behaviour bond" that can be taken away from them if it is ever proved that they broke the protocol's rules. Validators have unique identities in the form of their secret keys that they use to sign all their messages, so it is possible to hold individual validators to account, and punish them very specifically.

You might wonder why we need a concept like economic finality at all. After all, PBFT manages to deliver finality without such a construct. Couldn't the protocol simply refuse to finalise a conflicting checkpoint?

The difference is that in PBFT there is the luxury of a hard safety assumption that fewer than one-third of the validators are adversarial. Similarly, in Casper FFG, an adversary with less than one-third of the stake cannot finalise conflicting checkpoints. However, in the world of permissionless blockchains, we must have some defence for when more than one-third of the stake is adversarial. That defence is slashing, which gives us the economic finality guarantee: if more than one-third of validators are willing to behave badly, we can't prevent them from finalising conflicting checkpoints, but we can put a huge cost on doing so.³¹

In a blog post, On Settlement Finality, Vitalik puts it like this,

We can't guarantee that "X will never be reverted", but we *can* guarantee the slightly weaker claim that "either X will never be reverted or a large group of validators will voluntarily destroy millions of dollars of their own capital".

Faced with a greater than one-third attacker and an asynchronous network, it's not useful for validators simply to refuse to finalise conflicting checkpoints in-protocol. Attacks that can finalise conflicting checkpoints depend on partitioning the set of honest validators so that they don't see each other's votes, and don't know what the other side has finalised. Under the treat of such powerful attacks, economic finality is a powerful safety guarantee. The ultimate remedy in the event of conflicting finality is manual intervention. As Vitalik observes in the same post, "the user community around an on-chain asset is quite free to simply apply common sense to determine which fork was not an attack and actually represents the result of the transactions that were originally agreed upon as finalized".

Plausible liveness

Casper FFG on its own does not offer liveness in the classic sense of ensuring that users' transactions get included on chain. All block production and chain building is the responsibility of the underlying consensus mechanism, LMD GHOST in our case.

However, there is a sense in which we want Casper FFG to be live: we always want to be able to continue justifying and finalising checkpoints if at least two-thirds of validators are honest, without any of those validators getting slashed. Conversely, we never want to end up in a deadlock in which it is not possible to finalise a new checkpoint without honest validators being slashed. This accords with the "something good eventually happens" definition of liveness.

In Vitalik's words,

Plausible liveness basically means that "it should not be possible for the algorithm to get 'stuck' and not be able to finalize anything at all".

More formally, from the Casper paper,

at least 7.2 million ETH being slashed. This amounts to \$13.7 billion of economic security against reversion, at current prices.

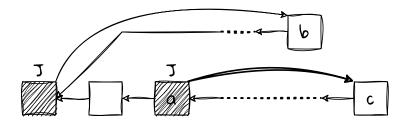
³¹This has some conceptual similarity to the cost of mounting a 51% attack in proof of work. Except that, in PoW, the cost of a successful attack can be zero, since the attacker gains all the block rewards, and the attack can be repeated indefinitely using the same hardware. The economic finality provided by slashing is much higher. In Vlad Zamfir's famous words, getting slashed is "as though your ASIC farm burned down if you participated in a 51% attack".

Supermajority links can always be added to produce new finalized checkpoints, provided there exist children extending the finalized chain.

The proof runs like this. There will be an existing highest justified checkpoint, a, and there will be a checkpoint b at the same height or higher (not necessarily descending from a) that is the highest checkpoint for which any validator has made a target vote.

Let c be a checkpoint on the chain descending from a in epoch h(b) + 1, that is, the epoch directly after b.

All validators can vote for the link $a \to c$ without fear of being slashed because, (1) it cannot be a double vote, since no validator has previously voted with target h(c), and (2) it cannot be a surround vote since no honest validator can have previously used a source higher than h(a), nor can it be a surrounded vote since no existing link has a target higher than h(b).



Voting for the link $a \to c$ is safe because (1) nobody has previously voted with c as the target as b has the highest target votes so far, and (2) it cannot surround another link since there is no higher justified checkpoint than a to use as a source vote.

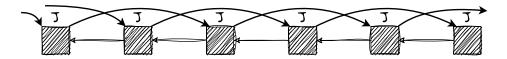
Therefore we can justify checkpoint c. It is then clearly safe for all validators to vote $c \to d$ where d is the direct child of c, and thus we can finalise c without breaking either of the commandments.

This requirement for plausible liveness underpins Casper FFG's fork choice rule: the underlying consensus mechanism must follow the chain containing the justified checkpoint of the greatest height. As long as the underlying chain keeps building on top of the highest justified checkpoint then, according to this proof, we are guaranteed to be able to keep finalising checkpoints on it without anyone getting slashed.

Exercise

As an interlude, it's a fun and useful exercise to think through different ways in which Casper FFG could behave.

For example, how could a situation like the following diagram arise? That is, with supermajority links continually skipping checkpoints, resulting in a string of justified checkpoints with none finalised.



Always justifying but never finalising. How can we get into such a situation?

The answer is below, but take a moment to think through the circumstances that could lead to this.

Casper FFG miscellania

Incentives

In LMD GHOST, we saw that correct head votes that are included in a block in the next slot receive a reward. But there was no penalty for late or incorrect head votes.

Rewards and penalties are a little more complex in the implementation of Casper FFG. Validators are well incentivised to make accurate and timely Casper FFG votes: 22% of a validator's potential staking rewards come from source votes, and 41% from target votes. Moreover, inaccurate or late source or target votes are penalised by the same amount as the reward.

To get any Casper FFG reward at all, a validator's source vote must be correct. That is, it must agree with the history that the eventual canonical chain converges on. If the source vote is incorrect, then it's as if the validator has not voted at all and it receives a full penalty for missing both source and target. The rationale for this is that having a wrong source means that it was working on a different branch from the one that became canonical in the end. Thus its votes were competing with rather than supporting the consensus.

To receive the source vote reward, the source vote must be correct, and it must also be timely. If a validator's vote is included in a block within five slots, then it receives the source vote reward, otherwise it receives a penalty of the same size. There is some discussion of the reason for the five slot limit in the Annotated Specification.

To receive the target vote reward, the target vote must be correct, and it must also be timely. If a validator's vote is included in a block within thirty-two slots, then it receives the target vote reward, otherwise it receives a penalty of the same size³².

The Annotated Spec has a full matrix of rewards and penalties for the different degrees of correctness and timeliness of votes.

Dynamic validator sets

In all of the above, we have discussed Casper FFG in terms of a static validator set, assuming that no validators enter or exit the protocol. This is not entirely realistic, as we wish to be able to onboard new stakers and to allow stakers to exit.

The Casper FFG paper discusses how accountable safety can be maintained when the validator set changes from epoch to epoch. It analyses this in terms of forward and rear validator sets. The implementation in Ethereum 2.0 ignores this mechanism, working around it instead by severely rate-limiting validator activations and exits. Each epoch, we allow activations and deactivations of validators amounting to a fraction of about 0.0015% of the full validator (see CHURN_LIMIT_QUOTIENT).

The effect of this simplification is analysed in the Gasper paper, section 8.6. By rate-limiting entries and exits, but not accounting for forward and rear validator sets, we fractionally reduce the level of accountable safety. That is, it is possible that slightly less than one-third of the stake gets slashed in the event of finalising a conflicting checkpoint. Specifically, if the validator sets between the epochs of the two conflicting finalised checkpoints differ by a staked amount ε , then the economic finality (the minimum amount of stake that will get slashed) becomes $\frac{2}{3} - \varepsilon$ rather than $\frac{2}{3}$. In practice, the rate limiting of validator set changes is so severe that this difference is negligible.

k-finality

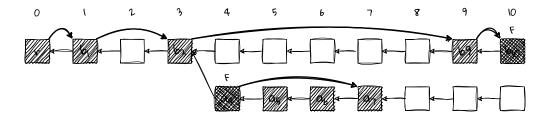
The original Casper paper requires that, to finalise a checkpoint, we must have a supermajority link from that checkpoint to its direct descendant. It turns out that we can generalise this without affecting the validity of the safety proof.

The key observation that the safety proof relies on is the existence of a supermajority link between two consecutive members of \mathcal{B} spanning the supermajority link $a_m \to a_{m+1}$ that finalises a_m . However, the surrounding link on the b branch must still exist if there is a supermajority link $a_m \to a_{m+k}$ where all the checkpoints between a_m and a_{m+k} are justified on the a branch. That's because \mathcal{B} cannot have members in the epochs m to m+k if this is so.

So, our generalised finality rule is that we can finalise checkpoint a_m when we have a supermajority link $a_m \to a_{m+k}$ and checkpoints a_{m+1} , a_{m+2} , ..., a_{m+k-1} are all justified.

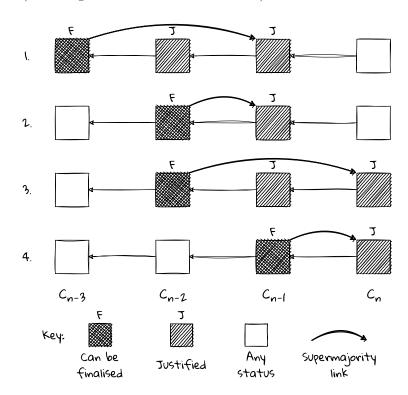
This is called k-finality and is discussed in section 4.5 of the Gasper paper.

³²This will be changed at the Deneb upgrade. Target votes for either the current or previous epoch will be valid, rather than expiring after 32 slots.



The guarantees of the accountable safety proof all carry over if we finalise a checkpoint when there is a supermajority link from it that jumps over only justified checkpoints. Here, a_5 and a_6 are justified, so we can safely finalise a_4 with the supermajority link $a_4 \rightarrow a_7$.

How many checkpoints k one might want to consider when calculating finality depends on how much record keeping one is prepared to do. On the Ethereum 2.0 beacon chain we have adopted 2-finality: we keep a record of the justification status of four consecutive epochs, and allow the processing of target votes for two epochs (older target votes are considered invalid).



The four cases of 2-finality. In each case the supermajority link causes the checkpoint at its start (the source) to become finalised and the checkpoint at its end (the target) to become justified. Cases 2 and 4 are classic 1-finality. Checkpoint numbers are along the bottom.

Almost always, we would expect to see only the 1-finality cases, in particular, case 4. The 2-finality cases would occur only in situations where many attestations are delayed, or when we are very close to the two-thirds participation threshold. Note that these evaluations stack, so it is possible for rule 2 to finalise C_{n-2} and then for rule 4 to immediately finalise C_{n-1} , for example.

The detailed mechanics of this are performed in the weigh_justification_and_finalization() function during epoch processing 33 .

 $^{^{33}\}mathrm{Danny}$ Ryan briefly discussed k-finality in this video from Devcon V.

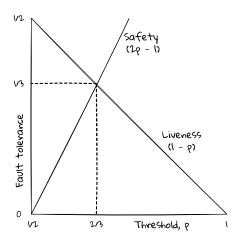
Why two-thirds?

Where does the $\frac{2}{3}$ majority threshold for finalisation come from? It's actually not obvious, and we could have chosen a different value to define a supermajority link. Let's call this threshold p: if a proportion p of the validator set votes to finalise a checkpoint then it is finalised.

We are seeking to balance two factors. On the one hand, a proportion 1-p of adversarial or faulty validators can prevent finality, which is a kind of liveness failure.

On the other hand, we want to maximise the accountable safety of finalisation. That is, the proportion of the stake that must equivocate in order to finalise conflicting checkpoints. This proportion is 2p-1.

Given these constraints, setting $p = \frac{2}{3}$ maximises fault tolerance against liveness attacks – less than one third of validators cannot prevent finalisation – while maximising tolerance to safety faults – at least one third of validators would be slashed if conflicting blocks were finalised.



The threshold that maximises both accountable safety and tolerance to liveness faults together is $p = \frac{2}{3}$.

Vitalik wrote some notes on this in footnote 2 of the Minimal Slashing Conditions article.

How not to get slashed

The two Casper commandments are quite simple, and avoiding being slashed is straightforward in principle: just don't break the rules.

By far the most common reason that validators get slashed is due to their secret signing key being run on different nodes at the same time. If the nodes' views of the network diverge at all – for example, due to a checkpoint block being seen late by one, but not the other – then each instance of the validator can end up signing different votes for the same epoch, violating the first commandment.

The basic way to avoid this is simply not to do that. Only ever run your keys in one place at any time. Client software implementations often provide a defensive mechanisms such as doppelganger detection to help to protect stakers from doing this inadvertently. Doppelganger detection will wait for a couple of epochs before starting to sign attestations; if, during this time, it sees signatures on chain from another instance with the same keys, it refuses to start. An alternative is to delegate signing of votes to a centralised signer that maintains a database of your validator's past votes, and will refuse to sign anything that violates the commandments. One such signing service is Web3Signer.

It is possible in rare instances for even a single instance of a validator to get into a situation where it could make slashable attestations. For example, if the host machine's clock were to jump backward in time. Or when there is a long reversion in the chain, greater than an epoch, a validator's duties can be recalculated. It may find that it has voted in the epoch once already due to its old duties, and then its new duties call for it to vote again later in the epoch, which will lead to a slashable double vote.

For reasons like these, all client software includes slashing protection mechanisms. Different clients take different approaches, but there is an agreed common interchange format for the slashing protection

data, EIP-3076, that can be used for migrating between clients if necessary. Teku takes a very robust, minimalist approach to this. For each validator managed by a Teku node, it maintains a text file with the epoch numbers of the validator's highest source vote and highest target vote to date. For a new attestation to be signed, its source must not be lower than the stored source, and its target must be higher than the stored target. This is sufficient to guarantee that a single instance of a Teku validator will not make a double vote for the same target epoch, and will not make a surround vote.

Casper FFG vs PBFT

As Vitalik acknowledges, the technical roots of Casper FFG are in the classical BFT (Byzantine fault tolerant) consensus protocols developed during the 1980s and 1990s. In particular, it has some similarities to the PBFT (Practical Byzantine Fault Tolerance) algorithm that was published in 1999.

Nevertheless, Casper FFG is not PBFT, and there are some marked differences between the two. What follows is not a rigorous comparison, but touches on the main points.

Both PBFT and Casper FFG are "round based", and involve a two-phase commit process. In Casper FFG, a full round is two epochs, but rounds are overlapped, or pipelined, so the PREPARE step of one round (justification) coincides with the COMMIT step of the previous round (finalisation). This overlap allows Casper FFG to use only one message type (an attestation) that contains two votes (the source and target). Classical PBFT relies on replicas (validators) broadcasting separate PREPARE and COMMIT messages, and rounds are strictly sequential.

Both PBFT and Casper FFG rely on a leader in some way. The leaders in Casper FFG are the block proposers of the underlying consensus mechanism, and are expected to change every round. The leader in PBFT is called the primary, and is only changed if it is deemed by the other replicas to be offline or faulty. PBFT has a whole "view change" mechanism to handle switching to a new leader when necessary.

Importantly, PBFT will stall if more than one-third of validators are offline since it will be unable to execute a view change. In these circumstances, block production would halt completely, which is a consequence of PBFT and its close relatives favouring safety over liveness. Casper FFG will also stall if more than one-third of validators offline in the sense that finalisation will not move forward. However, there is nothing to prevent the underlying chain from continuing to make progress and provide liveness to the system as a whole. This results from Casper FFG's nature as an overlay on top of an underlying block proposal mechanism.

Finally, the safety guarantees of each differ. Safety (finality) in PBFT is a guarantee that, when fewer than one-third of the replicas are faulty, the output of a round will never be changed. Of course, this is subject as always to social consensus. PBFT is a permissioned protocol, falling into the proof of authority category. If all the authorised participants colluded to update their software, they could revert the state of the system quite easily.

Safety in Casper FFG adds the further cryptoeconomic guarantee that a conflicting checkpoint cannot be finalised without burning at least one-third of the stake. This is a substantially different type of guarantee, but fits well with the permissionless nature of Ethereum's proof of stake protocol.

Are the Casper commandments optimal?

There's an interesting discussion to be had around whether the two Casper commandments are ideal or not. For example, there are situations, like the first surround vote shown above, that are harmless, but would nevertheless lead to the validator being slashed. Daniel Lubarov discussed another such scenario in a post that proposes replacing the second commandment with, "a validator must be prohibited from casting a *finalization* vote within the span of another vote" (we currently prohibit all spanned votes).

Along similar lines, Justin Drake has proposed a tight and intuitive Casper slashing condition that unifies the two commandments into a single commandment.

A validator must not cast a vote $s \to t$ that "hops over" one of his finalisation votes $\tilde{s} \to \tilde{t}$, i.e. $h(s) \le h(\tilde{s})$ and $h(t) \ge h(\tilde{t})$ [and such that the target votes conflict].

Jacob Eliosoff goes further by suggesting that we remove the source vote altogether and rework the slashing rules accordingly.

While worth thinking through, I think that proposals like these have failed to gain traction simply because what we have is good enough, on the principle of "if it ain't broke, don't fix it". Much work has been done on implementing, analysing, and formally verifying the current version of Casper FFG, and making any change now that does not gain us a huge benefit (such as single slot finality) is unlikely to be worth the effort.

Conflicting justification

If you want to test your ability to reason about this distributed consensus stuff – and it's not easy – it's worth thinking through why we need both a justified and a finalised status. Why can't I immediately mark as finalised any checkpoint for which I've seen a $\frac{2}{3}$ supermajority vote?

The key point is that justification is a local property; finality is global.

For me to justify a checkpoint means that I've heard from $\frac{2}{3}$ of the validators that they think that the checkpoint is good. But this is only my local view, since the other validators might have heard something different - I have no idea whether they did or didn't. Nevertheless, as an honest validator, I commit to never reverting any checkpoint that I've justified in my local view.

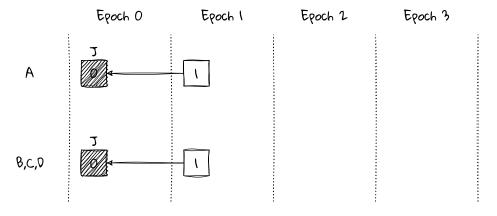
For me to *finalise* a checkpoint means that I've heard back from $\frac{2}{3}$ of the validators that they've heard from $\frac{2}{3}$ of the validators that the checkpoint is good. I now know that $\frac{2}{3}$ of the validators know that $\frac{2}{3}$ of validators have marked that checkpoint as justified, and therefore that a supermajority of validators globally has committed to never reverting it. That checkpoint is globally safe from reversion.

This is all a bit mind-bending, so perhaps it's best understood by looking at ways things can fail if we don't do the full round-trip of confirming that everyone confirms what I have confirmed³⁴.

Simplified model

Let's consider an extreme case. We have four validators, A, B, C, and D. They are all honest, but the network can suffer indefinite delays. For illustration purposes we will have a checkpoint at every block height. We'll arbitrarily number the epochs from 0, but block 0 is not intended to be the genesis block it could be, but that would slightly alter the description that follows.

Epoch 1 - setup



In epoch 1, block 1 contains enough votes to justify checkpoint 0. Everybody votes $0 \rightarrow 1$.

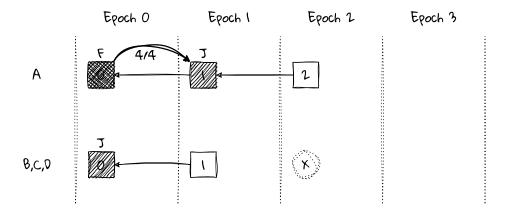
Recall that only Casper FFG votes contained in blocks affect justification and finalisation. At the start, all the validators have a common view. They all see block 1, and it contains enough votes to justify

³⁴If you really want to test your understanding of all this "I confirm that everybody has confirmed that everybody has confirmed" stuff, which is at the heart of consensus safety, then I highly recommend tackling the blue eyes puzzle. I think Joseph Poon introduced me to this in early 2018. It took me a good couple of hours of head scratching to get there, but the effort is worth it. The solution is out there, but I urge you to take a good run at the puzzle before looking it up.

checkpoint 0. So far this is the happy flow. All four validators make the same vote $0 \to 1$: their source checkpoint is 0, which they just justified; their target checkpoint is 1, the current epoch's checkpoint. It's a supermajority vote that *ought* to lead to checkpoint 1 being justified by everybody.

Epoch 2 - inconsistent justification

This is where things go wrong. In epoch 2, validator A is chosen to propose, but for some reason A's block is not seen by the others - it was severely delayed on the network, perhaps by a denial of service attack. Therefore, validators B, C and D don't see the supermajority link it contains that justifies checkpoint 1, so they don't know that anyone else likes checkpoint 1. We now have split views: validator A has justified checkpoint 1 and is irrevocably committed to it; the other validators still consider checkpoint 0 to be the highest justified.



In epoch 2, validator A proposes block 2. It contains all four $0 \to 1$ votes, but validators B, C and D never see it. Validator A has seen a supermajority link $0 \to 1$, so it marks checkpoint 1 as justified. Validators B, C and D saw no votes in epoch and their best justified checkpoint remains 0. A votes $1 \to 2$; B, C and D vote $0 \to X$, where X is an empty checkpoint.

The source of the issue is that A has seen everyone else agree, but the others have no evidence of the agreement. As far as B, C and D are aware, each is on its own. They have no alternative but to leave things as-is for now and to try to agree in the next round³⁵.

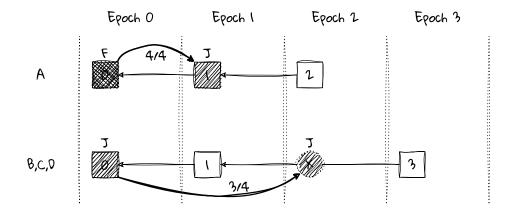
It's not important for this example, but it's worth noting that, by justifying checkpoint 1, validator A will have finalised checkpoint 0. Validator A knows that checkpoint 0 will never be reverted globally since it knows that at least $\frac{2}{3}$ of validators consider it justified (they used it as their source vote) and will therefore never revert it, irrespective of whatever else is happening.

As for voting in epoch 2, validator A will vote $1 \to 2$, and the three others will vote $0 \to X$, where X shows that they see the checkpoint in epoch 2 as empty. We haven't discussed empty checkpoints yet – we'll cover them when we get to Gasper – for now you can understand that a vote for empty checkpoint X is a statement that the head of the chain in epoch 2 remains block 1.

Epoch 3 - conflicting justification

Now assume that the block in epoch 3 is proposed by one of B, C or D. It contains the three $0 \to X$ votes, but cannot contain A's vote since it has a different source. In turn, validator A will consider block 3 to be invalid since it contains attestations whose source is not checkpoint 1, A's highest justified checkpoint. The three votes are enough in the views of B, C and D to form a supermajority, so they duly justify checkpoint X.

³⁵They are likely to have seen each others' votes via gossip, and in a more realistic model, with multiple blocks per epoch, are likely to include these votes in later blocks. But it is not guaranteed, and in our contrived, simplified model, is not possible.



In epoch 3, one of B, C or D publishes block 3. It contains the three $0 \to X$ votes, so validators B, C and D have a supermajority link justifying the empty checkpoint X. Validator A considers block 3 to be invalid.

At this point, validator A's situation is irrecoverable. The BCD chain will never make votes with checkpoint 1 as source, so validator A will never consider their attestations or their blocks valid, and vice-versa. Justification cannot progress on A's chain since it can see only $\frac{1}{4}$ of the voting weight. The only remedy is for the node hosting A to wipe its database and perform a fresh re-sync onto the canonical chain. Validator A will then be able to join in again as usual without any risk of violating a Casper commandment³⁶.

Note that we have not yet answered our question. What if validator A had immediately marked block 1 as final rather than only justified? In this example it would not have made a material difference. Block 1 ultimately appears in the canonical chain progressed by B, C and D, so marking it as final would have been fine.

Now with adversarial action

To see why skipping the justification step is dangerous we will introduce some adversarial action. Let's say that C and D are not honest validators.

When all three of B, C and D are acting honestly, as above, in epoch 2 they will vote for the empty checkpoint X that descends from block 1, then in epoch 3 will justify it. This locks them into including block 1 into their canonical chain, since the Casper FFG fork choice now prevents them from building a conflicting branch.

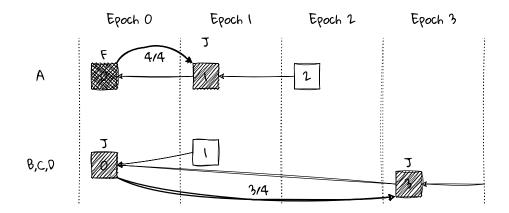
However, if a majority of B, C and D is dishonest, they can fail to justify X (by not voting), and in epoch 3 can choose to build a new branch on block 0, which remains their highest justified checkpoint. In so doing, they will orphan block 1. Crucially, they can do this without violating a slashing rule.

Now we get to the point. Had validator A immediately marked block 1 as final, it would be disastrous for any applications or users that relied on validator A's node for information about the chain. They would have seen a finalised block that never appears in the later canonical chain maintained by B, C and D. That is, they would have seen a "finalised" block being reverted without any slashing, violating Casper FFG's accountable safety guarantee.³⁷

Note that we've framed this in terms of adversarial action. But, actually, the assumption of dishonesty is not necessary to prove our point. Perhaps a network delay prevented the epoch 2 votes from C and D

³⁶It should be recognised that this is a rather extreme and contrived example. It would be very unusual for anything like this to occur in practice.

³⁷If we had assumed that C and D were controlled by the adversary from the outset, and that the adversary has some control over which of A or B sees their blocks, then it is quite simple for the adversary to split the views of A and B so that each justifies a checkpoint on a different branch. I shall leave it as an exercise for the reader to show this - the flow is similar to the above.



When a majority of B, C and D is not honest, they can fail to justify checkpoint X and build a branch that orphans block 1.

from making it on chain. It is evident that the bad consequences of premature finalisation don't depend on there being more than one-third dishonest validators, which is pretty disastrous.

In summary, the only way to guarantee safety is via the two-phase commit. This guarantees that a block marked finalised will always appear in the canonical chain, unless at least one-third of validators are slashed.

Summary and reflections

Using this toy model, we've have seen that we are able to achieve Casper FFG's guarantees only by using the two-phase commit. We cannot skip justification and go straight to finalisation when we see a supermajority link.

Even this radically simplified model of the beacon chain is quite tricky to reason about. But all the confirming and re-confirming of things is very much in the nature of distributed systems. Everything would be much easier if we had a trusted central authority. For example, in a national leadership election, we all cast our votes and the central authority counts them and broadcasts the result - it's a single round process. But the consequences can be very bad if the central authority turns out to be corrupt. The two-phase commit is the cost of making our protocol incorruptible.

History of Casper FFG

The development of the proof of stake consensus protocol for Ethereum 2.0 has a long history which is very well summarised by Vitalik in a tweet thread (consolidated here), and in Vlad Zamfir's memoirs linked from there.

The origins date back as far as January 2014 and Vitalik's Slasher: A Punitive Proof-of-Stake Algorithm article. Although almost nothing of the Slasher algorithm is in use today, it introduced the idea of punishing misbehaving validators for violating protocol rules, thus solving the nothing at stake problem that we discussed under LMD GHOST. Slashing paved the way for the idea of economic finality.

In 2015 Vitalik was working on consensus by bet, a form of which appeared in 2016 in the Ethereum.org 2.0 Mauve Paper. He describes consensus by bet as having been, "a big long, and ultimately unproductive, tangent". However, consensus by bet did pioneer the idea of retrospectively conferring finality on top of a forkful block production mechanism, which is the essence of Casper FFG.

The Casper FFG mechanism that we have today really started taking shape in 2017, after Vitalik had returned to the classical PBFT literature. The design that emerged begins to look quite familiar to us today, although it doesn't yet use the "justification" terminology, still preferring the PREPARE and COMMIT terms of PBFT. A really novel feature it provides is achieving economic finality through the use of slashing conditions. There were four slashing conditions at that time, which were later reduced to

two³⁸, with one message type.

Vitalik's Casper FFG and Vlad Zamfir's Casper CBC consensus protocols grew up alongside each other during this period. As Vitalik describes in a blog post in December, 2016, the design imperative for Casper FFG was to, "create a simple proof of stake protocol that would provide desirable properties with as few changes from proof of work as possible". He contrasts this typically pragmatic approach with Zamfir's more purist desire to "rebuild consensus from the ground up". Confusingly, the two resulting Casper protocols have little in common apart from generic proof of stake things. Nevertheless, Vitalik still occasionally expresses the hope that Ethereum might eventually switch to something like Casper CBC.

The first version of the Casper the Friendly Finality Gadget paper was uploaded in October 2017. It was written by Vitalik and Virgil Griffith, and pretty much describes the scheme that we use today - subject to the modifications for Gasper that we'll cover in the next section.

As noted earlier, the original plan had been to apply Casper FFG as an overlay on Ethereum's existing proof of work protocol. This effort progressed quite far, with an EIP-1011 testnet going live on the 31st of December, 2017.

The PoW overlay plan was abandoned in 2018 in favour of moving directly to full proof of stake via a new beacon chain architecture running the Gasper (LMD GHOST plus Casper FFG) consensus architecture - this is the architecture that we have today.

The initial specification for Casper FFG on the beacon chain was maintained on Ethresear.ch (you can see the document history there). It includes k-finality, a slightly weird version of the Casper FFG fork choice rule, and the two Casper commandments as we use them today. However, the beacon chain now uses 32 slot epochs rather than 64, and we did not implement the dynamic validator set mechanism.

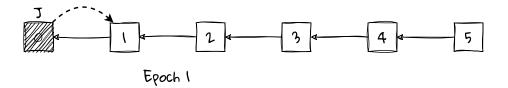
The current Casper FFG specification is maintained as part of epoch processing in the beacon chain's state transition function.

Answer to the Exercise

Here's the answer to the exercise above.

Answer

Suppose that attestations are always delayed by exactly one epoch, so that votes made in epoch N are not processed until epoch N+1, and consider the following progress of the Casper FFG algorithm.



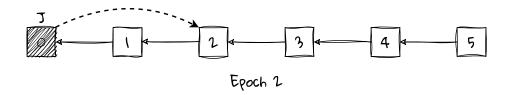
We start with Checkpoint 0 being justified. During Epoch 1 everyone votes $0 \to 1$ as usual. The supermajority link vote is shown dashed because processing the votes will be delayed until the next epoch.

See also

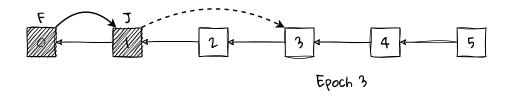
The original Casper the Friendly Finality Gadget paper remains the canonical reference. Although the details of our implementation in Ethereum 2.0 differ in some respects, the foundations remains the same.

That paper also discusses using an "inactivity leak" to recover from catastrophic crashes (section 4.2). I've covered elsewhere how we've implemented the inactivity leak in Eth2.

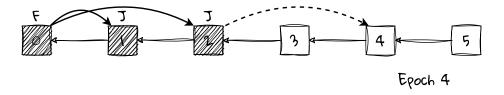
³⁸Footnote four of the Casper FFG paper explains the thinking behind reducing the number of message types from four to two.



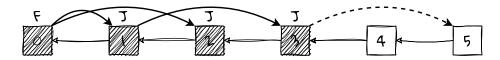
At the end of Epoch 1, no votes have been seen, due to the delay, so Checkpoint 1 remains unjustified. During Epoch 2 everyone votes $0 \to 2$.



At the end of Epoch 2, we can process the Epoch 1 votes, which justify Checkpoint 1 (and finalise 0, but that's irrelevant). Checkpoint 2 remains unjustified as we haven't seen the Epoch 2 votes yet. During Epoch 3 everyone votes $1 \rightarrow 3$.



Justification continues to lag one epoch behind due to the delayed attestations. During Epoch 4 everyone votes $2 \rightarrow 4$.



We are now perpetually locked into this leap-frog behaviour where votes always skip a checkpoint because the skipped checkpoint's justification always happens one epoch late.

Once again, Vitalik's Casper history Tweet storm (also available here and here) provides terrific first-hand background to the development of the Casper consensus protocols, CBC and FFG.

In the consensus layer specifications:

- Justification and finalisation calculations are performed during epoch processing, the entry point being process_justification_and_finalization(), with the main work done by weigh_justification_and_finalization(), including the k-finality handling.
- Rewards and penalties are applied during epoch processing by process_rewards_and_penalties(), but this is only a simple totting up the rewards calculated block-by-block in process_attestation().
- Casper FFG slashing violations are handled by process_attester_slashing().

One of the better articles I've found on Casper FFG is by Juin Chiu. It is particularly good on the relationship between Casper FFG and classical PBFT. Vitalik's Minimal slashing conditions article contains many insights (even if those slashing conditions did not turn out to be minimal).

Some formal verification work on the guarantees of Casper FFG (as presented in the original paper, that is, without k-finality, for example) is described in the Verification of Casper in the Coq Proof Assistant (2018) paper. It contains some useful insights that clarify the assumptions behind the plausible liveness proof, in particular.

Gasper

TODO

Safety and liveness in Gasper

TODO

Heads and tails

TODO

Issues and Fixes

LMD GHOST

TODO

Attestation consideration delay

TODO

Attestation recency

TODO. See the Annotated Fork Choice.

Attestation equivocation

TODO. See the Annotated Fork Choice.

Reorgs and Reversions

TODO

Ex ante reorgs

TODO

Ex post reorgs

Proposer boost

TODO. See the Annotated Fork Choice.

Casper FFG

Casper FFG's fork choice can cause long reorgs

Casper FFG's fork choice rule says that the underlying consensus protocol must follow the chain with the highest justified checkpoint. This guarantees Casper FFG's plausible liveness, but can also lead to long reorgs in exceptional circumstances.

Such an incident occurred on Ethereum's Goerli testnet on the 28th of July, 2023. The following explanation is guided by the excellent analysis by Potuz.

If we look at Epoch 192879 on the Goerli testnet, we notice that it has an initial block in Slot 6172128, but all subsequent blocks in the epoch are either missing completely or were orphaned. A fork choice visualiser shows that the proposers in Epoch 192880 simply ignored everything after the first slot of Epoch 192879 and chose instead to build on the block in Slot 6172128.

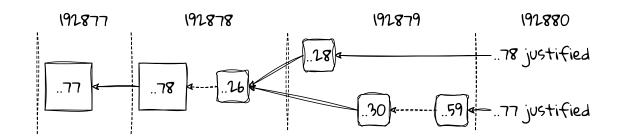
So, what happened?

- 1. Unusually, Checkpoint 192878 had not been justified by the end of Epoch 192878, since not enough votes had been accumulated.
- 2. The block at Slot 6172128, at the start of Epoch 192879, contained enough votes to justify Checkpoint 192878, but the block was published very late.
- 3. Subsequent proposers correctly ignored the block at Slot 6172128 due to its lateness and instead built a chain on the block at Slot 6172126. They continued building this chain throughout Epoch 192879.
 - However, the blocks on this new chain did not include the votes that would have justified Checkpoint 192878. By design, blocks have limited space for attestations. Due to several slots being empty, attestation space was congested.
 - They also did not have enough votes to justify Checkpoint 192879 by the end of Epoch 192879.
- 4. After epoch processing at the end of Epoch 192879 we have two branches:
 - 1. the first contains a single block in Epoch 192879, at Slot 6172128, and Checkpoint 192878 is the highest justified;
 - 2. the second contains many blocks in Epoch 192879, and Checkpoint 192877 is the highest justified.
- 5. At start of Epoch 192880, Casper FFG's fork choice says that Block 6172128 must be the new head since it has the highest justified checkpoint, and all of the subsequent blocks in Epoch 192879 must be ignored.

This was not due to an implementation bug, but due to Casper FFG's fork choice. If the bottom fork had remained canonical in epoch 192880, any validator following the top fork, and not seeing the blocks on the bottom fork until much later, would be forced eventually to move its justified epoch back from 192878 to 192877, potentially requiring them to make slashable surround votes in future.

The severity of the reorg was exacerbated by:

- the length of epochs, with accounting being performed only every 32 slots;
- overall participation rates that were close to the 67% supermajority threshold;
- a block (at slot 6172128) that contained key justification information having been published late;
- several empty slots that caused contention for block space, so that important attestations were excluded from the longer chain in Epoch 192879; and
- too tight a time window for attestations to be included, which ought to be helped by the change planned in EIP 7045.



During epoch processing at the end of 192879, the top branch contains votes that justify Checkpoint 192878, while the bottom branch does not contain sufficient votes to justify either 192878 or 192879. Casper FFG's fork choice forces proposers in 192880 to build on the branch with higher justification. As a result, all blocks in slots 6172130 to 6172159 were orphaned (reorged). The large squares are checkpoints, the rounded squares are blocks.

Note that all of this is independent of the separate issues around unrealised justification.

This scenario would be very unlikely to occur on the Ethereum Mainnet, principally because participation is almost always over 99%, way above the supermajority threshold, and blocks are much more rarely missed than on the testnets.

Gasper

TODO

Unrealised Justification

TODO. See the Annotated Fork Choice.

Weak Subjectivity

The two great problems that had to be solved in order for proof of stake to be a sound foundation for the world's economic activity were (1) the nothing at stake problem, and (2) long range attacks.

Ethereum's consensus solves the nothing at stake problem – that it is costless for a proof of stake validator to equivocate on every block proposal, building on every fork rather than picking one – with a slashing mechanism. The long range attack problem is solved by embracing weak subjectivity.

The Progress of a Slot

Introduction

TODO

Proposing

TODO

Attesting

TODO

Aggregating

TODO

Sync Committee Participation

The Progress of an Epoch

Introduction

TODO

Applying Rewards and Penalties

TODO

Justification and Finalisation

TODO

Other State Updates

Validator Lifecycle

Introduction

Deposits and Withdrawals

- Deposits are transfers of Ether from the execution layer to the consensus layer.
- Withdrawals are transfers of Ether from the consensus layer to the execution layer.
- Accounting on each layer is completely separate.
- Stakers send transactions to the deposit contract in order to stake.
- Staking is permissionless.
- Withdrawals are periodic and automatic.
- Withdrawals are either partial or full.

Overview

As a proof of stake protocol, Ethereum depends on stakers locking up capital within the protocol (deposits), and, eventually, receiving that capital back along with the rewards they have earned (withdrawals).

The form of capital that is staked is Ether (ETH), Ethereum's native currency. Ether on the consensus layer exists separately, and is accounted for separately, from Ether in normal Ethereum accounts and contracts. Ether on the consensus layer is in the form of balances of validator accounts. Validator accounts are extremely limited: they have a balance that increases due to deposits and rewards, and decreases due to withdrawals and penalties. You cannot make transfers between validator accounts or run any kind of transaction on them. Validator account balances are tracked as part of the beacon state, and do not form part of the normal Ethereum execution state. Note that execution balances are denominated in Wei (10^{-18} ETH) , whereas validator balances are denominated in Gwei (10^{-9} ETH) .

The basic architecture (that we'll cover thoroughly in the following sections) is that stakers make a deposit by sending an Ethereum transaction to the deposit contract, which is a standard Ethereum smart contract on the execution layer. It is important that staking is completely permissionless. Anybody may stake and gain the right to run a validator by sending 32 ETH to the deposit contract in a normal Ethereum transaction.

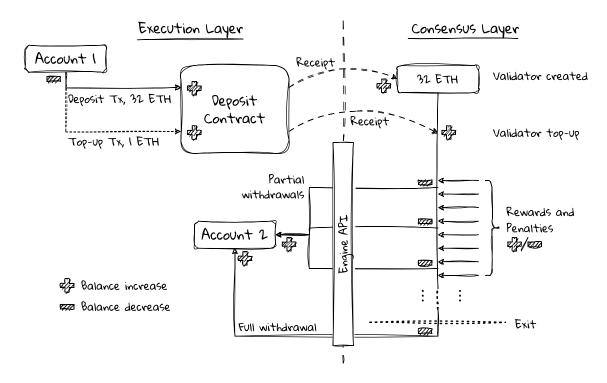
On receiving a deposit, the deposit contract emits a receipt. After a while, this receipt is picked up by the consensus layer, and a validator account is created and credited with the deposit amount. The staker can then run an Ethereum validator.

All being well, the validator will earn rewards. These will be periodically, and automatically, debited from the validator's balance and credited to the Eth1 account specified in the withdrawal credentials, the withdrawal address.

When the validator finally signals that it wants to exit the protocol (or is slashed), then any remaining balance is debited from the validator account and credited to the withdrawal address.

The whole flow is illustrated in the following diagram.

An amusing observation from the diagram is that there is no minus sign attached to the deposit contract: the deposit contract's balance is "up-only" as validators exit and restake. When a validator exits and restakes, the deposit contract's balance increases by 32 ETH while everything else is essentially unchanged. If this were to happen 3.2 million times (not inconceivable with well over half a million validators currently staked) then the balance of the deposit contract would exceed the total amount of Ether that's ever circulated, roughly 120 million ETH. This is of no importance, except to underline that the balance of



A sketch of the flows of deposits and withdrawals for a validator. Time runs roughly from top to bottom. Top-up deposits are optional, but shown for completeness. Accounts 1 and 2 may be the same, and may be contracts. Account 2 is the withdrawal address.

the deposit contract should be considered burned, and counted as zero when totting up Ethereum's total supply. 39

More importantly, there are two types of deposit and two types of withdrawals. A validator is created when its first deposit is processed by the consensus layer (which may or may not be enough to activate it). Any subsequent deposits for the same validator are top-up deposits and have a slightly different workflow with less validation.

As for withdrawals, partial withdrawals are regular transfers of anything above 32 ETH from the validator's balance to the execution layer. A full withdrawal occurs when the validator has exited the protocol and has become "withdrawable", at which point the whole of the validator's remaining balance will be transferred. Both types of withdrawal occur automatically and periodically.

In the following sections, we will look first at the mechanics of making a deposit, followed by an in-depth study of the deposit contract. We will close by looking at the consensus layer mechanics for processing deposits and withdrawals.

A constant theme of the next sections is that much of the complexity in the current deposit and withdrawal processes has arisen due to Ethereum's peculiar history. The deposit contract's incremental Merkle tree, the Eth1Data voting period, the Eth1 follow distance - all these are due to the execution layer having remained on proof of work while we built a separate beacon chain on proof of stake. The whole BLS withdrawal credentials saga arose from our uncertainty about the roadmap at the time.

Another theme is that, post-Merge, we have the opportunity to clean some of this up. EIP-6110 is a proposal for significantly streamlining deposit handling. Nevertheless, some of the complexity will be with us forever.

³⁹Now that the Engine API is available, we could in principle reduce the deposit contract's balance whenever a receipt is processed on the consensus layer, but the added complexity is undesirable only to fix this quirk.

Making a Deposit

- Initial deposits create a validator's record.
- Top-up deposits increase an existing validator's balance.
- Making a deposit involves sending a transaction to the deposit contract.
- The Ethereum Launchpad provides a nice interface for this, although alternatives exist.
- The deposit CLI tool, among others, can create deposit data and BLS keystores.

Introduction

This is not a how-to guide, so I'll only consider the main tools and workflows as an introduction to the ideas.

The Ethereum Foundation's Staking Launchpad is the entry point for many solo stakers. Large operations might use smart contracts to submit deposits in batches, but we will focus on a single deposit of 32 ETH.

The Launchpad will guide you towards using the staking deposit CLI tool⁴⁰. It is strongly recommended that you run the deposit CLI tool offline, possibly air-gapped and on a live-booted machine. This is to keep your mnemonic seed phrase as safe as possible⁴¹.

Initial deposits

When making an initial deposit – that is, for a validator that does not exist yet – the staking CLI can be run interactively as follows.

```
./deposit new-mnemonic --execution_address '0x00....09'
```

By default, without the --execution-address parameter, the staking CLI will generate old-style BLS withdrawal credentials. You'll want to be using the new-style Eth1 withdrawal credentials, so specify the address of an Ethereum account that you control here. If you don't do it now, you will need to change it later to receive your rewards and retrieve your stake.

The tool will generate a new 256 bit seed using your machine's randomness and convert it into a 24 word mnemonic phrase based on the BIP-39 standard. A single mnemonic seed phrase can be used to generate a large number of BLS12-381 private—public key pairs, and hence a large number of validators. Keep this mnemonic phrase very safely somewhere, and never online. You will need it if you ever need to recreate your validator keys, and when you exit your validator.

You can generate keystores for multiple validators at once, based on the same mnemonic. Just tell the deposit CLI how many. Each will need its own 32 ETH stake, however.

After running through all the prompts and confirmations, the deposit CLI will generate some files. There will be a single deposit_data-xxx.json file and one keystore-m_12381_3600_0_0_n_xxx.json files per validator you generated.

⁴⁰Eth-staking-smith is an alternative. I have not used it and cannot vouch for it, though the source is legit. It has the interesting feature of being able to use PBKDF2 as the key derivation function - see below.

⁴¹It used to be more important to protect your mnemonic as it controlled your withdrawal credentials as well as your signing key. Nowadays it will normally be used only for your signing key - an attacker can do you less harm with that than with the withdrawal credentials.

Deposit data

The deposit_data-xxx.json file is part of the Launchpad's workflow; other tools may have different ways to do this. When you submit the deposit data file to the Launchpad, it will create a deposit transaction for each validator, which you sign with your normal Ethereum wallet, thereby sending 32 ETH to the deposit contract.

The file contains a section like this for each validator (I've truncated some lines for convenience).

The fields are as follows.

- pubkey is generated from the secret key that was generated from your mnemonic. It is the unique identity of the validator on the consensus layer. You can look it up on the Beaconcha.in explorer, for example.
- withdrawal_credentials will begin with 01 if you specified the execution_address, and end with the 40 hexadecimal digits of the Ethereum account that withdrawals will go to. If you did not specify an execution_address, then withdrawal_credentials will begin 00 and be followed by a BLS withdrawal commitment.
- amount is in Gwei. 32000000000 is 32 ETH.
- signature is a BLS signature over the previous three fields, using your secret signing key.
- deposit_message_root is the actual data that is signed with signature. It is the hash tree root of the DepositMessage object. It's technically redundant as it can be recalculated easily, but the Launchpad uses it as a checksum to validate that the submitted data and signature all validate correctly.
- deposit_data_root is the hash tree root of the DepositData object created from the first four fields above (i.e. deposit message plus its signature). This is used as a checksum by the deposit contract.
- fork_version specifies which chain the deposit is for. The fork_version is encoded into the signature so that deposits are valid only on the intended chain. The chain's GENESIS_FORK_VERSION is always used when signing deposits.

The remaining fields are just administrative records.

Keystores

Also generated by the deposit CLI is a keystore file for each validator. This contains the validator's encrypted secret key. The keystore will be used by the staker's client software and needs to be installed as per the client's instructions. The keystore contents are protected by the password provided when the deposit CLI was run, which also needs to be provided to the staking client. Each client handles this differently, so consult the docs.

Example keystore

A keystore file has contents like the below. You can see that the pubkey matches the pubkey in the deposit data file, above. I won't go into the details of this, but the format is described in ERC-2335. The derivation path parameter is discussed in ERC-2334.

```
{
    "crypto": {
        "kdf": {
```

```
"function": "scrypt",
      "params": {
        "dklen": 32,
        "n": 262144,
        "r": 8,
        "p": 1,
        "salt": "d6679024b3693066eba27bbe7c2269fc62c98a1accf225c916d6eafb24abcdae"
      },
      "message": ""
    },
    "checksum": {
      "function": "sha256",
      "params": {},
      "message": "402eb9c5d6042f354bb8013ed19019b9d8cfa7deed1ed44eb2c0680615df1b13"
    },
    "cipher": {
      "function": "aes-128-ctr",
      "params": {
        "iv": "4ced4174acc07417f34106eb1cb5c685"
      },
      "message": "e7adc1ab79c2870fccd87b9cbd09830fcf0654cccca944ff3c9c26a1f6fb10b5"
   }
  },
  "description": "",
  "pubkey": "a70d57e5fd4615bd3110a709be82be7a8b966fe881290f2738e4d8d0b38f39fe..."
  "path": "m/12381/3600/0/0",
  "uuid": "7b25b4a7-9241-4ad8-9540-f0ed096f30cd",
  "version": 4
}
```

A key derivation function (KDF) is used to protect the secret key with a password. The KDF is designed to make it computationally infeasible to decrypt the secret key by brute-force.

The deposit CLI uses the Scrypt KDF which, by design, is slow and uses a lot of memory, about 300MB per key. This is fine for a solo-staker loading one or two keys, but can become a significant bottleneck for large staking services loading hundreds or thousands of keys at startup.

ERC-2335 keystores also support PBKDF2 as the KDF, which is much faster and less memory intensive. Depending on one's appetite for trading key security for loading speed, PBKDF2 may be preferable. The ethdo and eth-staking-smith tools are able to generate keystores using PBKDF2.

Top-up deposits

Top-ups are deposits for validators that already exist. You might want to top-up a validator if its effective balance falls below 32 ETH in order to restore it to maximum effectiveness.

The Staking Launchpad provides a top-up interface. You don't need access to your keystore or mnemonic to make a top-up deposit. In fact, anyone can top-up any validator at any time.

The transaction that gets sent to the deposit contract for a top-up is essentially the same as the transaction for an initial deposit, with the following differences:

- the public key must match the public key of an existing validator,
- the signature is not checked, and can be an "empty" dummy signature 42, and
- the withdrawal credentials are ignored.

It is possible to build up a validator's stake over time, with an initial deposit that's less than 32 ETH, followed by one or more top-up deposits. The validator will become active when its effective balance reaches 32 ETH. However, if you plan to do this, watch out for a tricky edge case involving hysteresis when the final top-up is 1 ETH.

 $^{^{42}}$ It seems that block explorers do not know this and can incorrectly mark top-up transactions as invalid.

See also

The Ethereum.org website has more information about solo staking, with a comparison of alternatives to the deposit CLI tool.

If you want to play around with consensus layer keys and wallets, the **ethdo** tool is extremely useful. It has been audited, and has a huge range of features as well as handling the basics.

Three ERC standards have been proposed in relation to key handling for the consensus layer.

- ERC-2333: BLS12-381 Key Generation.
- ERC-2334: BLS12-381 Deterministic Account Hierarchy.
- ERC-2335: BLS12-381 Keystore.

The Deposit Contract

- The deposit contract is the protocol's entry point for staking.
- Anybody may permissionlessly stake 32 ETH via the contract.
- On receiving a valid deposit the contract emits a receipt.
- An incremental Merkle tree maintains a Merkle root of all deposits.
- The deposit contract cannot verify a deposit's BLS signature.
- The balance of the deposit contract never decreases.
- Ether sent to the deposit contract should be considered burned.

Overview

The deposit contract is the means by which stakers commit their Ether to the protocol in order to gain the right to run a validator.

The source code for the contract is available in the specs repo, and the verified byte code is deployed on-chain.

Functionality

The deposit contract is a normal Ethereum smart contract running on the execution (Eth1) layer. Anyone wishing to place a stake in order to run a validator may send 32 ETH to the deposit contract via a normal Ethereum transaction.

In addition to the Ether transferred, the deposit transaction must contain further data as follows.

First, the public key of the validator. A validator's public key is derived from its secret signing key, and is its primary identity on the consensus layer. The staker will provide the secret signing key separately to the consensus client for normal operational use.

Second, withdrawal credentials specifying which Ethereum account rewards earned will be sent to. This will also be the address that receives the validator's full balance when it eventually exits. Withdrawal credentials come in two forms, which we will discuss later.

Third, a signature over the public key, the withdrawal credentials, and the deposit amount, using the normal signing key. This signature's main role is to serve as a "proof of possession" of the secret key of the validator, which side-steps a nasty rogue public key attack.

Fourth, the deposit data root, which is an SSZ Merkleization of all of the above data that serves as a kind of checksum that the contract can verify.

The deposit contract does some verification on these parameters. In particular, the deposit amount is subject to checks, and the deposit data root is verified. If either of these fails then the deposit will be rejected - that is, the deposit transaction will be reverted.

However, the deposit contract does not validate the signature - the EVM does not yet have the elliptic curve apparatus to do this, and it would be prohibitively expensive to do in normal bytecode. The signature will be validated later by the consensus layer, and if found to be incorrect (for new validators) the deposit will fail, and the Ether will be lost.

Once the deposit contract is as satisfied as it can be that the deposit is valid, it issues a receipt (an EVM log event) containing the deposit data. This receipt will later be picked up by the consensus layer for processing.

Development

The original deposit contract was written in Vyper, a Python-like smart contract language. Work on the contract code began in January 2018, some months before the beacon chain was conceived of: it is one of the very few carry-overs from earlier Ethereum proof of stake designs. The pre-beacon chain version, however, omitted all the of the Merkle tree apparatus as it was not required⁴³. Using the incremental (also called progressive) Merkle tree was suggested by Vitalik in January 2019.

Around April 2020, work began to rewrite the deposit contract in Solidity, a more mainstream smart contract language. The stated reason in the new repo is the following, which relates to formally verifying the contract.

The original motivation was to run the SMTChecker and the new Yul IR generator option (--ir) in the compiler.

Runtime Verification's verification work cites "community concerns about the [then] current Vyper compiler" as the motivation for the rewrite. These concerns are captured in Suhabe Bugrara's initial review of the Vyper contract, and discussed in the Ethereum Foundation's blog entry.

The deployed deposit contract was compiled from Solidity source code.

Verification work

Since Ethereum contracts are immutable once deployed, it was crucial that the deposit contract be correct: its balance would come to be a large fraction of all Ether. To this end, various analyses and formal verification activities were performed.

In June 2020 Runtime Verification performed a formal verification covering two aspects.

- 1. Verification that the incremental Merkle tree algorithm is equivalent to a full Merkle tree construction.
- 2. Verification that the bytecode was correctly generated from the Solidity source code, using the KEVM verifier.

Just prior to the deployment of the contract, Franck Cassez of Consensys performed some further work as described in his paper, Verification of the Incremental Merkle Tree Algorithm with Dafny, and GitHub repository. This goes further than Runtime Verification's work by fully mechanically verifying the incremental Merkle tree algorithm, using the Dafny formal verification language.

Deployment

The deposit contract was deployed on October the 14th, 2020, at 09:22:52 UTC to Ethereum address 0x00000000219ab540356cbb839cbe05303d7705fa.

The deploying account was presumably generated by grinding for a key whose first transaction would deploy the contract to an address with the distinctive eight zero prefix: Ethereum contract addresses are computed from the deployer's account address and nonce value. This would have taken on the order of 2^{32} (4.3 billion) key generation attempts.

 $^{^{43}}$ With EIP-6110 we might end up going back in that direction, with the Merkle root no longer needed.

Ignoring spam, there are only three transactions associated with the deploying account.

- The account was funded with 1 ETH (minus fee) via a transfer from Tornado Cash.
 - As a result, we have no way of identifying the deployer. Since the contract bytecode was publicly available, it could have been anybody.
- The deposit contract deployment cost 0.31478286 ETH.
- The leftover ETH was transferred to the WikiLeaks donation address.

Code

The following exposition is based on the Solidity source code as verified on Etherscan, which ought to match the source code in the consensus specs repository.

For brevity, I've omitted the interface boilerplate and some lengthy comments.

DepositContract

```
contract DepositContract is IDepositContract, ERC165 {
   uint constant DEPOSIT_CONTRACT_TREE_DEPTH = 32;
   // NOTE: this also ensures `deposit_count` will fit into 64-bits
   uint constant MAX_DEPOSIT_COUNT = 2**DEPOSIT_CONTRACT_TREE_DEPTH - 1;

   bytes32[DEPOSIT_CONTRACT_TREE_DEPTH] branch;
   uint256 deposit_count;

   bytes32[DEPOSIT_CONTRACT_TREE_DEPTH] zero_hashes;

   constructor() public {
        // Compute hashes in empty sparse Merkle tree
        for (uint height = 0; height < DEPOSIT_CONTRACT_TREE_DEPTH - 1; height++)
              zero_hashes[height + 1] = sha256(abi.encodePacked(zero_hashes[height], zero_hashes[height]));
   }
}</pre>
```

After declaring its interfaces – we will look at ERC165 below – comes constants and storage.

The DEPOSIT_CONTRACT_TREE_DEPTH specifies the number of levels in the internal Merkle tree. With a depth of 32, it can have 2^{32} leaves, allowing for up to 4.3 billion deposits (MAX_DEPOSIT_COUNT⁴⁴)⁴⁵. A deposit is a minimum of one ETH, so there's sufficient space for every ETH in existence to be deposited 35 times over.

The underlying data structure of the deposit contract is an incremental Merkle tree. This is a Merkle tree that supports only two operations, (1) appending a leaf, and (2) calculating the root. Constraining the data like this allows us to avoid storing the entire Merkle tree, which would be huge. Instead the contract stores only the last branch – a mere 32 nodes – which is all the information that's needed to calculate the Merkle root.

To gain this efficiency, we need an array of zero_hashes. At any given level of the tree, the zero hash is the value the node would have if all of the leaves under it were zero. Since we assign leaves sequentially, huge parts of the tree can be represented by the zero hashes.

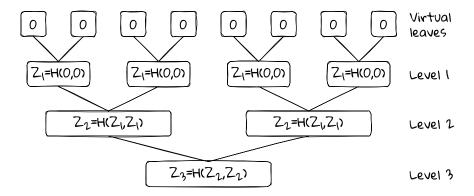
The constructor() (which takes no arguments) only initialises the zero_hashes structure, taking advantage of the EVM's default that the uninitialised zero_hashes[0] storage value will be zero.

get_deposit_root

```
function get_deposit_root() override external view returns (bytes32) {
   bytes32 node;
```

⁴⁴Regarding the comment on MAX_DEPOSIT_COUNT, it will of course fit into 32 bits, which is definitely less than 64. The point is that uints on the consensus layer are standardised at a size of 64 bits, and we don't want to overflow that.

⁴⁵With the proposed mechanism in EIP-6110 for deposit handling, we would no longer need the Merkle proofs and could in principle lift this limit. However, it is immutably encoded into the deposit contract, so would not be possible in practice.



To construct Z_n , we start with $Z_0 = 0$ and define $Z_{i+1} = \operatorname{Hash}(Z_i, Z_i)$.

```
uint size = deposit_count;
for (uint height = 0; height < DEPOSIT_CONTRACT_TREE_DEPTH; height++) {
    if ((size & 1) == 1)
        node = sha256(abi.encodePacked(branch[height], node));
    else
        node = sha256(abi.encodePacked(node, zero_hashes[height]));
    size /= 2;
}
return sha256(abi.encodePacked(
    node,
    to_little_endian_64(uint64(deposit_count)),
    bytes24(0)
));</pre>
```

Calculating the deposit root on demand saves us from having to use a storage slot to save it in. Local execution of view functions is free, while writing to blockchain state is very expensive.

The algorithm works as follows. In a binary Merkle tree, a node is either a left child or a right child.

- If a node is a left child (size & 1 == 0), we know its sibling must be a zero hash, since the tree is
 incremental.
- If a node is a right child, we take its sibling from branch. Thus, the important elements of branch are those that store the left-child nodes for the current value of deposit_count.

In effect, we are using the zero_hashes, Z_n , and the branch values, B_n , to summarise large parts of the tree. Z_n is the root of a subtree whose 2^n leaves are all zero, with $Z_0 = 0$. B_n is the root of a subtree, all of whose 2^n leaves were previously assigned, with B_0 being the last left-leaf that was inserted. By the time we reach the root, we will have effectively included all the leaves in the calculation.

This being an incremental Merkle tree, we know that the value of the leaf at deposit_count is zero: the count is zero-based, so leaf deposit_count has not yet been assigned; it will be the next leaf to be assigned.

To calculate the parent node, we hash together the value of its left and right children. Solidity's abi.encodePacked() function is used to concatenate the 32 bytes of each sibling.

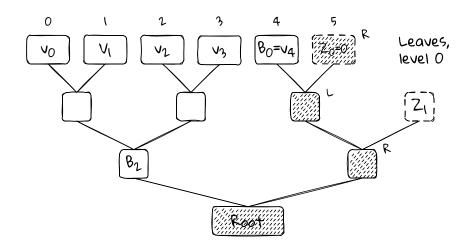
Note that we don't use any of the B_n for $n > \log_2 i$, where i is deposit count - any nodes we visit higher than this will be left nodes only. We make use of this when updating branch after a new deposit.

Toy example

}

The beauty of the incremental Merkle tree is that we can calculate a root for a tree with up to N leaves by maintaining just $\log_2 N$ values in storage, plus the deposit_count, with a further $\log_2 N$ constants.

The diagram shows an incremental Merkle tree with three levels. We have filled up five of the leaves with values v_0 to v_4 , but the only things that we actually store are the three B_n values of branch, and



Finding the root of a three-level incremental Merkle tree. Five leaves have been assigned, v_0 to v_4 , although we don't store their values. In the algorithm, node visits the dashed nodes from the leaf at the top to the root at the bottom. The B_n are branch values maintained by deposit(), and the Z_n are the pre-computed zero_hashes.

the three Z_n values of zero_hashes. At each level n we will use either B_n or Z_n to calculate the parent.

The deposit_count is 5, so we start with node at the leaf labelled "5", which we know will be zero since it has not yet been assigned. This is a right child, therefore we combine it with B_0 as its left sibling. We know that B_0 will be equal to the last leaf value inserted, v_4 . (If it were a left child, we would combine it with $Z_0 = 0$.)

Moving to level 1, node is now a left child, so we combine it with the level 1 zero hash, Z_1 . We know that all the leaves descended from that Z_1 node are zero.

On level 2, node is again a right child, so we combine it with our stored value of B_2 to obtain the value at the root of the tree.

Why do we need the deposit root?

As we shall see later, each staking node separately maintains its own Merkle tree of deposits, independently of the deposit contract, which it builds using the deposit receipts from the execution layer. Why, then, do we need to put all this complex apparatus into the deposit contract in order to calculate the root?

Using the deposit root provides a self-contained way to verify that the deposit data in a block is correct. In the early stages of Eth2, it was not at all clear that all beacon chain nodes would be connected to Eth1 clients. In fact, pre-Merge, it was perfectly fine for a non-staking node not to be connected to an Eth1 client. Those nodes needed some way to be able to reject blocks with fake deposits. Putting the evidence on-chain via a Merkle proof allowed them to do so.

By means of the voting process described below, validators periodically import a deposit root from the contract onto the beacon chain. When a proposer includes deposits in its block, it must add a proof that the deposits are included in that deposit root. This allows every node that processes the chain to verify every deposit without having to consult the Eth1 chain.

Interestingly, post-Merge, all nodes (whether running validators or not) are required to comprise both consensus and execution clients, and execution payloads are included in beacon blocks. Therefore, nowadays, the data we need to validate deposits is on-chain as a matter of course, and we no longer strictly need to mess about with all this deposit root stuff. In fact, EIP-6110 proposes to explicitly expose validator deposits on-chain, after which the deposit contract code for maintaining the root will be redundant. Although, being immutable, it will continue to exist forever.

get_deposit_count

```
function get_deposit_count() override external view returns (bytes memory) {
    return to_little_endian_64(uint64(deposit_count));
}
```

The only wrinkle here is the endianness transformation. The consensus layer uses little-endian format to serialise integers, whereas the EVM uses big-endian. The consensus layer calls this function to find out about new deposits, so it's convenient to get the output in the right format.

deposit

```
function deposit(
   bytes calldata pubkey,
   bytes calldata withdrawal credentials,
   bytes calldata signature,
   bytes32 deposit_data_root
) override external payable {
   // Extended ABI length checks since dynamic types are used.
    require(pubkey.length == 48, "DepositContract: invalid pubkey length");
    require(withdrawal_credentials.length == 32, "DepositContract: invalid withdrawal_credentials
                                    \hookrightarrow length");
   require(signature.length == 96, "DepositContract: invalid signature length");
   // Check deposit amount
   require(msg.value >= 1 ether, "DepositContract: deposit value too low");
    require(msg.value % 1 gwei == 0, "DepositContract: deposit value not multiple of gwei");
   uint deposit_amount = msg.value / 1 gwei;
    require(deposit amount <= type(uint64).max, "DepositContract: deposit value too high");</pre>
```

This is the business part of the contract - where stakers' deposits are made.

A deposit comprises the following items.

- The public key of the validator: pubkey is the 48 byte (compressed) BLS public key derived from the staker's secret signing key.
- The withdrawal credentials: withdrawal_credentials is 32 bytes of either 0x00 BLS credentials or 0x01 Eth1 credentials. Apart from their length, the withdrawal credentials are not validated anywhere in the contract, or even on the consensus layer.
- The signature is a 96 Byte BLS signature. It is generated by signing the hash tree root of a DepositMessage object (public_key, withdrawal_credentials, and deposit_amount), with the validator's signing key.
- The deposit data root is basically a form of checksum. See below for how it is verified.
- Finally, a msg.value. The message value is the amount of Ether (denominated in Wei, which are 10^{-18} ETH) that was sent with the transaction. This will normally be 32 ETH for a new validator, but can be more or less. It must be,
 - at least one ETH,
 - a whole number of ETH, and
 - less than 2⁶⁴ Gwei⁴⁶, which is 18.4 Billion ETH.

The very last condition is formally to avoid overflowing a consensus layer uint64, but seems kind of redundant in practice.

```
// Emit `DepositEvent` log
bytes memory amount = to_little_endian_64(uint64(deposit_amount));
emit DepositEvent(
   pubkey,
   withdrawal_credentials,
```

 $^{^{46}}$ A Gwei is 10^9 Wei, or 10^{-9} ETH, and is the unit of account on the consensus layer.

```
amount,
signature,
to_little_endian_64(uint64(deposit_count))
);
```

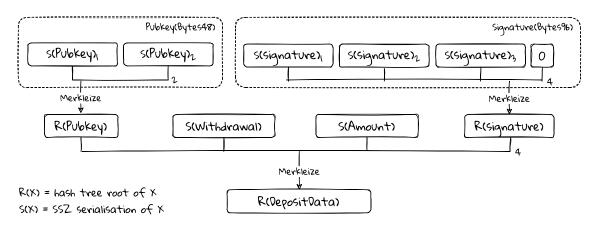
The contract now emits an event log (receipt). These receipts are how information about new deposits is picked up by the consensus layer. It looks a bit weird to emit the log before finishing all the checks (we have a couple more requires to pass yet), but if the transaction reverts, the beacon chain will also revert the event log, so no real harm is done emitting it early.

See below for more detail on the receipt.

Here we have a "by hand" implementation of the hash tree root for a consensus layer DepositData object.

```
class DepositData(Container):
   pubkey: BLSPubkey
   withdrawal_credentials: Bytes32
   amount: Gwei
   signature: BLSSignature # Signing over DepositMessage
```

Using the same style as in the Merkleization chapter, we can illustrate the process in the following diagram. With a bit of head-scratching it's not too difficult to map it onto the mess of sha256 calls in the code.



Each box is a 32 byte chunk, possibly padded with zeros (in the cases of $S(Pubkey)_2$ and S(Amount)). Merkleization is the process of finding the hash tree root by iteratively hashing together pairs of chunks, in the form of binary trees, until the root is reached.

The only reason for doing this here is as a kind of checksum. The staker provides <code>deposit_data_root</code>, which is their independent calculation of the deposit root from the input data. The contract recalculates it to ensure that it matches the supplied data.

The deposit_data_root is the quantity (node) that will be inserted as a new leaf in the Merkle tree and forms part of the verification of a deposit on the consensus layer.

```
// Avoid overflowing the Merkle tree (and prevent edge case in computing `branch`)
require(deposit_count < MAX_DEPOSIT_COUNT, "DepositContract: merkle tree full");

// Add deposit data root to Merkle tree (update a single `branch` node)
deposit_count += 1;
uint size = deposit_count;
for (uint height = 0; height < DEPOSIT_CONTRACT_TREE_DEPTH; height++) {
    if ((size & 1) == 1) {
        branch[height] = node;
        return;
    }
    node = sha256(abi.encodePacked(branch[height], node));
    size /= 2;
}
// As the loop should always end prematurely with the `return` statement,
// this code should be unreachable. We assert `false` just to be safe.
assert(false);
}</pre>
```

Finally, we must update the Merkle tree.

A very cool feature of the incremental Merkle tree is that, not only can we continuously maintain its root by maintaining only the 32 values in branch, but when we insert a new leaf value, we need to update only a *single value* of branch.

This is not obvious, but we can deduce it as follows. For a more formal explanation and analysis, see Franck Cassez's paper, Verification of the Incremental Merkle Tree Algorithm with Dafny.

Consider paths from adjacent leaves to the root: path P from leaf j-1, and path Q from leaf j, where j is deposit_count. Beyond some level i, paths P and Q will converge and visit the same nodes. At level i, path P will visit a left node, having visited only right nodes previously, and path Q will visit a right node, having visited only left nodes previously.

In short,

- Path P will comprise (i-1) right nodes, followed by a left node, followed by some tail shared with O.
- Path Q will comprise (i-1) left nodes, followed by a right node, followed by some tail shared with P.

Path Q is that path that will be used in the $get_deposit_root()$ algorithm.

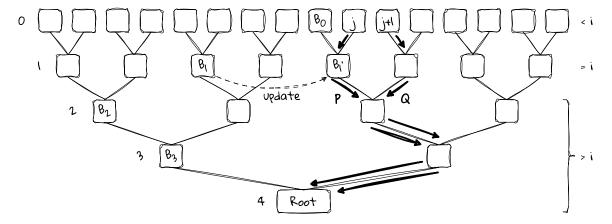
Now, by construction, the B_n (the branch values) always represent left nodes in the tree, and are needed only when path Q visits a right node.

For levels greater than or equal to i – where paths P and Q coincide – either the nodes visited are left nodes, in which case the B_n value is irrelevant, or they are right nodes, in which case the B_n value is unchanged since it is calculated from a sub tree whose leaves have not changed. So, no update is required to B_n for n > i.

As for levels n < i, all the Q_n are left nodes, and thus the B_n are irrelevant. Therefore the sole B_n that needs to be updated is B_i . The intuition is that, due to the way binary increments work, every time we need a new B_n , it have been be updated by the previous insertion, "just in time".

supportsInterface

 $^{^{47}}$ If it's not clear from thinking about paths, then consider binary numbers. If j-1 is 0111, then j is 1000. The zeros represent left nodes, and the ones represent right nodes.



We've just inserted a leaf at position j. Next time $get_deposit_root()$ is called, it will traverse path Q from j+1, having previously traversed P from j. The paths converge at height i+1. For n < i path Q is entirely left nodes, so B_n is irrelevant. For n > i, B_n is either unchanged or irrelevant. So we need only to updated B_i to B_i' .

This is standard code based on ERC-165 that allows calling applications to detect programmatically whether the contract supports a function interface based on the given function selector, interfaceID.

For example, according to the Ethereum ABI, the function selector for get_deposit_count() is 0x621fd130. Therefore, calling supportsInterface(0x621fd130) will return true.

I don't know of any reason for implementing this for the deposit contract, but I suppose it's considered good practice to do so.

to_little_endian_64

```
function to_little_endian_64(uint64 value) internal pure returns (bytes memory ret) {
    ret = new bytes(8);
    bytes8 bytesValue = bytes8(value);
    // Byteswapping during copying to bytes.
    ret[0] = bytesValue[7];
    ret[1] = bytesValue[6];
    ret[2] = bytesValue[5];
    ret[3] = bytesValue[4];
    ret[4] = bytesValue[3];
    ret[5] = bytesValue[2];
    ret[6] = bytesValue[0];
}
```

This is used in <code>get_deposit_root()</code>, <code>get_deposit_count()</code> and when emitting the <code>DepositEvent</code> log. All of these will be consumed by the consensus layer, which uses little-endian encoding for SSZ integers.

And we're done.

Deposit Receipts

For every deposit accepted by the deposit contract it issues a receipt (also called a log or event⁴⁸), which is generated via an EVM LOG1 opcode.

⁴⁸Naming of these things is really messed up. I believe that Eth1 logs, events, and receipts are all the same thing. Etherscan hedges its bets by calling them "Transaction Receipt Event Logs".

The receipt has a single topic, which is the DepositEvent signature: 0x649bbc62d0e31342afea4e5cd82d4049 e7elee912fc0889aa790803be39038c5, equal to keccak256("DepositEvent(bytes,bytes,bytes,bytes,bytes)").

The receipt's data is the 576 byte ABI encoding of pubkey, withdrawal_credentials, amount, signature, and deposit_count, converted to little-endian where required. Here's an example.

Example receipt data

The first column is the hexadecimal byte position of the start of the data in the second column.

Pointer to pubkey: 0x0a0

Pointer to withdrawal credentials: 0x100

Pointer to amount: 0x140

Pointer to signature: 0x180

Pointer to deposit_count: 0x200

Length of pubkey: 48 bytes

Pubkey data, padded with 16 zero bytes

0c0 b73fe99acbf91f0032ae95c3ed0d663ea246d02332373e101ff5c7ed520ce098
 0e0 652de3eab056a9889bb3d05d734be21400000000000000000000000000000

Length of withdrawal_credentials: 32 bytes

Withdrawal credentials (0x01 type)

120 01000000000000000000000000637a2acbc531531700fcb7d2ed7e6d96ed8bbe8

Length of amount: 8 bytes

Amount, little-endian encoded. 0x0773594000 = 32,000,000,000

Length of signature: 96 bytes

Signature data

 $1a0 \quad b4a7e1546b13be69d31849b4302d870a04867b9de73a973794f8be88c25dc71f$

 $1e0 \quad eaded 660 edb 6e0 30 df 480 74 ddf be 70 b26 d0 e9 db1 c3 be 28 afc0 b470 96 aab 7a616 \\$

Length of deposit count: 8 bytes

Deposit count, little-endian. 0x0a7bla = 686,874

A consensus client can request these receipts from its attached execution client via the standard eth_getLogs RPC method, filtering by the deposit contract address, block numbers, and event topic. This is how the consensus layer becomes aware of the details of new deposits.

The use of event logs here is an optimisation. The deposit contract could instead store all the Merkle tree's leaves and make them available via an eth_call method. However, since logs are not stored in

the chain's state, only in block history, it is much cheaper to use them than it would be to store the leaves in the contract's state. However, this places a constraint on the amount of history we must keep around - we cannot now discard block history from before the deployment of the deposit contract. A newly activated consensus client needs access to the full receipt history in order to rebuild its internal view of the Merkle tree, even if it is able to checkpoint sync its beacon state. For convenience, some clients now support starting from a deposit snapshot of the Merkle tree that can be shared with other clients in much the same way as checkpoint states. This allows aggressive pruning of block history for those who want to do that.

Deposit Processing

- The consensus layer commits to the state of the deposit contract after an 8 hour delay, with a 2048 slot voting period.
- The delay and voting are no longer necessary post-Merge and may be removed in future.
- When a new deposit root is voted in, proposers must include deposits in blocks.
- The block proposer makes an inclusion proof of the deposit against the contract's deposit root that all nodes can verify.
- Deposits for new public keys create new validator records.
- Deposits for existing public keys top up validators' balances.

Overview

The previous section on the deposit contract covered how deposits are handled on the execution layer. Now we shall look at how they get handed off to the consensus layer where the business of staking actually happens. A (valid) deposit into the execution layer deposit contract will either create a new validator on the consensus layer, or top up the balance of an existing validator.

There are two ways in which deposit information is transferred over from the execution layer to the consensus layer. One is the voting process by which the consensus layer comes to agreement on the state of the deposit contract at a particular execution block height. The other is validators directly importing deposit receipts from their attached Eth1 clients, which they will include in blocks and use to maintain their own copies of the deposit Merkle tree.

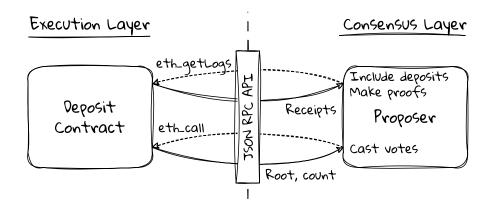
Both of these mechanisms are somewhat legacy, post-Merge, although still in place for now. There is a proposal to overhaul the whole consensus layer deposit handling workflow at some point, in the form of EIP-6110.

Eth1 Voting and Follow Distance

As mentioned above, Eth1 voting is a legacy of the pre-Merge era of the consensus layer. It is the means by which the beacon chain comes to agreement on a common view of the Ethereum 1.0 chain, and in particular, a common view of the state of the deposit contract. Post-Merge, execution payloads are included in beacon blocks, and by definition all correct beacon nodes now have a common view of the Eth1 chain.

The consensus layer's common view of the deposit contract is formed by a majority vote of beacon block proposers over a repeating cycle of 2048 slots (about 6.8 hours, see EPOCHS_PER_ETH1_VOTING_PERIOD). Each proposer includes in its block an Eth1Data vote as follows.

```
class Eth1Data(Container):
    deposit_root: Root
```



Only block proposers directly need information from the deposit contract. They acquire this by making calls to the execution layer via the standard JSON RPC interface. Proposers rely on deposit receipts for including deposits in blocks, and for maintaining a copy of the deposit Merkle tree to make proofs for those deposits. Proposers also cast a vote for a recent state of the deposit contract.

deposit_count: uint64
block hash: Hash32

The last field, block_hash, identifies a particular block on the execution chain. The deposit_root and deposit_count fields are set by calling the deposit contract's get_deposit_root() method at that block. The consensus client does this via normal JSON RPC eth_call invocations on the execution client.

During block processing, the beacon chain's process_ethl_data() function counts up the votes for each instance of Eth1Data seen in the current period. The first set of Eth1Data to be supported by more than 1024 validators (more than half of the period's block proposers) is adopted by immediately updating state.ethl_data. If no Eth1Data vote reaches the threshold during the voting period, then state.ethl_data is not updated. A fresh voting period begins only when the earlier one has run its full course of 2048 slots, even if new Eth1Data was voted in early.

Eth1 voting

Block proposers choose their Eth1 votes as described in the honest validator guide. Here's a summary of the process. We set S to be the wall clock time of the start of the current voting period. The 8 hours comes from ETH1_FOLLOW_DISTANCE (2048 Eth1 blocks) multiplied by SECONDS_PER_ETH1_BLOCK (set to 14 as an approximate average value under proof of work)⁴⁹.

- 1. First, ask the Eth1 client for all the Eth1 blocks with timestamps t in the interval, $(S-2\times8 \text{ hours}) \leq t \leq (S-8 \text{ hours})$.
- 2. Filter out any blocks that have a deposit count less than state.ethl_data.deposit_count: we've already seen these.
- 3. The proposer's default vote will be the Eth1Data from last block in this period, or if the list is empty (because Eth1 has stalled), then the winning vote from the previous voting period.
- 4. We're seeking to find agreement as quickly as possible, so an honest proposer will discard any Eth1Data that has not been voted for by other proposers already during the current period.
- 5. Finally, the honest proposer will cast a vote for the Eth1Data that already has the greatest support in the list that remains. If that list is empty (for example, if it is the first proposer in a voting period), it casts its default vote.

⁴⁹This is actually 28,672 seconds, but 8 hours is close enough for explanatory purposes. What's 128 seconds between friends?

This algorithm has been refined considerably over time. Anecdotally, Eth1 data voting has been the source of significant numbers of issues on testnets over the years. It seems to be difficult to get right, probably because it is difficult to test. Getting Eth1Data voting correct is also not incentivised by the protocol. Rather, it is mildly disincentivised, since on-boarding new validators dilutes existing validators' rewards. In any case, it will be good to see the whole thing gone.

Eth1 follow distance

Appearing in the above is an 8 hour delay, ETH1_FOLLOW_DISTANCE * SECONDS_PER_ETH1_BLOCK, before the consensus layer will even consider the state of the deposit contract.

This delay serves two functions. Under proof of work there was always a chance that blocks near the tip of the chain could be reorged out. It would be very bad for the beacon chain to include deposits that were later reverted - people might even try to "double spend" the consensus layer.

For all practical purposes, a delay of a few blocks would probably have been sufficient to counter this, since Ethereum under proof of work never suffered reversions longer than two or three blocks. Setting the follow distance as long as 8 hours is more about providing devs with enough time to respond if there were to be an incident on the Eth1 chain that might affect the deposit process, such as a chain split. In any case, this delay is now redundant as, post-Merge, the beacon chain and the execution chain move in lock-step.

The upshot of all of this is that the absolute minimum time interval between sending a deposit to the deposit contract and the consensus layer processing that deposit is around 11.4 hours: 8 hours due to the follow distance, and 3.4 hours being half of the voting period, the least required to get a majority vote. Assuming that voting is working well, the average time will be just over 17 hours. This doesn't include subsequent time waiting for the deposit to be included in a block, the validator sitting in the activation queue, etc.

For an in-depth analysis of the Eth1 follow distance and the Eth1 voting period length, see Mikhail Kalinin's Ethresear.ch article, On the way to Eth1 finality. Note that both the follow distance and the voting period have been doubled in length since the article was written.

Deposit inclusion

Let's say that new Eth1Data has been voted in, with the deposit_count, n, replacing the previous count, m < n, in the beacon state. This means that subsequent block proposers have n - m fresh deposits to include in blocks.

The deposit_root in the Eth1Data is the root of the deposit Merkle after n deposits. Block proposers must construct proofs that deposits m + 1, m + 2, ..., and n are included in that Merkle root: proofs of inclusion in the Merkle tree.

In order to do this, each validator maintains its own deposit Merkle tree based on the deposit receipts it has downloaded from its attached Eth1 client. To construct a proof that deposit m+1 is included in the tree, I need to have already built the tree that has all n deposits. Then I can easily provide the Merkle branch from leaf m+1 to the known value of deposit_root.

Beacon block proposers must include all available deposits, in consecutive order, along with their Merkle proofs of inclusion, up to a maximum of MAX_DEPOSITS. If a block fails to include all available deposits in the correct order then the entire block is invalid.

The actual data that will be included in the proposer's beacon block for each deposit is a Deposit object,

```
class Deposit(Container):
    proof: Vector[Bytes32, DEPOSIT_CONTRACT_TREE_DEPTH + 1] # Merkle path to deposit root
    data: DepositData
where DepositData is as follows,
class DepositData(Container):
    pubkey: BLSPubkey
    withdrawal_credentials: Bytes32
    amount: Gwei
    signature: BLSSignature
```

Up to MAX DEPOSITS (16) of these can be included per block.

Deposit verification

Deposits are verified by all nodes during block processing in process_deposit() and apply_deposit(). In addition, the check that the block contains the expected number of deposits (the lesser of MAX_DEPOSITS and the remaining number of deposits to be processed) is done in process_operations().

For each deposit, the first thing to be checked is its Merkle proof of inclusion. The verification is performed against the deposit root from the Eth1Data that was voted in. If a deposit passes the check, it proves that it was included in the deposit contract's tree at the same leaf position. If this check fails for any deposit, then the whole block is invalid.

When the deposit is for a new validator – that is, its public key does not already exist in the validator set – then the deposit's signature is verified. Signature verification proves that the public key belongs to a genuine, known secret key in the possession of the depositor. Importantly, a deposit with an invalid signature does not invalidate the whole block. It is just ignored and processing moves on. This is because the deposit contract was not able to validate the signature, so it is possible for invalid deposits to be present in its Merkle tree.

New Validators

If the public key in the deposit data does not already exist in the validator registry then a new validator record is created, and the deposit amount is credited to the validator's account. The deposit amount will usually be the full 32 ETH needed to activate a validator, but need not be. Later, at the end of the epoch, the validator's effective balance will be calculated - when the effective balance first becomes 32 ETH then the validator will be queued for activation, otherwise the account will just sit there inactive until the effective balance is raised to 32 ETH via a top-up deposit.

The validator's withdrawal credentials will also be set at this point. If they are 0×01 Eth1 withdrawal credentials, then they are permanent and cannot be changed in future. If they are 0×00 BLS withdrawal credentials then they may later be changed once to 0×01 credentials. See the next section for more on this.

Validator Top-ups

It is also possible to make top-up deposits for pre-existing validators. Anyone may do this for any validator. Top-up deposits have exactly the same structure as normal deposits, except that the top-up deposit's BLS signature is not checked, and the withdrawal credentials are ignored.

The minimum top-up amount is 1 ETH. One might wish to send a top-up if a validator's effective balance has dropped below the maximum of 32 ETH. Since most rewards are proportional to effective balance, such a validator will be under-performing. For example, with a 31 ETH effective balance your expected rewards will be reduced by around 3%, and topping up to maintain a 32 ETH effective balance might be worthwhile. Not many top-ups have been performed to date, but there are a some examples.

As noted earlier, it is possible to build up a validator's stake over time, with an initial deposit that's less than 32 ETH, followed by one or more top-up deposits. The validator will become active when its effective balance reaches 32 ETH. However, if you plan to do this, watch out for a tricky edge case involving hysteresis when the final top-up is 1 ETH.

See also

Largely of historic interest now, Mikhail Kalinin's article On the way to Eth1 finality is an exemplary analysis of the deposit bridge from the Eth1 to Eth2.

The relevant spec functions and data structures for deposits are as follows.

- The deposit contract.
- Constants ETH1_FOLLOW_DISTANCE, SECONDS_PER_ETH1_BLOCK, EPOCHS_PER_ETH1_VOTING_PERIOD, and MAX DEPOSITS.
- The Eth1Data, DepositData, and Deposit containers.

- Functions, process_eth1_data(), process_deposit(), is_valid_merkle_branch(), and apply_deposit(), all part of block processing.
- Eth1 data handling in the honest validator guide.

Withdrawals

- Consensus layer withdrawals were enabled in the Capella upgrade.
- A validator must have Eth1 withdrawal credentials to benefit from withdrawals.
- A one-time update from BLS credentials to Eth1 credentials is possible.
- Withdrawals are automatic and periodic.
- Up to 16 withdrawals per block can be processed.
- A withdrawal might be partial (for active validators) or full (for exited validators).

Background

The ability to make withdrawals from the consensus layer was enabled in the Capella upgrade, the first upgrade after the Merge.

Clearly, a fully-functioning proof of stake system needs ways both to stake and to unstake. However, for the first 29 months of the beacon chain's life, only staking was possible. All stakes, and all rewards earned, were locked within the consensus layer.

To have made withdrawals available pre-Merge would have needed a bridge from the beacon chain to Ethereum's proof of work chain, perhaps via some kind of beacon chain light-client implementation on the Eth1 side. This was deemed to be a complex project that would only have delayed the Merge.

For similar reasons, we didn't enable withdrawals at the time of the Merge, either. The Merge on its own was complex and carried risk. We did what we could to simplify and de-risk it as much as we could, which included postponing withdrawals once again.

Eventually, fulfilling the core devs' soft commitment to the Ethereum community, withdrawals were successfully enabled in the first post-Merge upgrade, Capella, on April the 12th, 2023.

Two approaches were considered for enabling beacon chain Ether to be recovered on the execution chain.

The first design was for pull withdrawals. After a validator had exited, the consensus layer would create a receipt that the staker could manually submit to the execution layer as a normal Ethereum transaction in order to recover the staked Ether and rewards. In a kind of mirroring of deposits, the consensus layer would maintain a Merkle tree of withdrawal receipts, exposing its root to the execution layer so that the withdrawal receipts could be validated when submitted there. Partial withdrawals were not really addressed in that work.

The adopted design, though, was for push withdrawals, as described below. Push withdrawals happen automatically and do not require any action by the staker. This approach provides a better user experience, and required barely any increase to the beacon state size. It takes advantage of the post-Merge Engine API as a bridge between the execution and consensus layers.

Withdrawal Credentials

When the beacon chain was conceived, it was to be only the first phase (Phase 0) of the much larger Ethereum 2.0 project. It wasn't at all clear at that time what would happen to the existing Ethereum

1.0 chain, what kind of accounts would be implemented in Eth2.0, what kind of signature schemes would be used, and so on.

In view of the unknowns, we decided to implement withdrawal credentials as a commitment to being able to withdraw *somehow* in the future, even though we had little idea what that might look like. The staker would keep a BLS withdrawal key, and, via the BLS withdrawal credentials, would be able to prove ownership of the validator's balance.

The beacon chain launched with only BLS withdrawal credentials, and all the early validators used these. Eth1 withdrawal credentials were committed to in the specs in February, 2021, only three months or so into the beacon chain's life. Since no validation is done on withdrawal credentials when a deposit is made, stakers continue to be free to use whichever they prefer. At the point of the Capella upgrade, 322,491 validators (56.9%) had BLS credentials, and 244,653 (43.1%) had Eth1 credentials⁵⁰.

BLS withdrawal credentials

BLS withdrawal credentials are often called 0x00 credentials due to their prefix. You can think of them as version zero credentials. A BLS withdrawal credential is the 32-byte hash of a 48-byte BLS public key, with the first byte replaced by 0x00.

Here's validator zero's original BLS withdrawal credential. Note the initial 0x00 byte.

0x00f50428677c60f997aadeab24aabf7fceaef491c96a52b463ae91f95611cf71

The idea is that the staker has a second BLS secret key, a withdrawal key, in addition to their usual signing key. The commitment from the protocol devs was that the withdrawal key could be used in future to sign a credential change message. The BLS withdrawal credential ensures that the claimed public key on that message matches the deposit that was initially made, so only the original depositor can access the stake and the rewards.

Separating the withdrawal key from the normal signing key has a number of benefits. Primarily, it separates ownership of the stake (controlled by the withdrawal key) from management of the stake (controlled by the signing key). This has allowed "non-custodial" staking services to appear, in which the staking service uses the signing key for day-to-day operations, but they have no ownership of the stake or rewards since the individual staker retains the withdrawal key. It also allows the withdrawal key to be kept offline, in cold storage, while the signing key remains online and "hot".

For ease of recovery, the BLS withdrawal key can be generated from the same mnemonic as the signing key by using a slightly different derivation path, as described in ERC-2334. This is what the staking-deposit-cli tool does.

Eth1 withdrawal credentials

Unless you want to keep your Ether locked up on the consensus layer for some reason, everybody should now use Eth1 withdrawal credentials. These are set either when staking⁵¹, or by sending a BLS to execution change message.

An Eth1 (execution) withdrawal credential has the prefix 0×01 , followed by eleven zero bytes, followed by the 20 bytes of a normal Ethereum address. That address is where all Ether from withdrawals will be sent.

Here's validator zero's current Eth1 withdrawal credential. Note the initial 0x01 byte.

0x010000000000000000000000d369bb49efa5100fd3b86a9f828c55da04d2d50

The withdrawal address may be a normal Ethereum account (an EOA) or a smart contract. However, when it is a smart contract, no code will be executed on receiving a withdrawal payout. This differs from receiving Ether via a transfer, which can cause a fallback function to be called.

⁵⁰You can check what type of credentials your validator has via its page on the Beaconcha.in explorer. Go to the "Deposits" tab. If your credentials begin 0x00 then they are BLS, if they begin 0x01 then they are Eth1.

⁵¹Take care when using the staking-deposit-cli to make a deposit. It (silently) defaults to BLS withdrawal credentials unless you specify the --ethl_withdrawal_address command line parameter.

Credential changes

Only validators that have Eth1 withdrawal credentials are eligible for withdrawals. Validators with BLS withdrawal credentials need to send a withdrawal credential change message to update to Eth1 credentials. Until they do this, their stake and rewards remain locked on the consensus layer.

Changing withdrawal credentials is a one-time operation. Once a validator has Eth1 credentials, no further change is possible. The only way to change your withdrawal payout address once it has been set is to exit your validator and re-stake with the new credentials.

Making a credential change

A staker whose validator has BLS withdrawal credentials, who wishes to change to Eth1 credentials, must send a message to the beacon chain, signed with the validator's withdrawal key. The staking-deposit-cli and the ethdo tool are both able to generate this message. It is a straightforward process, requiring the validator's public key, the mnemonic used when staking, and the validator's existing withdrawal credentials as a checksum. It is recommended that generating the message be done offline as the BLS withdrawal key remains highly valuable to hackers until after the credential change has been completed.

Once the credential change message has been generated, it needs to be uploaded to a beacon node to be broadcast to the network. This can be done via any beacon node's REST API, or via the Beaconcha.in explorer's handy signed message submission service.

Some time after the message has been uploaded and broadcast, a block proposer should include the credential change message in a beacon block for processing by the consensus layer. Up to MAX_BLS_TO_EXECUTION_CHANGES (16) such messages can be included per block.

For reference, a BLS to Eth1 credential change message has the following contents.

class BLSToExecutionChange(Container):
 validator_index: ValidatorIndex
 from bls pubkey: BLSPubkey

to_execution_address: ExecutionAddress

Processing a credential change

Credential change messages are handled during block processing by the process_bls_to_execution_change() function.

It checks that,

- 1. the validator currently has 0x00 BLS credentials,
- 2. the hash of the public withdrawal key (generated from the secret withdrawal key) matches the withdrawal credentials created when the deposit was made, and
- 3. the signature on the message verifies against the public withdrawal key provided.

Once satisfied that all is correct, the validator's withdrawal credentials are irrevocably updated to Eth1 withdrawal credentials. The validator is now eligible for automatic push withdrawals that will be made to the to_execution_address provided in the BLSToExecutionChange data.

To reiterate, changing withdrawal credentials is a one-time process. You can only change from BLS to Eth1 credentials. It is not possible to change Eth1 credentials without exiting the validator and re-staking.

Withdrawal processing

As mentioned above, we decided to adopt a "push" mechanism for withdrawals. Push withdrawals happen automatically, with no intervention from the staker. Up to MAX_WITHDRAWALS_PER_PAYLOAD (16) consensus layer withdrawals are made per block.

Validator withdrawals are processed in a round-robin fashion. Starting from validator 0 at the Capella upgrade, with each block, the consensus layer sweeps through the validator set in validator index order until it has found 16 withdrawals to include. The next block proposer will pick up where the previous

proposer left off in the validator set and scan for 16 further withdrawals, and so on. If every validator were eligible for a withdrawal, and if the beacon chain is performing perfectly, then a full sweep of 576,000 validators would take 5 days. That is, a validator could expect to receive a partial withdrawal payout every 5 days.

Finding withdrawals

To find the withdrawals it must include, the block proposer calls the <code>get_expected_withdrawals()</code> function. This will return a list of up to <code>MAX_WITHDRAWALS_PER_PAYLOAD</code> Withdrawal objects, each containing the following information.

class Withdrawal(Container):
 index: WithdrawalIndex

validator_index: ValidatorIndex
address: ExecutionAddress

amount: Gwei

The index field is the number of previous withdrawals ever made. It is populated from state.next_withdrawal_index and increases by one for each withdrawal. It is used only for uniquely indexing withdrawals in the execution layer. The validator_index is, of course, the validator whose beacon chain balance will be decreased, and whose Eth1 withdrawal address balance (the address field here) will be increased.

The list of withdrawals is generated deterministically. The block proposer starts from the current value of state.next_withdrawal_validator_index and considers validators in turn. If a validator is eligible for a withdrawal then it is added to the list, otherwise it is skipped. When either MAX_WITHDRAWALS_PER_PAYLOAD withdrawals have been added, or MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP have been considered, the list is returned. If the end of the validator registry is hit, the search wraps around again to validator 0.

To be eligible for a withdrawal, a validator must have Eth1 withdrawal credentials set, and one of the following must also apply:

- The validator has exited, has become withdrawable, and has a non-zero balance. Such a validator is eligible for a full withdrawal.
- The validator has an effective balance of MAX_EFFECTIVE_BALANCE (32 ETH), and an actual balance higher than that. Such a validator is eligible for a partial withdrawal.

Both of these may be true at once, in which case the first takes priority and a full withdrawal will be made for the validator.

Usually, a full list of 16 withdrawals will be generated. However, the search is bounded by considering a maximum of MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP validators. If this limit is hit, fewer than 16 withdrawals will be generated.

The reason for limiting the search, rather than making a full sweep through the whole validator set, is to bound the computational load on consensus nodes. Accessing the validator registry can be quite costly; an unbounded sweep could become a performance bottleneck.

There are two scenarios in which the bound might become relevant. The first is if there were long sections of the validator registry in which no validator had upgraded to Eth1 withdrawal credentials. This was more of a concern at the point of the Capella upgrade, when all early validators necessarily had BLS withdrawal credentials. More interesting is the possibility of an inactivity leak, which occurs when the chain stops finalising in a timely way. During an inactivity leak, no validator receives attestation rewards, and many validators receive extra inactivity penalties. Very few balances will be increasing only block proposers and sync committee members, perhaps. During a prolonged inactivity leak it is possible that large sections of the validator registry would be ineligible for a withdrawal, and the bound on the withdrawals sweep would be enforced.

Performing withdrawals

The consensus layer and the execution layer must coordinate carefully in order to process a withdrawal, which makes the full round-trip a little convoluted. The steps are as follows.

- 1. The beacon block proposer assembles a list of withdrawals by calling get_expected_withdrawals() as detailed above.
- 2. The beacon block proposer sends the withdrawals list to its attached execution client via the Engine API. See prepare_execution_payload() in the Honest Validator spec. The relevant Engine API data structure is PayloadAttributesV2.
- 3. The execution client returns an execution payload that includes the list of withdrawals, along with everything else.
- 4. The block proposer incorporates the execution payload into its beacon block and broadcasts it to the network.
- 5. On receiving the block, all consensus nodes extract the withdrawals list from the execution payload and call process_withdrawals() to deduct the withdrawal amounts from the validators' balances. Each node calls get_expected_withdrawals() independently, and the beacon block is valid only if its withdrawals list matches.
- 6. The consensus node sends the execution payload to its attached execution client. The execution client will process the withdrawals alongside all the other transactions in the payload, incrementing the Eth1 withdrawal addresses as required.

The execution layer mechanics of withdrawal processing are described in EIP-4895. Withdrawal transactions are processed after all the normal transactions in the block.

As mentioned above, withdrawal transactions don't trigger smart contract processing when the Eth1 account balance is incremented. This is primarily to avoid failures (EVM transaction reversions) that would complicate the entire process. It also avoids placing an unknown load on the execution client. The benefit of this is that withdrawals are gasless and therefore free. The receiving account's balance will increase by precisely the same amount of ETH as is deducted from the validator's beacon chain balance.

Partial and full withdrawals

A validator might be eligible for a partial withdrawal or for a full withdrawal. Neither type is prioritised over the other; they both occur alongside each other as validators are considered during the withdrawals sweep. If a validator is eligible for both, a full withdrawal will be performed.

In both cases, there is no minimum withdrawal amount - it could be a single Gwei, the beacon chain's smallest unit of account. Withdrawals are not created for zero amounts.

Partial withdrawals

Partial withdrawals make up the majority of withdrawals processed. Partial withdrawals periodically skim excess balance from validators as they earn rewards.

To be eligible for a partial withdrawal, all of the following must be true. The second and third criteria are checked in the is_partially_withdrawable_validator() predicate.

- The validator has Eth1 withdrawal credentials.
- The validator's effective balance is MAX EFFECTIVE BALANCE (32 ETH).
- The validator's actual balance exceeds MAX_EFFECTIVE_BALANCE.

The amount of the partial withdrawal will be the validator's balance in excess of MAX_EFFECTIVE_BALANCE.

The condition on the validator's effective balance eliminates an edge case where a validator has an effective balance of 31 ETH, but an actual balance of over 32 ETH, which can arise due to hysteresis. If the condition on effective balance were not applied, it might become impossible for a validator ever to regain a full effective balance of 32 ETH (without a top-up deposit), due to its balance being continually skimmed.

Full withdrawals

A full withdrawal takes place after a validator has exited the validator set and subsequently become withdrawable. A validator normally becomes withdrawable about 27 hours after making its way through the exit queue, but a slashed validator will take much longer.

The precise criteria are in the is_fully_withdrawable_validator() predicate. All of the following must apply.

- The validator has Eth1 withdrawal credentials.
- The validator is withdrawable (the current epoch is greater than or equal to its withdrawable epoch).
- The validator has a non-zero balance.

The amount of the full withdrawal will be the validator's entire balance.

Note that there is no flag to indicate that a validator has been withdrawn. This in principle allows a top-up deposit to be made for a validator after a full withdrawal has occurred, in which case another full withdrawal will occur, and the top-up amount will be returned to the execution layer.

See also

The Ethereum.org pages have a section on withdrawals, and there is a separate withdrawals FAQ. They both have plenty of links to further resources.

The relevant spec functions and data structures for withdrawals are as follows.

- The constants MAX_WITHDRAWALS_PER_PAYLOAD, MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP, and MAX_EFFECTIVE BALANCE.
- next_withdrawal_index, and next_withdrawal_validator_index in the beacon state.
- The Withdrawal container, and the withdrawals list in the ExecutionPayload container.
- get_expected_withdrawals(), process_withdrawals() in block processing.
- is_fully_withdrawable_validator(), is_partially_withdrawable_validator() in predicates.
- Preparing the ExecutionPayload in the Capella honest validator guide, and PayloadAttributesV2 in the Execution API.
- EIP-4895, "Beacon chain push withdrawals as operations", covers the execution layer side.

And for credential changes.

- Withdrawal prefixes in constants.
- The BLSToExecutionChange and SignedBLSToExecutionChange containers.
- process_bls_to_execution_change() in block processing.
- The submitPoolBLSToExecutionChange method of the Beacon API.

The Incentive Layer

Carrots and Sticks and Sudden Death

Permissionless blockchains are cryptoeconomic systems: cryptography enforces correct behaviour where possible; economics incentivises correct behaviour where it cannot be enforced. The correct behaviours we're looking for roughly correspond to availability and security. We want the chain to keep making progress, and we want the chain to give reliable, non-contradictory results under all reasonable circumstances.

This chapter describes the economic tools the beacon chain uses to incentivise its participants; the cryptography side is covered elsewhere. Broadly speaking, the tools available to help us meet these goals are (1) rewards for behaviour that helps the protocol, (2) penalties for behaviour that hinders the protocol, and (3) punishments for behaviour that looks like an attack on the protocol.

One of the few attractive aspects of proof of work is the simplicity of its economic model. Miners receive block rewards for creating blocks that get included on chain, and receive fees for including transactions in their blocks. The block rewards come from newly created coins (issuance), and transaction fees are from previously issued coins. There are no explicit in-protocol penalties or punishments. Combined with the "heaviest chain" fork choice rule, this simple model has proved to be incredibly robust. Ethereum 1 added a little complexity with uncle rewards for miners and the EIP-1559 fee burning mechanism, but it remains fundamentally simple and fairly easy to reason about.

By contrast, the Ethereum 2.0 proof of stake protocol employs an array of different economic incentives. We will break things down into the following elements over the next sections.

- 1. The most fundamental economic component is the stake itself.
- 2. Within the protocol, the stake is represented in validator balances, in particular a quantity called the "effective balance" that is the actual measure of the influence a particular validator has on the protocol.
- 3. Similarly to proof of work, the protocol issues new coins to provide the incentives we are discussing. We'll look at this in the section on issuance.
- 4. An array of rewards is used to incentivise desirable behaviours such as publishing beacon blocks and timely attestations.
- 5. Penalties are used to disincentivise undesirable behaviours such as failing to make attestations, or making late or incorrect attestations.
- 6. The inactivity leak is a special regime that the beacon chain may enter in which rewards and penalties are modified to much more heavily penalise non-participation.
- 7. Slashings are punishments for breaking the protocol rules in very specific ways that look like attacks.
- 8. Finally, we close with a note on how aspects of these incentives combine to make diversity of deployment of beacon chain infrastructure the safest strategy.

Be aware that the discussion in these sections considers the consensus layer in isolation. Now that we are post-Merge, this is no longer the whole picture. In addition to protocol-generated rewards, Ethereum stakers can now profit from transaction fee tips, and MEV (maximal extractable value). In future, they might be able to profit from restaking. All of these can modify the protocol incentives. For example, a validator behaved economically rationally when it got itself slashed (at a cost of 1 ETH) to gain around \$20 million of MEV income, although it acted dishonestly by the protocol rules in doing so. The effects of these things are the subject of much discussion, development and debate, and merit an entire book to themselves. Nevertheless, for the purposes of this work, I am focusing only on the consensus layer cryptoeconomic stack.

See also

Vlad Zamfir's memoirs on the development of the Casper Protocol are not only a great read, but a good introduction to the challenges of designing a proof of stake protocol. They discuss the background to many of the design decisions that led, eventually, to the protocol we see today. Part 1, Part 2, Part 3, Part 4, Part 5.

Much of the material in the following sections is also covered in the more recent report by Umberto Natale of Chorus One, Analysing Ethereum Cryptoeconomics: the validator's perspective.

Staking

- The stake in proof of stake provides three things: an anti-Sybil mechanism, an accountability mechanism, and an incentive alignment mechanism.
- The 32 ETH stake size is a trade-off between network overhead, number of validators, and time to finality.
- Combined with the Casper FFG rules, stakes provide economic finality: a quantifiable measure of the security of the chain.

Introduction

A stake is the deposit that a full participant of the Ethereum 2 protocol must lock up. The stake is lodged permanently in the deposit contract on the Ethereum chain, and reflected in a balance in the validator's record on the beacon chain. The stake entitles a validator to propose blocks, to attest to blocks and checkpoints, and to participate in sync committees, all in return for rewards that accrue to its beacon chain balance.

In Ethereum 2 the stake has three key roles.

First, the stake is an anti-Sybil mechanism. Ethereum 2 is a permissionless system that anyone can participate in. Permissionless systems must find a way to allocate influence among their participants. There must be some cost to creating an identity in the protocol, otherwise individuals could cheaply create vast numbers of duplicate identities and overwhelm the chain. In proof of work chains a participant's influence is proportional to its hash power, a limited resource⁵². In proof of stake chains participants must stake some of the chain's coin, which is again a limited resource. The influence of each staker in the protocol is proportional to the stake that they lock up.

Second, the stake provides accountability. There is a direct cost to acting in a harmful way in Ethereum 2. Specific types of harmful behaviour can be uniquely attributed to the stakers that performed them, and their stakes can be reduced or taken away entirely in a process called slashing. This allows us to quantify the economic security of the protocol in terms of what it would cost an attacker to do something harmful.

Third, the stake aligns incentives. Stakers necessarily own some of what they are guarding, and are incentivised to guard it well.

Stake size

The size of the stake in Ethereum 2 is 32 ETH per validator.

This value is a compromise. It tries to be as small as possible to allow wide participation, while remaining large enough that we don't end up with too many validators. In short, if we reduced the stake, we would potentially be forcing stakers to run more expensive hardware on higher bandwidth networks, thus increasing the forces of centralisation.

The main practical constraint on the number of validators in a monolithic 53 L1 blockchain is the messaging overhead required to achieve finality. Like other PBFT-style consensus algorithms,

⁵²In the Bitcoin white paper, Satoshi wrote that, "Proof-of-work is essentially one-CPU-one-vote", although ASICs and mining farms have long subverted this. Proof of stake is one-stake-one-vote.

⁵³A monolithic blockchain is one in which all nodes process all information, be it transactions or consensus-related. Pretty much all blockchains to date, including Ethereum, have been monolithic. One way to escape the scalability trilemma is to go "modular".

[•] More on the general scalability trilemma: Why sharding is great by Vitalik.

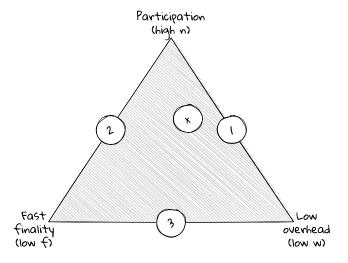
Casper FFG requires two rounds of all-to-all communication to achieve finality. That is, for all nodes to agree on a block that will never be reverted.

Following Vitalik's notation, if we can tolerate a network overhead of ω messages per second, and we want a time to finality of f, then we can have participation from at most n validators, where

$$n \leq \frac{\omega f}{2}$$

We would like to keep ω small to allow the broadest possible participation by validators, including those on slower networks. And we would like f to be as short as possible since a shorter time to finality is much more useful than a longer time⁵⁴. Taken together, these requirements imply a cap on n, the total number of validators.

This is a classic scalability trilemma. Personally, I don't find these pictures of triangles very intuitive, but they have become the canonical way to represent the trade-offs.



A version of the scalability trilemma: pick any two.

- 1. Our ideal might be to have high participation (large n) with low overhead (low ω) lots of stakers on low-spec machines –, but finality would take a long time since message exchange would be slow.
- 2. We could have very fast finality and high participation, but would need to mandate that stakers run high spec machines on high bandwidth networks in order to participate.
- 3. Or we could have fast finality on reasonably modest machines by severely limiting the number of participants.

It's not clear exactly how to place Ethereum 2 on such a diagram, but we definitely favour participation over time to finality: maybe "x" marks the spot. One complexity is that participation and overhead are not entirely independent: we could decrease the stake to encourage participation, but that would increase the hardware and networking requirements (the overhead), which will tend to reduce the number of people able or willing to participate.⁵⁵

• More on modularity: Modular Blockchains: A Deep Dive by Alec Chen of Volt Capital.

...a block chain with some finality time f has utility roughly $-\log(f)$, or in other words increasing the finality time of a block chain by a constant factor causes a constant loss of utility. The utility difference between 1 minute and 2 minute finality is the same as the utility difference between 1 hour and 2 hour finality.

He goes on to make a justification for this (p.10).

⁵⁴In an unfinished paper Vitalik attempts to quantify the "protocol utility" for different times to finality.

 $^{^{55}}$ Exercise for the reader: try placing some of the other monolithic L1 blockchains within the trade-off space.

To put this in concrete terms, the hard limit on the number of validators is the total Ether supply divided by the stake size. With a 32 ETH stake, that's about 3.6 million validators today, which is consistent with a time to finality of 768 seconds (two epochs), and a message overhead of 9375 messages per second⁵⁶. That's a substantial number of messages per second to handle. However, we don't ever expect *all* Ether to be staked, perhaps around 10-20%. In addition, due to the use of BLS aggregate signatures, messages are highly compressed to an asymptotic 1-bit per validator.

Given the capacity of current p2p networks, 32 ETH per stake is about as low as we can go while delivering finality in two epochs. Anecdotally, my staking node continually consumes about 3.5mb/s in up and down bandwidth. That's about 30% of my upstream bandwidth on residential ADSL. If the protocol were more any chatty it would rule out home staking for many.

An alternative approach might be to cap the number of validators active at any one time to put an upper bound on the number of messages exchanged. With something like that in place, we could explore reducing the stake below 32 ETH, allowing many more validators to participate, but each participating only on a part-time basis.

Note that this analysis overlooks the distinction between nodes (which actually have to handle the messages) and validators (a large number of which can be hosted by a single node). A design goal of the Ethereum 2 protocol is to minimise any economies of scale, putting the solo-staker on as equal as possible footing with staking pools. Thus, we ought to be careful to apply our analyses to the most distributed case, that of one-validator per node.

Fun fact: the original hybrid Casper FFG PoS proposal (EIP-1011) called for a minimum deposit size of 1500 ETH as the system design could handle up to around 900 active validators. While 32 ETH now represents a great deal of money for most people, decentralised staking pools that can take less than 32 ETH are now becoming available.

Economic finality

The requirement for validators to lock up stakes, and the introduction of slashing conditions allows us to quantify the security of the beacon chain in some sense.

The main attack we wish to prevent is one that rewrites the history of the chain. The cost of such an attack parameterises the security of the chain. In proof of work, this is the cost of acquiring an overwhelming (51%) of hash power for a period of time. Interestingly, a successful 51% attack in proof of work costs essentially nothing, since the attacker claims all the block rewards on the rewritten chain.

In Ethereum's proof of stake protocol we can measure security in terms of *economic finality*. That is, if an attacker wished to revert a finalised block on the chain, what would be the cost?

This turns out to be easy to quantify. To quote Vitalik's Parametrizing Casper,

State H_1 is economically finalized if enough validators sign a message attesting to H_1 , with the property that if both H_1 and a conflicting H_2 are finalized, then there is evidence that can be used to prove that at least $\frac{1}{3}$ of validators were malicious and therefore destroy their entire deposits.

Ethereum's proof of stake protocol has this property. In order to finalise a checkpoint (H_1) , two-thirds of the validators must have attested to it. To finalise a conflicting checkpoint (H_2) requires two-thirds of validators to attest to that as well. Thus, at least one-third of validators must have attested to both checkpoints. Since individual validators sign their attestations, this is both detectable and attributable: it's easy to submit the evidence on-chain that those validators contradicted themselves, and they can be punished by the protocol.

If one-third of validators were to be slashed simultaneously, they would have their entire effective balances burned (up to 32 ETH each). At that point with, say, fifteen million ETH staked in total, the cost of reverting a finalised block would be five million of the attackers' ETH being permanently burned and the attackers being expelled from the network.

It is obligatory at this point to quote (or paraphrase) Vlad Zamfir: comparing proof of stake to proof of work, "it's as though your ASIC farm burned down if you participated in a 51% attack".

⁵⁶Vitalik's estimate of 5461 is too low since he omits the factor of two in the calculation.

For more on the mechanics of economic finality, see below under Slashing, and for more on the rationale and justification, see the section on Casper FFG.

See also

- Parametrizing Casper: the decentralization/finality time/overhead tradeoff presents some early reasoning about the trade-offs for different stake sizes. Things have moved on somewhat since then, most notably with the advent of BLS aggregate signatures.
- Why 32 ETH validator sizes? from Vitalik's Serenity Design Rationale.

Vitalik's discussion document around achieving single slot finality looks at the participation/overhead/finality trade-off space from a different perspective.

Balances

- Each validator maintains an *effective balance* in addition to its actual balance.
- The validator's influence in the protocol is proportional to its effective balance, as are its rewards and penalties.
- The effective balance tracks the validator's actual balance, but is designed to change much more rarely. This is an optimisation.
- A validator's effective balance is capped at 32 ETH.

Introduction

The beacon chain maintains two separate records of each validator's balance: its actual balance and its effective balance.

A validator's actual balance is straightforward. It is the sum of any deposits made for it via the deposit contract, plus accrued beacon chain rewards, minus accrued penalties and withdrawals. The actual balance is rapidly changing, being updated at least once per epoch for all active validators, and every slot for sync committee participants. It is also fine-grained: units of the actual balance are Gwei, that is, 10^{-9} ETH.

A validator's effective balance is derived from its actual balance in such a way that it changes much more slowly. To achieve this, the units of effective balance are whole ETH (see EFFECTIVE_BALANCE_INCREMENT), and changes to the effective balance are subject to hysteresis.

Using the effective balance achieves two goals, one to do with economics, the other purely engineering.

Economic aspects of effective balance

The effective balance was first introduced to represent the "maximum balance at risk" for a validator, capped at 32 ETH. A validator's actual balance could be much higher, for example if a double deposit had been accidentally made a validator would have an actual balance of 64 ETH but an effective balance of only 32 ETH. We could envisage a protocol in which each validator has influence proportional to its uncapped actual balance, but that would complicate committee membership among other things. Instead, we cap the effective balance and require stakers to deposit for more validators if they wish to stake more.⁵⁷

The scope of effective balance quickly grew, and now it completely represents the weight of a validator in the consensus protocol.

⁵⁷There is, in fact, a proposal to increase the maximum effective balance to 2048 ETH.

All the following consensus-related quantities are proportional to the effective balance of a validator:

- the probability of being selected as the beacon block proposer;
- the validator's weight in the LMD-GHOST fork choice rule;
- the validator's weight in the justification and finalisation calculations; and
- the probability of being included in a sync committee.

Correspondingly, the following rewards, penalties, and punishments are also weighted by effective balance:

- the base reward for a validator, in terms of which the attestation rewards and penalties are calculated;
- the inactivity penalties applied to a validator as a consequence of an inactivity leak; and
- both the initial slashing penalty and the correlated slashing penalty.

However, the block proposer reward is not scaled in proportion to the proposer's effective balance. Since a validator's probability of being selected to propose is proportional to its effective balance, the reward scaling with effective balance is already taken care of. For the same reason sync committee rewards are not proportional to the participants' effective balances either.

Engineering aspects of effective balance

We could achieve all the above simply by using validators' actual balances as their weights, capped at 32 ETH. However, we can gain significant performance benefits by basing everything on effective balances instead.

For one thing, effective balances are updated only once per epoch, which means that we need only calculate things like the base reward per increment once then cache the result for the whole epoch, irrespective of any changes in actual balances.

But the main feature of effective balances is that they are designed to change much more rarely than that. This is achieved by making them very granular, and by applying hysteresis to any updates.

One of the big performance challenges in calculating the beacon chain state transition is generating the hash tree root of the entire state. The Merkleization process allows parts of the state that have not been changed to be cached, providing a significant performance boost.

The list of validator records in the state is a large data structure. Were we to store the validators' actual balances within those records they would be frequently changing, and the whole data structure would need to be re-hashed at least once per epoch.

The first approach to addressing this simply moved the validators' balances out of the validator records into a dedicated list in the state. This reduces the amount of re-hashing required as the whole validator list does not need to be re-hashed when only the validators' balances change.

However, that leads to a performance issue elsewhere. Light clients needing information on validators' balances would now need to acquire data from two different parts of the state – both the validator record and the validator balance list. This requires two Merkle proofs rather than one, significantly increasing their bandwidth costs.

A way round this is to store a slowly changing version of the balances in the validators' records – meaning that they need to be re-hashed infrequently – and to store the fast-changing actual balances in a separate list, a much smaller structure to re-hash.

From the notes for an early attempt at a kind of effective balance implementation:

[Effective balances are an] "approximate balance" that can be used by light clients in the validator_registry, reducing the number of Merkle branches per validator they need to download from 3 to 2 (actually often from ~2.01 to ~1.01, because when fetching a committee the Merkle branches in active_index_roots are mostly shared), achieving a very significant decrease in light client bandwidth costs

The point is that light clients will not need to access the list of actual balances that is stored separately in state, only the validator records they were downloading anyway.

In summary, adding effective balances to validators' records allows us to achieve two performance goals simultaneously: avoiding the workload of frequently re-hashing the validator list in the state while not increasing the workload of light clients.

Increments

Although effective balances are denominated in Gwei they can only be whole multiples of EFFECTIVE_BALANCE_INCREMENT, which is 1 ETH (10^9 Gwei) . Actual balances can be any number of Gwei.

This multiple is known in the spec as an "increment" and shows up in places like calculating the base reward, and other rewards and penalties calculations. Being a handy 1 ETH, it's easy to mentally substitute "Ether" for "increment" to gain some intuition.

It would probably be cleaner to store effective balance in terms of increments instead of Gwei. It would certainly reduce the amount of dividing and multiplying by EFFECTIVE_BALANCE_INCREMENT that goes on, and the associated danger of arithmetic overflows. But the current version evolved over time, and it would be intrusive and risky to go back and change things now.

Hysteresis

Effective balances are guaranteed to vary much more slowly than actual balances by adding hysteresis to their calculation.

In our context, hysteresis means that if the effective balance is 31 ETH, the actual balance must rise to 32.25 ETH to trigger an effective balance update to 32 ETH. Similarly, if the effective balance is 31 ETH, then the actual balance must fall to 30.75 ETH to trigger an effective balance update to 30 ETH.

The following chart illustrates the behaviour.

- The actual balance and the effective balance both start at 32 ETH.
- Initially the actual balance rises. Effective balance is capped at 32 ETH, so it does not get updated.
- Only when the actual balance falls below 31.75 ETH does the effective balance get reduced to 31 ETH.
- Although the actual balance rises and oscillates around 32 ETH, no effective balance update is triggered, and it remains at 31 ETH.
- Eventually the actual balance rises above 32.25 ETH, and the effective balance is updated to 32 ETH.
- Despite the actual balance falling again, it does not fall below 31.75 ETH, so the effective balance remains at 32 ETH.

The hysteresis levels are controlled by the hysteresis parameters in the spec:

Name	Value
HYSTERESIS_QUOTIENT	uint64(4)
HYSTERESIS_DOWNWARD_MULTIPLIER	uint64(1)
HYSTERESIS_UPWARD_MULTIPLIER	uint64(5)

These are applied at the end of each epoch during effective balance updates. Every validator in the state (whether active or not) has its effective balance updated as follows:

- If actual balance is less than effective balance minus 0.25 (= HYSTERESIS_DOWNWARD_MULTIPLIER / HYSTERESIS QUOTIENT) increments (ETH), then reduce the effective balance by an increment.
- If actual balance is more than effective balance plus 1.25 (= HYSTERESIS_UPWARD_MULTIPLIER / HYSTERESIS_QUOTIENT) increments (ETH), then increase the effective balance by an increment.

The effect of the hysteresis is that the effective balance cannot change more often than it takes for a validator's actual balance to change by 0.5 ETH, which would normally take several weeks or months.

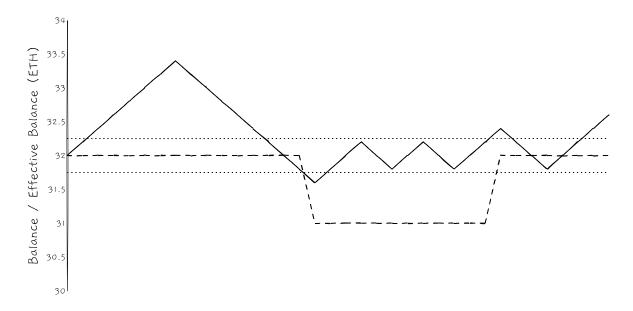


Illustration of the relationship between the actual balance (solid line) and the effective balance (dashed line) of a validator. The dotted lines are the thresholds at which the effective balance gets updated - the hysteresis.

An edge case

The hysteresis design gives rise to an interesting edge case in deposit processing. The deposit contract allows a staker to deposit any amount greater than or equal to 1 ETH; a deposit doesn't have to be the full 32 ETH. This allows a stake to be accumulated from multiple deposits. For example, a deposit of 24 ETH followed by a separate deposit of 8 ETH makes up a full stake and will activate the validator once the second deposit has been processed.

The edge case occurs when the final deposit for a validator takes its actual balance to 32 ETH or more but, due to the hysteresis, is not sufficient to update its effective balance to 32 ETH. For example, after a deposit of 31 ETH the validator's actual and effective balances will both be 31 ETH. A further deposit of 1 ETH will take the validator's actual balance to 32 ETH – which makes it technically eligible for activation – but will leave its effective balance at 31 ETH due to the hysteresis calculation. Thus, it will not be activated.

Validator 418408 is an example of this occurring on mainnet. The penultimate deposit of 1 ETH took the validator's total balance to 32 ETH, but it was not activated until a further deposit of 1 ETH was made in order to force an update to effective balance.

A historical note

The initial implementation of hysteresis effectively had QUOTIENT = 2, DOWNWARD_MULTIPLIER = 0, and UPWARD_MULTIPLIER = 3. This meant that a validator starting with an actual balance of 32 ETH, but suffering a minor initial outage, would immediately drop to 31 ETH effective balance. To get back to 32 ETH effective balance it would need to achieve a 32.5 ETH actual balance, and meanwhile the validator's rewards would be 3.1% lower due to the reduced effective balance. This seemed unfair, and incentivised stakers to "over-deposit" Ether to avoid the risk of an initial effective balance drop, hence the change to adopt the current parameters.

See also

From the spec:

• The presets that constrain the effective balance, MAX_EFFECTIVE_BALANCE and EFFECTIVE_BALANCE_INCREMENT.

- The parameters that control the hysteresis.
- The function process_effective_balance_updates() for the actual calculation and application of hysteresis.
- Validator objects store the effective balances. The registry in the beacon state contains the list of validators alongside a separate list of the actual balances.

Issuance

- Issuance is the amount of new Ether created by the protocol in order to incentivise its participants.
- An ideally running beacon chain issues a set amount of Ether per epoch, which is a multiple of the base reward per increment.
- Total issuance is proportional to the square root of the number of validators. This is not a completely arbitrary choice.

Introduction

There are three views we can take of the rewards given to validators to incentivise their correct participation in the protocol.

First, there is "issuance", which is the overall amount of new Ether generated by the protocol to pay rewards. Second there is the expected reward a validator might earn over the long run. And, third, there is the actual reward that any particular validator earns.

In this section we will look at issuance, and in the next we'll look at rewards. There is a strong relationship between these, though, so the separation is not totally clean.

First we must define the fundamental unit of reward, which is the "base reward per increment".

The base reward per increment

We will call the base reward per increment b for brevity. An increment is one unit of effective balance, which is 1 ETH (EFFECTIVE_BALANCE_INCREMENT), so active validators have up to 32 increments.

The BASE_REWARD_FACTOR is the big knob that we could turn if we wished to change the issuance rate of Ether on the beacon chain. So far it's always been set at 64 which results in the issuance graph we see below. This seems to be working very well and there are no plans to change it.

Rewards come from issuance

Issuance is the amount of new Ether created by the protocol in order to incentivise its participants. The net issuance, after accounting for penalties, burned transaction fees and so forth is sometimes referred to as inflation, or supply growth.

Pre-Merge, the Eth1 chain issued new Ether in the form of block and uncle rewards. Since the London upgrade this issuance has been offset in part, or even at times exceeded, by the burning of transaction base fees due to EIP-1559.

Post-Merge, there are no longer any block or uncle rewards issued on the Eth1 chain. But the base fee burn remains. It is possible for the net issuance to become negative – such that more Ether is destroyed

than created 58 – at least in the short to medium term. In the longer term, Anders Elowsson argues that there will be a circulating supply equilibrium arising from Ether issuance by proof of stake and Ether destruction due to EIP-1559.

In the following we will be assuming that the beacon chain is running optimally, that is, with all validators performing their duties perfectly. In reality this is impossible to achieve on a permissionless, globally distributed, peer-to-peer network, although the beacon chain has been performing within a few percent of optimally for most of its history. Actual validator rewards and net issuance will certainly be a little or a lot lower, depending on participation rates in the network.

Overall issuance

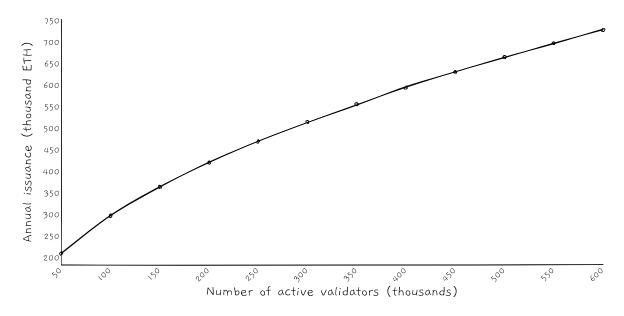
Under the ideal conditions we are assuming, the beacon chain is designed to issue a total of exactly Tb Gwei in rewards per epoch. Here, T is the total number of increments held by active validators, or in other words the total of all their effective balances in Ether. This is the maximum issuance – the maximum amount of new Ether – that the beacon chain can generate. If all N validators have the maximum 32 ETH effective balance, then this works out to be 32Nb Gwei per epoch in total.

With $365.25 \times 225 = 82181.25$ epochs per year, and BASE_REWARD_FACTOR = 64,

Max issuance per year = 82181.25 ×
$$\frac{32 \times 64 \times N}{\sqrt{32 \times 10^9 \times N}}$$
ETH = 940.8659 \sqrt{N}

With 500,000 validators this equates to 665,292 ETH per year, plus change. For comparison, under proof of work, Ethereum's block and uncle rewards amounted to almost five million ETH per year.

We can graph the maximum issuance as a function of the number of validators. It's just a scaled square root curve.



Maximum annual protocol issuance on the beacon chain as a function of the number of active validators.

Validator rewards

The goal is to distribute these rewards evenly among validators (continuing to assume that things are running optimally), so that, on a long term average, each validator i earns $n_i b$ Gwei per epoch, where

⁵⁸You can see Ethereum's current issuance and play with various scenarios at ultrasound.money.

 n_i is the number of increments it possesses, equivalently its effective balance in Ether. In these terms $T = \sum_{i=0}^{N-1} n_i$.

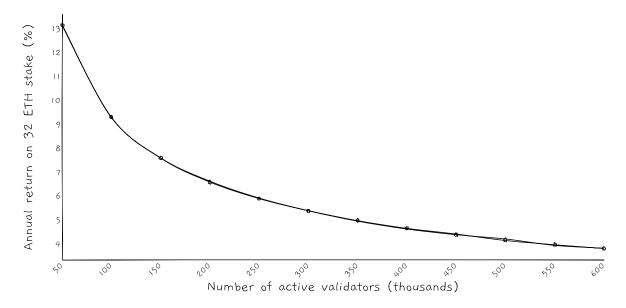
Given this, a well-performing validator with a 32 ETH effective balance can expect to earn a long-term average of 32b Gwei per epoch. Of course, b changes over time as the total active balance changes, but in the absence of a mass slashing event that change will be slow.

Similarly to the issuance calculation, we can calculate the expected annual percentage reward for a validator due to participating in the beacon chain protocol:

$$\begin{split} \text{APR} &= 100 \times 82181.25 \times \frac{64}{\sqrt{32 \times 10^9 \times N}} \% \\ &= \frac{2940.21}{\sqrt{N}} \% \end{split}$$

For example, with 500,000 validators participating, this amounts to an expected return of 4.16% on a validator's effective balance.

Graphing this give us an inverse square root curve.



The expected annual percentage rewards for stakers as a function of the number of active validators.

Inverse square root scaling

The choice to scale the per-validator expected reward with $\frac{1}{\sqrt{N}}$ is not obvious, and we can imagine different scenarios.

If we model the per-validator reward as $r \propto N^{-p}$, then some options are as follows.

- 1. p = 0: each validator earns a constant return regardless of the total number of validators. Issuance is proportional to N.
- 2. $p=\frac{1}{2}$: issuance scales like \sqrt{N} , the formula we are using.
- 3. p = 1: each validator's expected reward is inversely proportional to the total number of validators. Issuance is independent of the total number of validators.

Adopting a concave function is attractive as it allows an equilibrium number of validators to be discovered without constantly fiddling with parameters. Ideally, if more validators join, we want the per-validator reward to decrease to disincentivise further joiners; if validators drop out we want the per-validator reward

to increase to encourage new joiners. Eventually, an equilibrium number of validators will be found that balances the staking reward against the perceived risk and opportunity cost of staking. Assuming that the protocol is not overly sensitive to the total number of validators, this seems to be a nice feature to have.

That would rule out the first, p = 0, option. The risk with p = 0 is that, if the reward rate is set lower than the perceived risk, then all rational validators will exit. If we set it too high, then we end up paying for more security than we need (too many over-incentivised validators). Frequent manual tuning via hard-forks could be required to adjust the rate.

The arguments for selecting $p=\frac{1}{2}$ over p=1 are quite subtle and relate to discouragement attacks. With $p\neq 0$, a set of validators may act against other validators by censoring them, or performing other types of denial of service, in order to persuade them to exit the system, thus increasing the rewards for themselves. Subject to various assumptions and models, we find that we require $p\leq \frac{1}{2}$ for certain kinds of attack to be profitable. Essentially, we don't want to increase rewards too much for validators that succeed in making other validators exit the beacon chain.

Note that since the Merge, validators' income can include a significant component from transaction priority fees and MEV. This has the effect of pushing p closer to 1, and much of the reasoning above becomes moot. Discouragement attacks in this regime are an unsolved problem.

See also

For more background to the $\frac{1}{\sqrt{N}}$ reward curve, see

- Casper: The Fixed Income Approach,
- Vitalik's Serenity Design Rationale, and
- the Discouragement Attacks paper.

Anders Elowsson's work on Ethereum's circulating supply equilibrium and minimum viable issuance takes a deeper look at the relationship between staking issuance and total Ether supply. See his post and comments on Ethresear.ch, and ETHconomics presentation at Devconnect 2022.

Rewards

- Validators receive rewards for making attestations according to their view of the chain, proposing blocks, and participating in sync committees in varying proportions.
- Votes that make up attestations must be both correct and timely in order to be rewarded.
- The proposer's reward is a fixed proportion, $\frac{1}{7}$, of the total reward for all the duties it includes in its block.
- A validator's expected long-term reward is *nb* per epoch (number of increments times the base reward per increment), but there is significant variance due to the randomness of proposer and sync committee assignments.
- Rewards are scaled both with a validator's effective balance and with the total participation rate of the validator set.
- The need to defend against discouragement attacks has shaped various aspects of the protocol.

Introduction

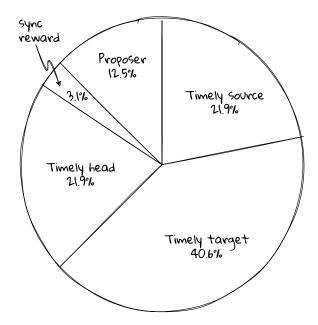
In this section we will consider only rewards. We'll cover penalties in the next section.

The beacon chain protocol incentivises each validator to behave well by providing rewards for three activities as follows.

- 1. Attesting to its view of the chain as part of the consensus protocol:
 - voting for a source checkpoint for Casper FFG;
 - voting for a target checkpoint for Casper FFG; and
 - voting for a chain head block for LMD-GHOST.
- 2. Proposing beacon chain blocks.
- 3. Signing off on blocks in the sync committees that support light clients.

The first of these, making attestations, happens regularly every epoch and accounts for the majority a validator's total expected reward.

However, validators are selected at random to propose blocks or participate in sync committees, so there is a natural variance to the latter two rewards. Over the long run, the expected proportion of rewards earned for each activity breaks down as per the following chart.



The proportion of a validator's total reward derived from each activity.

These proportions are set by the incentivisation weights in the spec. For convenience, I've assigned a symbol to each weight in the last column.

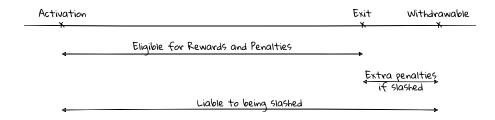
Name	Value	Percentage	Symbol
TIMELY_SOURCE_WEIGHT	uint64(14)	21.9%	W_s
TIMELY_TARGET_WEIGHT	uint64(26)	40.6%	W_t
TIMELY_HEAD_WEIGHT	uint64(14)	21.9%	W_h
SYNC_REWARD_WEIGHT	uint64(2)	3.1%	W_y
PROPOSER_WEIGHT	uint64(8)	12.5%	W_p
WEIGHT_DENOMINATOR	uint64(64)	100%	W_{Σ}

One further reward is available to block proposers for reporting violations of the slashing rules, but this ought to be very rare, and we will ignore it in this section (see Slashing for more on this).

Rewards are newly created Ether that is simply added to validators' balances on the beacon chain.

Eligibility for rewards

There are three relevant milestones in a validator's lifecycle: its activation epoch, its exit epoch, and its withdrawable epoch. Eligibility for rewards, penalties and slashing vary based on these.



Timeline of the eligibility of validators for rewards

Validators may receive rewards only between their activation and exit epochs. Note that, after submitting a voluntary exit, there may be a delay while the validator moves through the exit queue until its exit epoch is passed. The validator is expected to participate as usual during this period.

Similarly, validators receive penalties only between their activation and exit epochs. The exception to this is slashed validators. As a special case, slashed validators continue to receive penalties until they reach their withdrawable epoch, which may be long after their exit epoch.

All unslashed validators that are between their activation epoch and their withdrawable epoch are liable to being slashed.

Rewards scale with effective balance

As described earlier, all rewards are scaled in proportion to a validator's effective balance. This reflects the fact that a validator's influence (weight) in the protocol is proportional to its effective balance.

If a validator has n increments (that is, an effective balance of $n \times \text{EFFECTIVE_BALANCE_INCREMENT}$, or n ETH in other words) then its expected⁵⁹ income per epoch is nb, where b is the base reward per increment.

For the regular attestations that occur every epoch, this is achieved explicitly by multiplying the base reward by the number of increments in get_base_reward().

For the random elements – block proposals and sync committee participation – the scaling is achieved implicitly by modifying the probability that a validator is selected for duty to be proportional to $\frac{n}{T}$, where T is the total number of increments of the active validator set. So, if your effective balance is 24 ETH, then you are 25% less likely to be selected to propose a block or join a sync committee than a validator with 32 ETH. See compute_proposer_index() and get_next_sync_committee_indices() for the details.

Attestation rewards

The largest part, 84.4%, of validators' rewards come from making attestations. Although committee and slot assignments for attesting are randomised, every active validator will be selected to make exactly one attestation each epoch.

Attestations receive rewards only if they are included in beacon chain blocks. An attestation contains three votes. Each vote is eligible for a reward subject to conditions.

 $^{^{59}}$ I'm using the word "expected" in its technical sense here. Due to randomness there is a chance that some validators earn less and a chance that some validators earn more. The averagely lucky validator can expect their rewards to average out to nb Gwei per epoch over the long term.

Validity	Timeliness	Reward
Correct source	Within 5 slots	$\frac{W_s}{W_\Sigma} nb$
Correct source and target	Within 32 slots	$rac{W_t^2}{W_\Sigma}nb$
Correct source, target and head	Within 1 slot	$rac{W_s}{W_{\Sigma}} nb \ rac{W_t}{W_{\Sigma}} nb \ rac{W_h}{W_{\Sigma}} nb \ rac{W_h}{W_{\Sigma}} nb$

These are cumulative, so the maximum attestation reward per epoch (for getting all three votes correct and getting the attestation included the next block) is $\frac{W_s + W_t + W_h}{W_{\Sigma}} nb$, or 0.84375 nb.

The full matrix of possible weights for an attestation reward is as follows. In each case we need to multiply by $\frac{nb}{W_{\Sigma}}$ to get the actual reward.

Timeliness	1 slot	<=5 slots	<=32 slots	> 32 Slots (missing)
Wrong source	0	0	0	0
Correct source	W_s	W_s	0	0
Correct source and target	$W_s + W_t$	$W_s + W_t$	W_t	0
Correct source, target and head	$W_s + W_t + W_h$	$W_s + W_t$	W_t	0

But this is not the whole picture: we will also need to account for penalties for incorrect or late attestations.

The maximum total issuance per epoch across all validators is

$$I_A = \frac{W_s + W_t + W_h}{W_\Sigma} Tb$$

where, once again, T is the total number of increments of active validators (the sum of their effective balances in ETH terms).

Correctness

"Correct" in the above means that the attestation agrees with the view of the blockchain that the current block proposer has. If the attesting validator votes for different checkpoints or head blocks then it is on a different fork and that vote is not useful to us. For instance, if the source checkpoint vote is different from what we as proposer think it ought to be, then our view of the chain's history is fundamentally different from the attester's, and so we must ignore their attestation. The attestation will instead receive rewards in blocks on the other fork, and eventually one fork or the other fork will win. To disincentivise attacks it is important that only participants in the winning chain receive rewards.

Timeliness

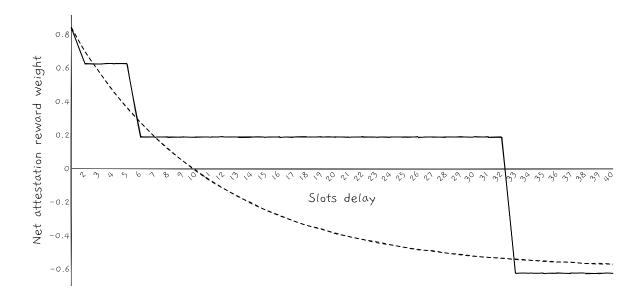
One of the changes brought in with Altair was a tightening of the timeliness requirements for attestations. Previously, there were rewards for correctness and a separate reward for timely inclusion that declined as $\frac{1}{d}$, where d was the inclusion distance in slots, up to a maximum of 32 slots. This led to oddities, like it being worth waiting slightly longer to make sure to get the head vote correct since that was worth more than any loss due to lateness of inclusion, even though a late head vote is pretty much useless.

The new timeliness reward better reflect the relative importance of the votes. A head vote that is older than one slot is not useful, so it gets no reward.

Target votes are always useful, but we only want to track attestations pertaining to the current and previous epochs, so we ignore them if they are older than 32 slots. The number 32 was chosen for

reasons of fairness: whichever slot in an epoch validators attest, their attestations are valid for the same length of time. 60

The choice of distance for including the source vote is interesting. It is chosen to be $\lfloor \sqrt{\mathsf{SLOTS_PER_EPOCH}} \rfloor = \lfloor \sqrt{32} \rfloor = 5$, which is the geometric mean of 1 and 32, the head and target values. It's a somewhat arbitrary choice, but is intended to put a fully correct attestation on an exponentially decreasing curve with respect to timeliness: each step down in (net) reward happens after an exponentially increasing number of slots.⁶¹



It is plausible that setting the inclusion distance for correct source to 5 gives a kind of exponential reduction in reward with time. This graph shows the net reward (reward + penalty) for a completely correct attestation as it gets older plotted against an exponential curve for comparison.

Remarks

Note that the attester does not have full control over whether it receives rewards or not. An attester may behave perfectly, but if the next block is skipped because the proposer is offline, then it will not receive the correct head block reward. Or if the next proposer happens to be on a minority fork, the attester will again forgo rewards. Or if the next proposer's block is late and gets orphaned - subsequent proposers are supposed to pick up the orphaned attestations, but there can be considerable delays if block space is tight. There are countless failure modes outside the attester's control.

It often perplexes stakers when, to all intents and purposes, their validators seem to be working perfectly, yet they still miss out on rewards or receive penalties. But this is the nature of permissionless, global, peer-to-peer networks. It is a testament to the quality of the protocol and the various client implementations that missed rewards have been surprisingly rare on the beacon chain so far.

vbuterin:

The rationale for the number 5 is just that 5 is geometrically halfway in between 1 and 32 And so we get the closest that makes sense to a smooth curve in terms of rewarding earlier inclusion

ah I mean on an exponential curve, not quadratic

To me exponential feels more logical

What's a bigger improvement in quality, 4 slot delay vs 6 slot delay, or 20 slot delay vs 23 slot delay?

⁶⁰EIP-7045 proposes to change this in the Deneb upgrade to accept and reward target votes for the whole of the current and previous epochs. Danny Ryan made an insightful presentation on the reasons for changing this, and a defence of why the changes remain fair to validators, in the PEEPanEIP 114 session.

 $^{^{61}\}mathrm{This}$ is taken from a conversation on the Ethereum R&D Discord server:

Proposer rewards for attestations

If the attestations in a block are worth a total of R in rewards to the attesters, then the proposer that includes the attestations in a block receives a reward of

$$R_{A_P} = \frac{W_p}{W_\Sigma - W_p} R$$

Thus, over an epoch, the maximum total issuance due to proposer rewards in respect of attestations is

$$I_{A_P} = \frac{W_p}{W_{\Sigma} - W_p} I_A$$

with I_A being the maximum issuance to attesters per epoch, as above.

Thus, a proposer is strongly incentivised to include high value attestations, which basically means including them quickly, and including well-packed, as correct as possible aggregates.

Sync committee rewards

Once every 256 epochs (27.3 hours), 512 validators are selected to participate in the sync committee. For any given validator this will happen rarely; with 500,000 validators, the expected interval between being chosen for sync committee duty is around 37 months. However, during the 27-hour period of participation the rewards are relatively very large.

Sync committee participants receive a reward for every slot that they correctly perform their duties. With 512 members in the committee, and 32 slots per epoch, the reward per validator per slot for correct participation is

$$R_Y = \frac{W_y}{32 \times 512 \times W_{\Sigma}} Tb$$

The T here is the total increments of the whole active validator set, so this is a large number. The per-epoch per-validator reward is 32 times this.

The maximum issuance per epoch to sync committee members in respect of their sync contributions is then

$$I_Y = \frac{W_y}{W_{\Sigma}} Tb$$

Proposer rewards for sync committees

As with attestations, the block proposer that includes the sync committee's output receives a reward proportional to the reward of the whole committee:

$$R_{Y_P} = 512 \frac{W_p}{W_{\Sigma} - W_p} R_Y$$

So the maximum issuance per epoch to proposers for including sync committee contributions is

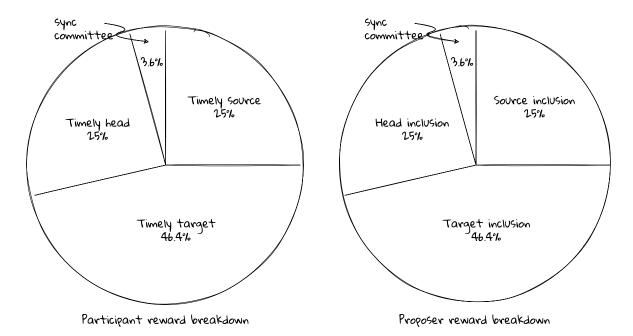
$$I_{Y_P} = \frac{W_p}{W_\Sigma - W_p} I_Y$$

Remarks on proposer rewards

You'll note that, for both attestations and sync committees, the proposer reward for including them in a block is a fixed fraction of the validator reward. If R is the validator reward for a duty, then the proposer reward is $\frac{W_p}{W_{\Sigma}-W_p}R$. In Vitalik's words, "The proposer reward for a duty is the attester reward for that duty, multiplied by the proposer reward as a fraction of everything but the proposer reward" (emphasis his).

This factor works out to be $\frac{8}{56} = \frac{1}{7}$ which means that $\frac{7}{8}$ of rewards go to validators performing duties and $\frac{1}{8}$ to the proposers including the evidence in blocks.

In the following charts, I have separated out the validator rewards from the proposer rewards, and we can see that they have exactly the same division among the duties. The chart on the right should probably be one seventh of the size of the one on the left for true accuracy.



On the left, the breakdown of expected rewards for validators for performing duties. On the right, the breakdown of rewards for proposers for including evidence of those duties.

This equivalence ensures that the interests of attesters and proposers are aligned.

Total issuance

To check that the calculations above are consistent with our claim that the maximum issuance by the beacon chain per epoch is Tb Gwei, let us sum up the issuance due to the four rewards: attester rewards, proposer rewards in respect of attestation inclusion, sync committee rewards, and proposer rewards in respect of sync committee inclusion. The total maximum issuance per epoch is

$$\begin{split} I &= I_A + I_{A_P} + I_Y + I_{Y_P} \\ &= \left(1 + \frac{W_p}{W_\Sigma - W_p}\right) (I_A + I_Y) \\ &= \left(1 + \frac{W_p}{W_\Sigma - W_p}\right) \left(\frac{W_s + W_t + W_h + W_y}{W_\Sigma}\right) Tb \\ &= \left(\frac{W_\Sigma}{W_\Sigma - W_p}\right) \left(\frac{W_\Sigma - W_p}{W_\Sigma}\right) Tb \\ &= Tb \end{split}$$

as expected.

Rewards in numbers

The following calculations are based on 500 thousand active validators, all performing perfectly and all with 32 ETH of effective balance.

• Base reward per increment

$$-b = \frac{1,000,000,000 \times 64}{\sqrt{32,000,000,000 \times 500,000}} = 505$$
 Gwei

• Value of a single attestation

–
$$R_A = \frac{14 + 26 + 14}{64} 32b = 13{,}635$$
 Gwei

• Value of a single sync committee contribution

$$-R_Y = \frac{2}{32 \times 512 \times 64} 500,000 \times 32b = 15,411$$
 Gwei

• Value of a block proposal due to attestations

–
$$R_{A_P} = \frac{500,000}{32} \frac{8}{64-8} R_A = 30,\!435,\!267$$
 Gwei

- Note: this can actually be higher if the chain is not performing perfectly, as after a skip slot
 the proposer can include high value attestations from the missed slot.
- Value of a block proposal due to sync committee contributions

–
$$R_{Y_{\rm p}} = 512 \frac{8}{64-8} R_Y = 1,127,204$$
 Gwei

Putting it all together, the total available reward per epoch across all validators is $500,000R_A+32(512R_Y+R_{A_P}+R_{Y_P})=8,080,000,000$ Gwei (to 5 significant figures)

Finally, as a check-sum, $Tb = 500,000 \times 32b = 8,080,000,000$ Gwei = 8.080 ETH issued per epoch.

Individual validator rewards vary

Actual individual validator returns, even on an optimally running beacon chain, will vary above and below the expected amounts, since block proposals and sync committee duties are assigned randomly. This leads to variance in the rewards, with some validators earning more and some earning less. Nonetheless, an average validator over a long period can expect to earn a return in line with nb per epoch.

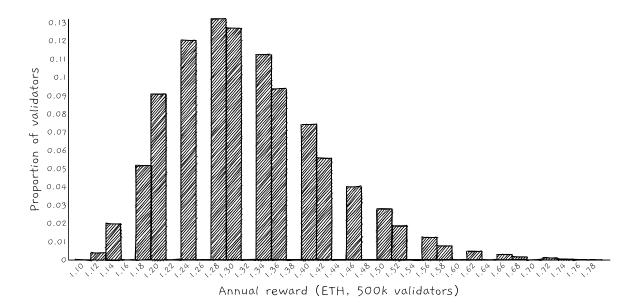
The following chart shows the expected distribution of annual rewards for 500,000 validators, all participating perfectly, each with 32 ETH of effective balance. The mean reward is 1.3302 ETH/year (the 4.16% number from earlier), and the median 1.3123 ETH/year, but there is a large standard deviation of 0.1037 due to the randomness of being selected to propose blocks or participate in sync committees. In fact, ten percent of validators will earn less than 1.2175 ETH in rewards over the year, and 10% more than 1.4704 ETH, due solely to randomness in assigning duties.

A few remarks on this.

First, the Altair upgrade did not change the expected reward per validator, but it did change the variance considerably. This is due to an increase in the block reward of a factor of four and the introduction of sync committees, with a corresponding reduction in attestation rewards. Since block proposals and sync committee participation are randomly assigned, while attestation rewards are steady, Altair greatly increased the variance in actual rewards. For an analysis of the change, see Pintail's article.

Second, there are further sources of variation that the above analysis doesn't account for. For example, if my validator proposes a block right after a skipped slot, in which there was no block, then my block proposal could be worth up to 71.4% more than a normal block proposal. This is because I get to include attestations from the skipped slot as well as from my own slot, and benefit from the extra source and target votes (but not the extra head votes, which will be too late, or the extra sync committee inclusion).

Third (and most significantly), post-Merge, validators additionally receive the transaction priority fees from execution payloads, and potentially MEV-related income as well. These can substantially increase the percentage earnings and variance in earnings for stakers, but will not affect overall issuance on the beacon chain since they come from recycled Ether rather than new issuance.



Distribution of annual beacon chain rewards for 500,000 perfectly performing validators with 32 ETH staked. The variance comes from the probabilities of different numbers block proposals or sync committee assignments. Some values are not attainable in this idealised model.

Rewards scale with participation

One surprising aspect of attestation rewards not so far mentioned is that they are scaled in proportion to participation. That is, for each duty (source, target, head vote) the attester's reward is scaled by the proportion of the total stake that made the same vote.

For example, if I made a correct head vote, and validators with 75% of the total effective balance increments made the same head vote, then I would receive $0.75 \times \frac{W_h}{W_{\Sigma}} nb$ reward for that vote.

A hand-wavy reason for this is that this scaling makes it to my advantage to help other validators get their attestations included. Several aspects of the protocol are not explicitly incentivised yet are somewhat expensive, such as forwarding gossip messages and attestation aggregation duty. This scaling provides me with an implicit reward for helping out other validators by providing these services: if they perform better, then I perform better.

For a more quantitative analysis, see on discouragement attacks below.

One interesting side effect of this is that, if participation drops by 10% (due to 10% of validators being offline, say), then total issuance of rewards due to attestations will fall by 19%, in addition to a further reduction from penalties.

We can calculate the participation rate at which net issuance due to attestations turns negative. With a participation rate p, the reward for a fully correct attestation is 0.844nbp, and the penalty for a missed attestation is 0.625Tb. This gives us a net issuance of $p^2(0.844Tb) - (1-p)(0.625Tb)$. The positive root of this is p = 56.7%. But since this is below the 2/3 participation rate for finalisation, the inactivity leak will kick-in before we reach this level and completely change the reward and penalty profile, so the calculation is of theoretical interest only.

Note that the proposer reward is not scaled like this – proposers are already well incentivised to include all relevant attestations – and neither are sync committee rewards. Penalties do not scale with participation, either.

Discouragement attacks

Quoting from Vitalik's Discouragement Attacks paper,

A discouragement attack consists of an attacker acting maliciously inside a consensus mechanism in order to reduce other validators' revenue, even at some cost to themselves, in order to encourage the victims to drop out of the mechanism.

Attackers might do this to gain more rewards with fewer participants in the system. Or they might do it as preparation for an attack on the chain: by reducing the number of validators they decrease their own cost of attack.

The paper goes into some quantitative analysis of different kinds of discouragement attacks. I would encourage you to read it and think through these things. As per the conclusion:

In general, this is still an active area of research, and more research on counter-strategies is desired.

Some parts of the beacon chain design that have already been influenced by a desire to avoid discouragement attacks are:

- the inverse square root scaling of validator rewards;
- the scaling of rewards with participation;
- the zeroing of attestation rewards during an inactivity leak; and
- rate limiting of validator exits, which means that an attacker needs to sustain an attack for longer, at greater cost to achieve the same ends.

See also

The detailed rewards calculations are defined in the spec in these functions:

- Validator rewards for attestations are calculated in get_flag_index_deltas() as part of epoch processing.
- Proposer rewards for attestations are calculated in process_attestation() as part of block processing.
- Both validator and proposer rewards for sync committee participation are calculated in process_sync_aggregate() as part of block processing.

The discussion of the variance of rewards is based on Pintail's analysis of Altair. The code I used to generate the stats and the chart are based on the code in that article.

Discouragement attacks are analysed in a paper by Vitalik.

Penalties

- Validators that do not fulfil their assigned duties are penalised by losing small amounts of stake.
- Receiving a penalty is not the same as being slashed!
- Break-even uptime for a validator is around 43%.

Introduction

Incentivisation of validators on the beacon chain is a combination of carrot and stick. Validators are rewarded for contributing to the chain's security, and penalised for failing to contribute. As we shall see, penalties are quite mild. Nonetheless, they provide good motivation for stakers to ensure that their validator deployments are running well.

It's common to hear of the penalties for being offline being referred to as "getting slashed". This is incorrect. Being slashed is a severe punishment for very specific misbehaviours, and results in the validator being ejected from the protocol in addition to some or all of its stake being removed.

Penalties are subtracted from validators' balances on the beacon chain and effectively burned, so they reduce the net issuance of the beacon chain.

Attestation penalties

Attestations are penalised for being missing, late, or incorrect. We'll lump these together as "missed" for conciseness.

Attesters are penalised for missed Casper FFG votes, that is, missed source or target votes. But there is no penalty for a missed head vote. If a source vote is incorrect, then the target vote is missed; if the source or target vote is incorrect then the head vote is missed.

Let's update our rewards' matrix to give the full picture of penalties and rewards for attestations. Recall that this shows the weights; we need to multiply by $\frac{nb}{W_{\Sigma}}$ to get the actual reward.

Timeliness	1 slot	<=5 slots	<= 32 slots	> 32 Slots (missing)
Wrong source	$-W_s - W_t$	$-W_s - W_t$	$-W_s - W_t$	$-W_s - W_t$
Correct source only	$W_s - W_t$	W_s-W_t	$-W_s-W_t$	$-W_s-W_t$
Correct source and target only	$W_s + W_t$	$W_s + W_t$	$-W_s + W_t$	$-W_s-W_t$
Correct source, target and head	$W_s + W_t + W_h$	$W_s + W_t$	$-W_s + W_t$	$-W_s-W_t$

For more intuition, we can put in the numbers, $W_s=14,~W_t=26,~W_h=14,$ and normalise with $W_{\Sigma}=64$:

Timeliness	1 slot	<=5 slots	<= 32 slots	> 32 Slots (missing)
Wrong source	-0.625	-0.625	-0.625	-0.625
Correct source only	-0.188	-0.188	-0.625	-0.625
Correct source and target only	+0.625	+0.625	+0.188	-0.625
Correct source, target and head	+0.844	+0.625	+0.188	-0.625

Break-even uptime

Stakers sometimes worry that downtime will be very expensive. To examine this, we can estimate the break-even uptime. We'll ignore sync committee participation since that is so rare, so only attestations are relevant for the calculation.

We'll assume that, when online, the validator's performance is perfect, and that the rest of the validators are performing well (both of which are pretty good approximations to the beacon chain's actual performance over its first year).

If p is the proportion of time the validator is online, then its net income is, 0.844p - 0.625(1 - p) = 1.469p - 0.625. This is positive for p > 42.5%. So, if your validator is online more than 42.5% of the time, you will be earning a positive return.

A useful rule of thumb is that it takes about a day of uptime to recover from a day of downtime.

Sync committee penalties

The small group of validators currently on sync committee duty receive a reward in each slot that they sign off on the correct head block (correct from the proposer's point of view).

Validators that don't participate (sign the wrong head block or don't show up at all) receive a penalty exactly equal to the reward they would have earned for being correct. And the block proposer receives nothing for the missing contribution.

Historical note: Since sync committee participation is rare for any given validator, and since rewards are significant, there were concerns with earlier designs that the resulting variance in rewards for validators would be quite unfair. Small stakers might prefer to join staking pools rather than solo stake in order to smooth out the variance, similarly to how proof of work mining pools have sprung up.

One suggested approach to reducing the variance was not to reward sync committee participation at all, but rather to raise overall reward levels for everyone and to penalise the sync committee validators if they did not participate. Ultimately the approach adopted was to reduce the length of sync committees (meaning lower rewards, but more often), reduce the proportion of total reward for participation, and introduce a penalty for non-participation – kind of half-way to the other proposal.

The main reasons⁶² for not adopting the former proposal, although it is elegant, seem to be around the psychology of being explicitly penalised but never explicitly rewarded. The penalty for not participating in a sync committee would be substantially bigger than the attestation reward over an epoch. In addition, participation is not entirely in the validator's own hands: it depends on the next block proposer being on the right fork. There were also concerns about changing the clean relationship between proposer rewards and the value of the duties they include in blocks.

Remarks on penalties

There are no explicit penalties related to block proposers.

In particular, there is no explicit penalty for failing to include deposits from the Eth1 chain, nor any direct incentive for including them. However, if a block proposer does not include deposits that the rest of the network knows about, then its block is invalid. This provides a powerful incentive to include outstanding deposits.

Also note that penalties are not scaled with participation as rewards are.

See also

The detailed penalty calculations are defined in the spec in these functions:

- Penalties for missed attestations are calculated in get_flag_index_deltas() as part of epoch processing.
- Penalties for missed sync committee participation are calculated in process_sync_aggregate() as part of block processing.

Inactivity leak

- When the beacon chain is not finalising it enters a special "inactivity leak" mode
- Attesters receive no rewards. Non-participating validators receive increasingly large penalties based on their track records.
- This is designed to restore finality in the event of the permanent failure of large numbers of validators.

 $^{^{62}\}mathrm{The}$ quite interesting discussion remains on the Ethereum R&D Discord.

Introduction

If the beacon chain hasn't finalised a checkpoint for longer than MIN_EPOCHS_TO_INACTIVITY_PENALTY (4) epochs, then it enters "inactivity leak" mode⁶³.

The inactivity leak is a kind of emergency state in which rewards and penalties are modified as follows.

- Attesters receive no attestation rewards while attestation penalties are unchanged.
- Any validators deemed inactive have their inactivity scores raised, leading to an additional inactivity
 penalty that potentially grows quadratically with time. This is the inactivity leak, sometimes known
 as the quadratic leak.
- Proposer and sync committee rewards are unchanged.

The idea for the inactivity leak was proposed in the original Casper FFG paper. The problem it addresses is that of how to recover finality (liveness, in some sense) in the event that over one-third of validators goes offline. Finality requires a majority vote from validators representing 2/3 of the total stake.

The mechanism works as follows. When loss of finality is detected the inactivity leak gradually reduces the stakes of validators who are not making attestations until, eventually, the participating validators control 2/3 of the remaining stake. They can then begin to finalise checkpoints once again.

This inactivity penalty mechanism is designed to protect the chain long-term in the face of catastrophic events (sometimes referred to as the ability to survive World War III). The result might be that the beacon chain could permanently split into two independent chains either side of a network partition, and this is assumed to be a reasonable outcome for any problem that can't be fixed in a few weeks. In this sense, the beacon chain formally prioritises availability over consistency. (You can't have both.)

In any case, it provides a powerful incentive for stakers to fix any issues they have and to get back online.

The reason why no validators receive attestation rewards during an inactivity leak is once again due to the possibility of discouragement attacks. An attacker might deliberately drive the beacon chain into an inactivity leak, perhaps by a combination of censorship and denial of service attack on other validators. This would cause the non-participants to suffer the leak, while the attacker continues to attest normally. We need to increase the cost to the attacker in this scenario, which we do by not rewarding attestations at all during an inactivity leak.

As with penalties, the amounts subtracted from validators' beacon chain accounts due to the inactivity leak are effectively burned, reducing the overall net issuance of the beacon chain.

Mathematics

Let's study the effect of the leak on a single validator's balance, assuming that during the period of the inactivity leak (non-finalisation) the validator is completely offline.

At each epoch, the offline validator will be penalised an amount proportional to tB/α , where t is the number of epochs since the chain last finalised, B is the validator's effective balance, and α is the prevailing inactivity penalty quotient (currently INACTIVITY PENALTY QUOTIENT BELLATRIX).

The effective balance B will remain constant for a while, by design, during which time the total amount of the penalty after t epochs would be $t(t+1)B/2\alpha$: the famous "quadratic leak". If B were continuously variable, the penalty would satisfy $\frac{dB}{dt} = -\frac{tB}{\alpha}$, which can be solved to give the exponential $B(t) = B_0 e^{-t^2/2\alpha}$. The actual behaviour is somewhere between these two (piecewise quadratic) since the effective balance is neither constant nor continuously variable but decreases in a step-wise fashion.

In the continuous approximation, the inactivity penalty quotient, α , is the square of the time it takes to reduce the balance of a non-participating validator to $1/\sqrt{e}$, or around 60.7% of its initial value. With the value of INACTIVITY PENALTY QUOTIENT BELLATRIX at 2^{24} , this equates to 4096 epochs, or 18.2 days.

For Phase 0 of the beacon chain, the value of INACTIVITY_PENALTY_QUOTIENT was increased by a factor of four from 2^{24} to 2^{26} , so that validators would be penalised less severely if there were non-finalisation due

⁶³The Ethereum mainnet had nine consecutive epochs of delayed finality from epoch 200,750 to 200,758 on the 12th of May, 2023. This was the first sufficiently long period of delayed finality on mainnet to trigger the inactivity leak.

to implementation problems in the early days. As it happens, there were no instances of non-finalisation during the whole eleven months of Phase 0 of the beacon chain.

The value was decreased by one quarter in the Altair upgrade from 2^{26} (INACTIVITY_PENALTY_QUOTIENT) to $3 \cdot 2^{24}$ (INACTIVITY_PENALTY_QUOTIENT_ALTAIR), and to its final value of 2^{24} (INACTIVITY_PENALTY_QUOTIENT_BELLATRIX) in the Bellatrix upgrade. Decreasing the inactivity penalty quotient speeds up recovery of finalisation in the event of an inactivity leak.

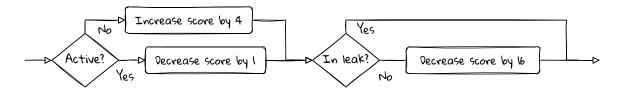
Inactivity scores

During Phase 0, the inactivity penalty was an increasing global amount applied to all validators that did not participate in an epoch, regardless of their individual track records of participation. So a validator that was able to participate for a significant fraction of the time could still be quite severely penalised due to the growth of the inactivity penalty. Vitalik gives a simplified example: "if fully [off]line validators get leaked and lose 40% of their balance, someone who has been trying hard to stay online and succeeds at 90% of their duties would still lose 4% of their balance. Arguably this is unfair." We found during the Medalla testnet incident that keeping a validator online when all around you is chaos is not easy. We don't want to punish stakers who are honestly doing their best.

To improve this, the Altair upgrade introduced individual validator inactivity scores that are stored in the state. Validators' scores are updated each epoch as follows.

- At the end of epoch N, irrespective of the inactivity leak,
 - decrease a validator's score by one when it made a correct and timely target vote in epoch N-1, and
 - increase the validator's score by INACTIVITY_SCORE_BIAS (four) otherwise.
- When *not* in an inactivity leak,
 - decrease every validator's score by INACTIVITY SCORE RECOVERY RATE (sixteen).

Graphically, the flow-chart looks like this.



How each validator's inactivity score is updated. The happy flow is right through the middle. "Active", when updating the scores at the end of epoch N, means having made a correct and timely target vote in epoch N-1.

Note that there is a floor of zero on the score.

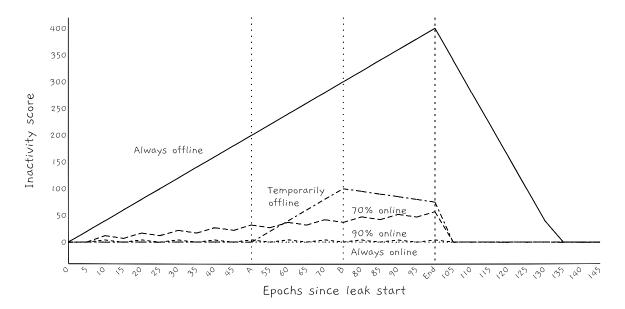
When not in an inactivity leak validators' inactivity scores are reduced by INACTIVITY_SCORE_RECOVERY_RATE + 1 per epoch when they make a timely target vote, and by INACTIVITY_SCORE_RECOVERY_RATE - INACTIVITY_SCORE_BIAS when they don't. So, even for non-performing validators, scores decrease outside a leak

When in a leak, if p is the participation rate between 0 and 1, and λ is INACTIVITY_SCORE_BIAS, then the expected score after N epochs is $\max(0, N((1-p)\lambda-p))$. For $\lambda=4$ this is $\max(0, N(4-5p))$. So a validator that is participating 80% of the time or more can maintain a score that is bounded near zero. With less than 80% average participation, its score will increase unboundedly.

This is nice because, if many validators are able to participate intermittently, it indicates that whatever event has befallen the chain is potentially recoverable, unlike a permanent network partition, or a supermajority network fork, for example. The inactivity leak is intended to bring finality to irrecoverable situations, so prolonging the time to finality if it's recoverable is likely a good thing.

The following graph illustrates some scenarios. We have an inactivity leak that starts at zero, and ends after 100 epochs, after which finality is recovered and we are no longer in the leak. There are five validators. Working up from the lowest line, they are:

- 1. Always online: correctly registering a timely target vote in every epoch. The inactivity score remains at zero.
- 2. 90% online: the inactivity score remains bounded near zero. From the analysis above, it is expected that anything better than 80% online will bound the score near zero.
- 3. 70% online: the inactivity score grows slowly over time.
- 4. Generally online, but offline between epochs 50 and 75: the inactivity score is zero during the initial online period; grows linearly and fairly rapidly while offline during the leak; declines slowly when back online during the leak; and declines rapidly once the leak is over.
- 5. Always offline: the inactivity score increases rapidly during the leak, and declines even more rapidly once the leak is over.



The inactivity scores of five different validator personas in an inactivity leak that starts at zero and ends at epoch 100 (labelled "End" and shown with a dashed line). The dotted lines labelled "A" and "B" mark the start and end of the offline period for the fourth validator.

Inactivity penalties

The inactivity penalty is applied to all validators at every epoch based on their individual inactivity scores, irrespective of whether a leak is in progress or not. When there is no leak, the scores return to zero (rapidly for active validators, less rapidly for inactive ones), so most of the time this is a no-op.

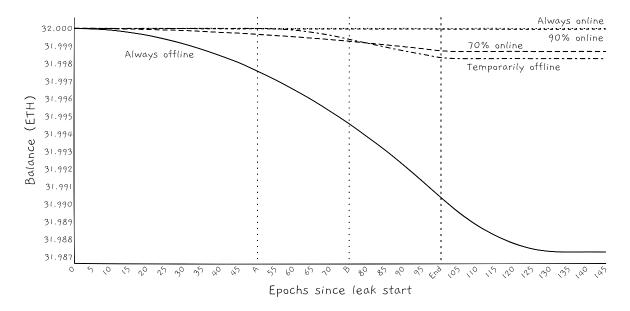
The penalty for validator i is calculated as

$$s_i B_i / (\text{INACTIVITY_SCORE_BIAS} \times \text{INACTIVITY_PENALTY_QUOTIENT_BELLATRIX}) \\ = \frac{s_i B_i}{4 \times 16,777,216}$$

where s_i is the validator's inactivity score, and B_i is the validator's effective balance.

This penalty is applied at each epoch, so (for constant B_i) the total penalty is proportional to the area under the curve of the inactivity score, above. With the same five validator persona's we can quantify the penalties in the following graph.

- 1. Always online: no penalty due to the leak.
- 2. 90% online: negligible penalty due to the leak.
- 3. 70% online: the total penalty grows quadratically but slowly during the leak, and rapidly stops after the leak ends.
- 4. Generally online, but offline between epochs 50 and 75: a growing penalty during the leak, that rapidly stops when the leak ends.
- 5. Always offline: we can clearly see the quadratic nature of the penalty in the initial parabolic shape of the curve. After the end of the leak it takes around 35 epochs for the penalties to return to zero.



The balance retained by each of the five validator personas after the inactivity leak penalty has been applied. The scenario is identical to the chart above.

We can see that the new scoring system means that some validators will continue to be penalised due to the leak even after finalisation starts again. This is intentional. When the leak causes the beacon chain to finalise, at that point we have just two-thirds of the stake online. If we immediately stop the leak (as we used to), then the amount of stake online would remain close to two-thirds and the chain would be vulnerable to flipping in and out of finality as small numbers of validators come and go. We saw this behaviour on some of the testnets prior to launch. Continuing the leak after finalisation serves to increase the balances of participating validators to greater than two-thirds, providing a buffer that should mitigate such behaviour.

Ejection

It is not necessary for non-participating validators to be ejected from the active validator set in order for the inactivity leak to be effective at regaining finality. Reducing the proportion of the total stake held by those non-participating validators is sufficient.

Nonetheless, a validator will be exited when its effective balance drops to EJECTION_BALANCE. This is taken care of in the end of epoch registry updates. Note that, due to the way that effective balance is calculated, the ejection will happen when the actual balance drops below 16.75 ETH.

We can simulate how long it would take for a completely offline validator to be ejected due solely to the inactivity leak. It will be slightly sooner in reality due to the additional penalties for missing attestations.

Ejection simulation code

INACTIVITY SCORE BIAS = 4

INACTIVITY PENALTY QUOTIENT = 2 ** 24

For a validator starting the leak period with an actual balance of 32 ETH, the simulation shows that it would take 4686 epochs (almost 3 weeks) for it to be ejected. We can also take this as a rough upper-bound on how long it would take the beacon chain to recover finality, however many validators went offline⁶⁴.

GWEI = 10 ** 9
EJECTION_BALANCE = 16 * GWEI
MAX_EFFECTIVE_BALANCE = 32 * GWEI
HYSTERESIS_QUOTIENT = 4

```
# Simplified hysteresis for monotonically decreasing balance
def calc_effective_balance(balance):
    return min(MAX_EFFECTIVE_BALANCE, (balance + GWEI // HYSTERESIS_QUOTIENT) // GWEI * GWEI)
```

```
score = 0
balance = 32 * GWEI
effective_balance = calc_effective_balance(balance)
while effective_balance > EJECTION_BALANCE:
    balance -= effective_balance * score // (INACTIVITY_SCORE_BIAS * INACTIVITY_PENALTY_QUOTIENT)
    effective_balance = calc_effective_balance(balance)
    score += INACTIVITY_SCORE_BIAS
    epoch += 1

print(balance / GWEI)
```

See also

print(epoch)

epoch = 0

From the spec:

print(effective_balance // GWEI)

- Inactivity scores are updated during epoch processing in process_inactivity_updates().
- Inactivity penalties are calculated in def get inactivity penalty deltas().

For the original description of the mechanics of the inactivity leak, see the Casper paper, section 4.2.

Slashing

- Validators are slashed for breaking very specific protocol rules that could be part of an attack on the chain.
- Slashed validators are exited from the beacon chain and receive three types of penalty.
- Correlated penalties mean that punishment is light for isolated incidents, but severe when many validators are slashed in a short time period.
- Block proposers receive rewards for reporting evidence of slashable offences.

⁶⁴This is complicated by the need for validators to be queued for exit, and the rate-limit on processing that queue. It is not possible to instantly exit validators en masse. Exiting validators remain subject to the inactivity leak while they sit in the queue, so their effective balances could drop lower than 16 ETH.

Introduction

Slashing occurs when validators make attestations or block proposals that break very specific protocol rules. It applies to behaviour that could potentially be part of an attack on the chain. Getting slashed means losing a significant amount of stake and being ejected from the protocol. It is more "punishment" than "penalty"⁶⁵. The good news is that stakers can take simple precautions to protect against ever being slashed.

The behaviours that lead to slashing are as follows.

- 1. Related to Casper FFG consensus,
 - making two differing attestations for the same target checkpoint, or
 - making an attestation whose source and target votes "surround" those in another attestation from the same validator.
- 2. Related to LMD GHOST consensus,
 - proposing more than one distinct block at the same height, or
 - attesting to different head blocks, with the same source and target checkpoints⁶⁶.

All of these slashable behaviours relate to "equivocation", which is when a validator contradicts something it previously advertised to the network. 67

The slashing conditions related to Casper FFG underpin Ethereum 2.0's economic finality guarantee. They effectively impose a well-determined price on reverting finality.

The slashing conditions related to LMD GHOST are designed to combat the nothing at stake problem, and are not directly related to economic finality. They punish bad behaviour that could lead to serious issues such as the balancing attack. Since we already had the slashing mechanism available for use with Casper FFG, it was simple enough to extend it to LMD GHOST.

As with penalties, any amount removed from validators' beacon chain accounts due to slashing is effectively burned, reducing the overall net issuance of the beacon chain.

The cost of being slashed

When it comes to the punishment for being slashed it does not matter which rule was broken. All slashings are dealt with in the same way.

The initial penalty

Slashing is triggered by the evidence of the offence being included in a beacon chain block. Once the evidence is confirmed by the network, the offending validator (or validators) is slashed.

The offender immediately has $\frac{1}{32}$ (MIN_SLASHING_PENALTY_QUOTIENT_BELLATRIX) of its effective balance deducted from its actual balance. This is a maximum of 1 ETH due to the cap on effective balance.

This initial penalty was introduced to make it somewhat costly for validators to self-slash for any reason⁶⁸.

⁶⁵The concept of slashing has its roots in Vitalik's Slasher algorithm from early 2014. Our current design looks quite different, but some things remain. In particular, he says that, "we are calling [it] Slasher to express its harshly punitive nature", and we retail the name "slashing" for the same reason.

⁶⁶This condition is not very obvious in the code. It comes about because two attestations with the same source and target votes but different head votes differ from each other. They are therefore counted as conflicting votes for the same target and slashed under the first Casper FFG rule.

⁶⁷To avoid being slashed, simply be sure not to equivocate. Any normally operating client (in the absence of bugs) will never do so. As far as can be determined, every Ethereum slashing to date has been due to a node operator simultaneously running the same validator keys on two different nodes, perhaps as a misguided way to improve uptime. Don't do this. (Update: one slashing was due to a proposer attacking a MEV Relay.)

⁶⁸It is not clear to me under what circumstances self-slashing would give any advantage under the beacon chain's current design. To date, the only effect of the initial penalty has been to punish small stakers for misconfiguring their staking setups (by running keys in more than one place) which seems to me unduly harsh. I have argued that it ought to be removed entirely. Nonetheless, it remains.

Along with the initial penalty, the validator is queued for exit, and has its withdrawability epoch set to around 36 days (EPOCHS_PER_SLASHINGS_VECTOR, which is 8192 epochs) in the future.

During Phase 0 the initial penalty was $\frac{1}{128}$ of the offender's effective balance, and during Altair, $\frac{1}{64}$. It was raised to its full value of $\frac{1}{32}$ of the slashed validator's effective balance, a maximum of 1 ETH, in the pre-Merge Bellatrix upgrade.

The correlation penalty

At the halfway point of its withdrawability period (18 days after being slashed) the slashed validator is due to receive a second penalty.

This second penalty is based on the total amount of stake slashed during the 18 days before and after our validator was slashed. The idea is to scale the punishment so that a one-off event posing little threat to the chain is only lightly punished, while a mass slashing event that might be the result of an attempt to finalise conflicting blocks is punished to the maximum extent possible.

To be able to calculate this, the beacon chain maintains a record of the effective balances of all validators that were slashed during the most recent 8192 epochs (about 36 days).

The correlated penalty is calculated as follows.

- 1. Compute the sum of the effective balances (as they were when the validators were slashed) of all validators that were slashed in the previous 36 days. That is, for the 18 days preceding and the 18 days following our validator's slashing.
- 2. Multiply this sum by PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX, but cap the result at total_balance, the total active balance of all validators.
- 3. Multiply the slashed validator's effective balance by the result of #2 and then divide by the total_balance. This results in an amount between zero and the full effective balance of the slashed validator. That amount is subtracted from its actual balance as the penalty. Note that the effective balance could exceed the actual balance in odd corner cases, but decrease_balance() ensures the balance does not go negative.

The slashing multiplier since Bellatrix is set to 3. With S being the sum of increments in the list of slashed validators over the last 36 days, B my effective balance, and T the total increments, the calculation looks as follows.

Correlation penalty =
$$\min(B, \frac{3SB}{T})$$

Interestingly, due to the way the integer arithmetic is constructed in the implementation the result of this calculation will be zero if 3SB < T. Effectively, the penalty is rounded down to the nearest whole amount of Ether. As a consequence, when there are few slashings there is no extra correlated slashing penalty at all, which is probably a good thing.

The proportional slashing multiplier was increased gradually through the early deployment of the beacon chain. At Genesis, it was set to one (PROPORTIONAL_SLASHING_MULTIPLIER), at Altair it was increased to two (PROPORTIONAL_SLASHING_MULTIPLIER_ALTAIR), and at Bellatrix set to its final value of three (PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX). This was intended to punish slashed validators less harshly while we were becoming accustomed to running the beacon chain. As it happened, no correlated slashings occurred that incurred a penalty greater than zero under this mechanism.

Other penalties

Validators that exit normally (by sending a voluntary exit message) are expected to participate only until their exit epoch, which is normally only a couple of epochs later.

A validator that is slashed continues to receive attestation penalties until its withdrawable epoch, which is set to 8192 epochs (36 days) after the slashing, and they are unable to receive any attestation rewards

during this time. They are also subject for this entire period to any inactivity leak that might be in operation. Whatever the slashed validator does, it is penalised exactly as if it is failing to participate.⁶⁹

So, in addition to the initial slashing penalty and the correlation penalty, there is a further penalty of up to $8192\frac{14+26}{64}32b = 82,739,200$ Gwei = 0.0827 ETH, based on 500k validators, where b is the base reward per increment. This assumes that the chain is not in an inactivity leak; the penalties will be much higher if it is.

Slashed validators are eligible to be selected to propose blocks until they reach their exit epoch, but those blocks will be considered invalid, so there is no proposer reward available to them. This is in preference to immediately recomputing the duties assignments which would break the lookahead guarantees they have. (The proposer selection algorithm could easily be modified to skip slashed validators, but that is not how it is implemented currently.)

In an interesting edge case, however, slashed validators are eligible to be selected for sync committee duty until they reach their exit epoch and to receive the rewards for sync committee participation. The odds of this happening, though, in the absence of a mass slashing event, are pretty tiny.

The value of reporting a slashing

In order for the beacon chain to verify slashings and take action against the offender, the evidence needs to be included in a beacon block. To incentivise validators to make the effort there is a specific reward for the proposer of a block that includes slashings.

The proposer reward

At the point of the initial slashing report being included in a block, the proposer of the block receives a reward of validator.effective_balance / WHISTLEBLOWER_REWARD_QUOTIENT, which is B/512 if B is the effective balance of the validator being slashed.

A report of a proposer slashing violation can slash only one validator, but a report of an attestation slashing violation can simultaneously slash up to an entire committee, which might be hundreds of validators. This could be very lucrative for the proposer including the reports. A single block can contain up to 16 proposer slashing reports and up to 2 attester slashing reports.

Note that no new issuance is required to pay for this reward. The proposer reward is much less than the initial slashing applied to the validator, so the net issuance due to a slashing event is always negative.

The whistleblower reward

In the code implementing the reward for reporting slashing evidence there is provision for a "whistleblower reward", with the whistleblower receiving $\frac{7}{8}$ of the above reward and the proposer $\frac{1}{8}$.

The idea is to incentivise nodes that search for and discover evidence of slashable behaviour, which can be an intensive process.

However, this functionality is not currently used on the beacon chain, and the proposer receives both the whistleblower reward and the proposer reward, as above. The challenge is that it is too easy for a proposer just to steal a slashing report, so there's no point incentivising them separately. It's not an ideal situation, but so far there seem to be sufficient altruistic slashing detectors running on the beacon chain for slashings to be reported swiftly. There only needs to be one in practice.

This functionality may become useful in future upgrades.

See also

From the spec:

 The initial slashing penalty and proposer reward are applied in slash_validator() during block processing.

⁶⁹Having such a long overhang from being slashed during which validators continue to receive penalties seems like "kicking a man when he's down", especially since slashed validators are locked in for twice as long as needed to calculate the correlation penalty. Vitalik says that this measure "is included to prevent self-slashing from being a way to escape inactivity leaks." But validators don't need to self-slash to avoid this; they could just make a normal voluntary exit.

• The correlation slashing penalty is applied in process_slashings() during epoch processing.

In the Serenity Design Rationale Vitalik gives some further background on why Ethereum 2.0 includes proposer slashing. It is specifically intended to discourage stakers from simultaneously running primary and backup nodes.

Diversity

- Beacon chain incentives strongly encourage diversity among client deployments, hosting infrastructure, and staking pools.
- Lack of diversity puts at risk both the chain in general and all those running the majority client.
- The greater the share of validators hosted by a single client implementation the greater the risk.
- The beacon chain is at its most robust and fault-tolerant when no single client type manages more than one-third (33%) of validators.

Diversity makes us all stronger

Just as diversity in biological ecosystems makes them more resilient, and monocultures make them very fragile – yes, I've been watching David Attenborough –, so it is with Ethereum staking.

It is not unintentional that both the inactivity leak and the slashing correlation penalty provide a strong encouragement to diversify the network as much as possible.

For example, the inactivity leak is much more likely to occur on a network in which a single client implementation runs over 33% of validators, or a single staking operator controls over 33% of validators, or over 33% of validators are deployed to the same hosting infrastructure. All these scenarios constitute single points of failure that could prevent the beacon chain from finalising and lead to a leak that penalises those running the majority (offline) client most harshly.

Scenarios

Let's consider some scenarios. For the sake of this exercise you are running the beacon chain client X. In each scenario you and others using client X host validators managing a certain fraction of the total stake. We will consider what happens if client X has a bug that takes it down. It might be a consensus bug or another kind of bug that takes the client off the network: we saw examples of both of these on the pre-launch testnets.

1. Client X has less than one-third of the stake

When a client managing less than one-third of the total stake goes down, the consequences are minimal. The beacon chain can continue to finalise as normal. Users of client X will suffer only the normal offline penalties until the bug is fixed, though rewards will be lower across the board for the other validators. But this is not catastrophic and there is time to recover without a panic, either by fixing the bug or swapping to a different client.

The beacon chain is at its most robust and fault-tolerant when no single client type manages more than one-third (33%) of validators.

2. Client X has more than one-third of the stake

If client X goes down while managing more than one-third of the total stake, then the beacon chain will be unable to finalise and will enter the inactivity leak.

In this situation no validators will receive rewards for attesting. Users of non-X clients will not lose stake, but users of client X will suffer much bigger losses than usual, due to the quadratically increasing inactivity leak. There is strong time pressure to get the issue with client X resolved either by fixing the bug or swapping to a different client.

3. Client X has around half of the stake

The situation becomes potentially much worse when X hosts around half of the validators. If X were to have a consensus bug, but otherwise keep running, the beacon chain would split into two similarly sized chains. Each chain would see half its validators missing and start leaking out the stakes of those validators. Within three to four weeks each chain would have leaked out enough of the stake of the missing validators that the present validators would control two-thirds of the remaining stake, meaning that the chains could each finalise separately. It would be extremely difficult – effectively impossible – to reunite these chains ever again since they would contain conflicting finalised checkpoints. The beacon chain would be permanently partitioned.

Hopefully, 3-4 weeks is sufficient time for client X to fix its bug or for users of X to migrate to other clients. Meanwhile, users of X are suffering large inactivity penalties on the correct chain as per scenario 2.

4. Client X approaches or exceeds two-thirds of the stake

A scenario in which a single client approaches⁷⁰ hosting two-thirds (66%) of the validators is potentially catastrophic. A consensus bug in that client would very quickly – possibly within 13 minutes – finalise a broken version of the chain with no chance to intervene.

That would leave the Ethereum community with a horrible dilemma.

One possible response would be to modify the other clients (and the specification) to reproduce the bug and allow them to join X's chain. The feasibility of this depends on the nature of the consensus bug. For a trivial bug it might be possible, but it would be very unfair to the non-X clients since they would suffer penalties despite having acted perfectly correctly. In any case, many types of consensus bug would make this infeasible: one way or another X's chain is broken and now incompatible with the entirety of the rest of the ecosystem.

The correct – but nuclear – option is to fix the bug in client X. Unfortunately, however, there would be no way for the stakers on the incorrect X chain to rejoin the correct chain. Any that tried to do so would be slashed, having previously finalised a checkpoint on the incorrect chain. The only reasonable strategy for (former) users of client X would be to stop validating and voluntarily exit their stakes. Exiting could take a long time due to the queuing mechanism, resulting in large penalties from the inactivity leak. Many of the affected stakers are likely to try to start validating again and would surely be slashed.

There are no good outcomes here, which is why it is critical that we never have a client with a two-thirds or more supermajority.⁷¹

Slashing

As for slashing, once again running a majority client could be an act of self-harm. In the unlikely event that a client implementation has a bug that leads to its validators becoming slashed en-masse, the correlated slashing penalties would be much more severe than if the same thing happened to those running a minority client.

Another view

Danny Ryan has presented a slightly different angle on client diversity that's insightful:

If a single client:

• Does not exceed 66.6%, a fault/bug in a single client cannot be finalized.

⁷⁰If the share is less than 67% the incorrect chain won't finalise immediately, but very soon the inactivity leak will raise the proportion above 67% on that chain, and it will then finalise.

⁷¹As of 2022-01-12, the Prysm client appeared to have 68.1% of the validators.

- Does not exceed 50%, a fault/bug in a single client's fork choice cannot dominate the head of the chain.
- Does not exceed 33.3%, a fault/bug in a single client cannot disrupt finality.

Epilogue

Let me emphasise that these scenarios are far from theoretical. It is of existential importance to the Ethereum network that stakers pay attention to the distribution of client software and avoid adding to the share of the majority client.

It is instructive to revisit the major incident that occurred on the Medalla testnet, in which an issue in the majority client caused a high degree of chaos and led to large numbers of slashings. Had that client managed a smaller proportion of the network, the consequences for everybody would have been much less severe.

See also

- Run the majority client at your own peril! by Dankrad Feist.
- What Happens If Beacon Chain Consensus Fails? by Adrian Sutton.

The Building Blocks

Introduction

In this chapter we will explore some of the fundamental innovations that make the Ethereum 2 protocol practical, the building blocks from which the higher level protocol is constructed.

None of the building blocks is absolutely brand new – they all depend to a degree on existing technologies – but in each case some aspect of the application to Eth2 is novel. The Ethereum Foundation R&D team deserves huge credit for the research and insights behind these advances.

Be alert, as you read, to the trade-offs that underpin these design choices. The gateway to deep understanding is always in the trade-offs.

Some of the trade-offs are quite interesting. For example, neither the shuffling algorithm nor the state root calculation algorithm are the most efficient that we could have chosen, at least in terms of pure speed. In both cases we preferred algorithms that enable a light client ecosystem over algorithms that might be more performant for full nodes.

The building blocks I've grouped together in this chapter are those that are part of the protocol specification itself. Client implementations often employ other optimisations that are not part of the specification. We'll consider some of those later in the Implementation chapter.

These are the topics that I've picked out for special attention.

- BLS Signatures precipitated the total redesign of Ethereum's proof of stake protocol, and underpin the scale and ambition of Ethereum 2.
- Randomness is a vital aspect of security, but difficult to generate in a deterministic system. The beacon chain accomplishes it with BLS signatures.
- Shuffling uses randomness to populate committees. But, for the sake of light clients, we use an "oblivious" shuffle rather than the standard Fisher–Yates.
- Committees distribute the workload of the beacon chain.
- Aggregator Selection secretly selects small subsets of committees to do the work of aggregating attestations.
- SSZ: Simple Serialize is a novel serialisation technique that appears everywhere in the protocol. It
 embodies elegance and efficiency.
- Hash Tree Roots and Merkleization are applications of SSZ. Among other things, they make light clients practical.
- Generalised indices and Merkle proofs (TODO).
- Sync Committees (TODO).

BLS Signatures

- Proof of stake protocols use digital signatures to identify their participants and hold them accountable.
- BLS signatures can be aggregated together, making them efficient to verify at large scale.
- Signature aggregation allows the beacon chain to scale to hundreds of thousands of validators.
- Ethereum transaction signatures on the execution (Eth1) layer remain as-is.

Digital signatures

Digital signatures are heavily used in blockchain technology. A digital signature is applied to a message to ensure two things: (1) that the message has not been tampered with in any way; and (2) that the sender of the message is who it claims to be. Digital signatures are not new, and really developed during the 1980s as a result of the invention of asymmetric cryptography. However, more recent developments involving elliptic curve, pairing-based cryptography have heavily influenced the design of Ethereum 2.

Every time you send an Ethereum transaction you are using a digital signature; all Ethereum users are familiar with the signing work flow. But that's at the transaction level. At the consensus protocol level digital signatures are not used at all in Ethereum 1 – Under proof of work, a block just needs to have a correct mixHash proving that it was correctly mined, nobody cares who actually mined the block, so no signature is needed.

In Ethereum 2, however, validators have identities and are accountable for their actions. In order to enforce the Casper FFG rules, and in order to be able to count votes for the LMD GHOST fork choice, we need to be able to uniquely identify the validators making individual attestations and blocks.

Digital signature usage

The primary function of a digital signature is to irrevocably link the sender of a message with the contents of the message. This can be used, for example, to prove with certainty that a validator has published conflicting votes and is therefore subject to being slashed.

The ability to tie messages to validators is also useful outside the protocol. For example, in the gossip layer, signatures are validated by nodes before they are forwarded as an anti-spam mechanism.

Alongside their usual function of identifying message senders, digital signatures have a couple of fairly novel uses within the Ethereum 2 protocol. They are used when contributing randomness to the RANDAO, and they are used when selecting subsets of committees for aggregation duty. We will discuss those usages in their respective sections and focus on the signing of protocol messages in this section.

Background

One of the characteristics of proof of stake protocols is the sheer number of protocol messages that need to be handled. With 500,000 active validators, the current beacon chain design calls for over 1,300 attestations per second to be gossiped across the network. That's a sustained average, there are much higher bursts in practice. Not only do these messages need to travel over the network, but each individual digital signature needs to be verified by every node, which is a CPU-intensive operation. Not to mention having to store all those signed messages in the block history. These challenging requirements have typically limited the validator numbers in proof of stake or proof of authority networks. Pure PBFT-based consensus protocols tend to have validator sets that number in the dozens rather than the thousands.

The prevailing work-in-progress design in early 2018 for Ethereum's (partial) move to proof of stake, EIP-1011, estimated that the protocol could handle a maximum of around 900 validators due to this message overhead, and accordingly set a hefty stake size of 1500 ETH per validator.

The turning point came in May 2018 with the publication by Justin Drake of an article on the Ethresear.ch forum titled Pragmatic signature aggregation with BLS. The article proposed using a new signature scheme that is able to aggregate many digital signatures into one while preserving the individual accountability of each validator that signed. Aggregation provides a way to dramatically reduce the number of individual messages that must be gossiped around the network, and the cost of verifying the integrity of those messages. It therefore enables us to scale to hundreds of thousands of consensus participants.⁷²

⁷²To give credit where it is due, the Dfinity blockchain researchers had published a white paper a few months earlier proposing the use of BLS signatures in a threshold scheme. However, their use of threshold signatures makes the chain vulnerable to liveness failures, and also requires a tricky distributed key generation protocol. Ethereum's aggregation-based approach has neither of these issues. Nonetheless, the name "beacon chain" that we still use today derives from Dfinity's "randomness beacon" described in that paper.

This signature aggregation capability was the main breakthrough that prompted us to abandon the EIP-1011 on-chain PoS management mechanism entirely and move to the "beacon chain" model that we have today⁷³.

BLS Digital Signatures

Digital signatures in the blockchain world are usually based on elliptic curve groups. For signing users' transactions, Ethereum uses ECDSA signatures with the secp256k1 elliptic curve. However, the beacon chain protocol uses BLS signatures with the BLS12-381 elliptic curve⁷⁴. Although similar in usage, ECDSA and BLS signatures are mathematically quite different, with the latter relying on a special property of certain elliptic curves called "pairing". Although ECDSA signatures are much faster than BLS signatures, it is the pairing property of BLS signatures that allows us to aggregate signatures, thus making the whole consensus protocol practical.

Several other blockchain protocols have adopted or will adopt BLS signatures over the BLS12-381 curve, and throughout our implementation in Eth2 we have been mindful to follow whatever standards exist, and to participate in the defining of those standards where possible. This both helps interoperability and supports the development of common libraries and tooling.

The high-level workflow for creating and verifying a BLS signature is relatively straightforward. In the sections that follow I'll describe how it all works with some words, some pictures, and some maths. Feel free to skip the maths if you wish, it's not compulsory and there's no test at the end. Though it is rather elegant.

Components

There are four component pieces of data within the BLS digital signature process.

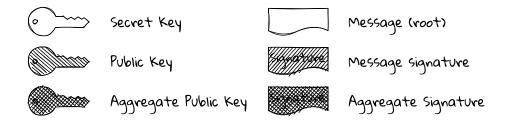
- 1. The secret key. Every entity acting within the protocol (that is, a validator in the context of Eth2) has a secret key, sometimes called a private key. The secret key is used to sign messages and must be kept secret, as its name suggests.
- 2. The *public key*. The public key is uniquely derived from the secret key, but the secret key cannot be reverse engineered from it (without impossibly huge amounts of work). A validator's public key represents its identity within the protocol, and is known to everybody.
- 3. The *message*. We'll look later at the kinds of messages used in the Eth2 protocol and how they are constructed. For now, the message is just a string of bytes.
- 4. The *signature*, which is the output of the signing process. The signature is created by combining the message with the secret key. Given a message, a signature for that message, and a public key, we can verify that the validator with that public key signed exactly that message. In other words, no-one else could have signed that message, and the message has not been changed since signing.

More mathematically, things look like this. We use two subgroups of the BLS12-381 elliptic curve: G_1 defined over a base field F_q , and G_2 defined over the field extension F_{q^2} . The order of both the subgroups is r, a 77 digit prime number. The (arbitrarily chosen) generator of G_1 is g_1 , and of G_2 , g_2 .

- 1. The secret key, sk, is a number between 1 and r (technically the range includes 1, but not r. However, very small values of sk would be hopelessly insecure).
- 2. The public key, pk, is $[sk]g_1$ where the square brackets represent scalar multiplication of the elliptic curve group point. The public key is therefore a member of the G_1 group.
- 3. The message, m is a sequence of bytes. During the signing process this will be mapped to some point H(m) that is a member of the G_2 group.
- 4. The signature, σ , is also a member of the G_2 group, namely [sk]H(m).

⁷³The last significant update to EIP-1011 was made on the 16th of May 2018. Justin Drake's post on signature aggregation was made just two weeks later.

⁷⁴There is a curious naming collision here. The BLS trio of "BLS signatures" are Boneh, Lynn, and Shacham, whereas those of the "BLS12-381" elliptic curve are Barreto, Lynn, and Scott. Ben Lynn is the only common name between the two.



The key to the keys. This is how we will depict the various components in the diagrams below. Variants of the same object are hatched differently. The secret key is mathematically a scalar; public keys are G_1 group members; message roots are mapped to G_2 group members; and signatures are G_2 group members.

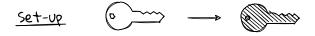
Key pairs

A key pair is a secret key along with its public key. Together these irrefutably link each validator with its actions.

Every validator on the beacon chain has at least one key pair, the "signing key" that is used in daily operations (making attestations, producing blocks, etc.). Depending on which version of withdrawal credentials the validator is using, it may also have a second BLS key pair, the "withdrawal key", that is kept offline.

The secret key is supposed to be uniformly randomly generated in the range [1, r). EIP-2333 defines a standard way to do this based on the KeyGen method of the draft IRTF BLS signatures standard. It's not compulsory to use this method – no-one will ever know if you don't – but you'd be ill-advised not to. In practice, many stakers generate their keys with the eth2.0-deposit-cli tool created by the Ethereum Foundation. Operationally, key pairs are often stored in password-protected EIP-2335 keystore files.

The secret key, sk is a 32 byte unsigned integer. The public key, pk, is a point on the G_1 curve, which is represented in-protocol in its compressed serialised form as a string of 48 bytes.



A validator randomly generates its secret key. Its public key is then derived from that.

Signing

In the beacon chain protocol the only messages that get signed are hash tree roots of objects: their so-called signing roots, which are 32 byte strings. The compute_signing_root() function always combines the hash tree root of an object with a "domain" as described below.

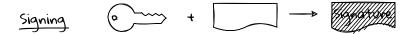
Once we have the signing root it needs to be mapped onto an elliptic curve point in the G_2 group. If the message's signing root is m, then the point is H(m) where H() is a function that maps bytes to G_2 . This mapping is hard to do well, and an entire draft standard exists to define the process. Thankfully, we can ignore the details completely and leave them to our cryptographic libraries⁷⁵.

Now that we have H(m), the signing process itself is simple, being just a scalar multiplication of the G_2 point by the secret key:

$$\sigma = [sk]H(m)$$

 $^{^{75}}$ Unless you have to implement the thing, as I ended up doing in Java.

Evidently the signature σ is also a member of the G_2 group, and it serialises to a 96 byte string in compressed form.



A validator applies its secret key to a message to generate a unique digital signature.

Verifying

To verify a signature we need to know the public key of the validator that signed it. Every validator's public key is stored in the beacon state and can be simply looked up via the validator's index which, by design, is always available by some means whenever it's required.

Signature verification can be treated as a black-box: we send the message, the public key, and the signature to the verifier; if after some cryptographic magic the signature matches the public key and the message then we declare it valid. Otherwise, either the signature is corrupt, the incorrect secret key was used, or the message is not what was signed.

More formally, signatures are verified using elliptic curve pairings.

With respect to the curve BLS12-381, a pairing simply takes a point $P \in G_1$, and a point $Q \in G_2$ and outputs a point from a group $G_T \subset F_{q^{12}}$. That is, for a pairing $e, e : G_1 \times G_2 \to G_T$.

Pairings are usually denoted e(P,Q) and have special properties. In particular, with P and S in G_1 and Q and R in G_2 ,

- $e(P, Q + R) = e(P, Q) \cdot e(P, R)$, and
- $e(P + S, R) = e(P, R) \cdot e(S, R)$.

(Conventionally G_1 and G_2 are written as additive groups, and G_T as multiplicative, so the \cdot operator is point multiplication in G_T .)

From this, we can deduce that all the following identities hold:

$$e([a]P,[b]Q)=e(P,[b]Q)^a=e(P,Q)^{ab}=e(P,[a]Q)^b=e([b]P,[a]Q)$$

Armed with our pairing, verifying a signature is straightforward. The signature is valid if and only if

$$e(q_1, \sigma) = e(pk, H(m))$$

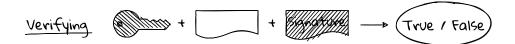
That is, given the message m, the public key pk, the signature σ , and the fixed public value g_1 (the generator of the G_1 group), we can verify that the message was signed by the secret key sk.

This identity comes directly from the properties of pairings described above.

$$e(pk, H(m)) = e([sk]g_1, H(m)) = e(g_1, H(m))^{(sk)} = e(g_1, [sk]H(m)) = e(g_1, \sigma)$$

Note that elliptic curves supporting such a pairing function are very rare. Such curves can be constructed, as BLS12-381 was, but general elliptic curves such as the more commonly used secp256k1 curve do not support pairings and cannot be used for BLS signatures.

 $^{^{76}}$ If it helps, you can loosely think of a pairing as being a way to "multiply" a point in G_1 by a point in G_2 . If we were to write all the groups additively then the arithmetic would work out very nicely. However, we conventionally write G_T multiplicatively, so the notation isn't quite right.



To verify that a particular validator signed a particular message we use the validator's public key, the original message, and the signature. The verification operation outputs true if the signature is correct and false otherwise.

The verification will return True if and only if the signature corresponds both to the public key (that is, the signature and the public key were both generated from the same secret key) and to the message (that is, the message is identical to the one that was signed originally). Otherwise, it will return False.

Aggregation

So far we've looked at the basic set up of BLS signatures. In functional terms, what we've seen is very similar to any other digital signature scheme. Where the magic happens is in aggregation.

Aggregation means that multiple signatures over the same message – potentially thousands of signatures – can be checked with a single verification operation. Furthermore, the aggregate signature has the same size as a regular signature, 96 bytes. This is a massive gain in scalability, and it is this gain that fundamentally makes the Ethereum 2 consensus protocol viable.

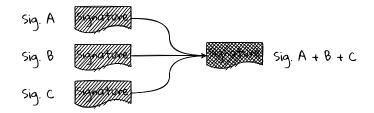
How does this work? Recall that public keys and signatures are elliptic curve points. Because of the bilinearity property of the pairing function, e(), it turns out that we can form linear combinations of public keys and signatures over the same message, and verification still works as expected.

This statement is a little opaque; let's go step by step.

Aggregating signatures

In the following we will only consider aggregation of signatures over the same message⁷⁷.

The process is conceptually very simple: we simply "add up" the signatures. The exact operations are not like the normal addition of numbers that we are familiar with, but the operation is completely analogous. Addition of points on the elliptic curve is the group operation for the G_2 group, and each signature is a point in this group, thus the result is also a point in the group. An aggregated signature is mathematically indistinguishable from a non-aggregated signature, and has the same 96 byte size.

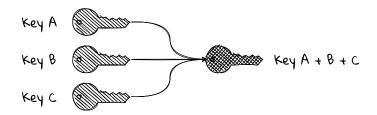


Aggregation of signatures is simply group addition in the G_2 group.

Aggregating public keys

To verify an aggregate signature, we need an aggregate public key. As long as we know exactly which validators signed the original message, this is equally easy to construct. Once again we simply "add up" the public keys of the signers. This time the addition is the group operation of the G_1 elliptic curve group, and the result will also be a member of the G_1 group, so it is mathematically indistinguishable from a non-aggregated public key, and has the same 48 byte size.

⁷⁷A note on terminology. The original paper describing this scheme uses the term "multi-signature" when combining signatures over the same message, and "aggregate signature" when combining signatures over distinct messages. In Eth2 we only do the former, and just call it aggregation.



Aggregation of public keys is simply group addition in the G_1 group.

Verifying aggregate signatures

Since aggregate signatures are indistinguishable from normal signatures, and aggregate public keys are indistinguishable from normal public keys, we can simply feed them into our normal verification algorithm.



Verification of an aggregate signature is identical to verification of a normal signature as long as we use the corresponding aggregate public key.

This miracle is due to the bilinearity of the pairing operation. With an aggregate signature σ_{agg} and a corresponding aggregate public key pk_{agg} , and common message m, we have the following identity, which is exactly the same as the verification identity for a single signature and public key.

$$\begin{split} e(pk_{agg},H(m)) &= e(pk_1 + pk_2 + \dots + pk_n, H(m)) \\ &= e([sk_1 + sk_2 + \dots + sk_n]g_1, H(m)) \\ &= e(g_1,H(m))^{(sk_1 + sk_2 + \dots + sk_n)} \\ &= e(g_1,[sk_1 + sk_2 + \dots + sk_n]H(m)) \\ &= e(g_1,\sigma_1 + \sigma_2 + \dots + \sigma_n) \\ &= e(g_1,\sigma_{agg}) \end{split}$$

Benefits of aggregation

Verification of a BLS signature is expensive (resource intensive) compared with verification of an ECDSA signature – more than an order of magnitude slower due to the pairing operation – so what benefits do we gain?

The benefits accrue when we are able to aggregate significant numbers of signatures. This is exactly what we have with beacon chain attestation committees. Ideally, all the validators in the committee sign-off on the same attestation data, so all their signatures can be aggregated. In practice, there might be differences of opinion about the chain state between committee members resulting in two or three different attestations, but even so there will be many fewer aggregates than the total number of committee members.

Speed benefits

To a first approximation, then, we can verify all the attestations of a whole committee – potentially hundreds – with a single signature verification operation.

This is a first approximation because we also need to account for aggregating the public keys and the signatures. But these aggregation operations involve only point additions in their respective elliptic curve groups, which are very cheap compared with the verification.

In summary:

- We can verify a single signature with two pairings.
- We can naively verify N signatures with 2N pairings.
- Or we can verify N signatures via aggregation with just two pairings, N-1 additions in G_1 , and N-1 additions in G_2 . Each elliptic curve point addition is much, much cheaper than a pairing.

Space benefits

There is also a huge space saving when we aggregate signatures.

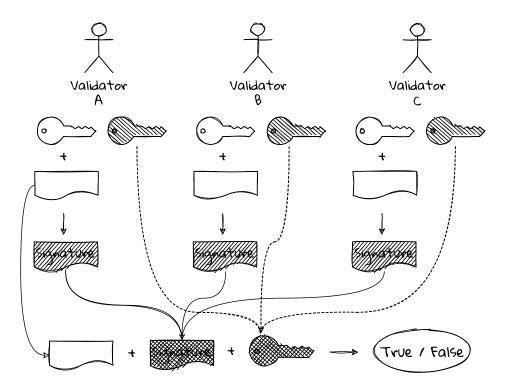
An aggregate signature has 96 bytes as all BLS signatures do. So, to a first approximation, an aggregate of N signatures occupies $\frac{1}{N}$ the space of the unaggregated signatures.

Again, this is only a first approximation. The subtlety here is that, in order to construct the corresponding aggregate public key, we somehow need to keep track of which validators signed the message. We cannot assume that the whole committee participated, and we need to be careful not to include any validator more than once.

If we know in advance who the members of the committee are and how they are ordered then this tracking can be done at the marginal cost of one bit per validator: true if the validator contributed to the aggregate, false if it did not.

The full picture

This diagram illustrates the full flow from signing, through aggregating, to verifying. There are three validators in this case, although there could be many more, and each is signing the same message contents. Each validator has its own unique secret key and public key pair. The workflow is entirely non-interactive, and any of the actions before the verification can happen independently. Even the aggregation can be done incrementally.



The end-to-end aggregate signature workflow. Verifying the single aggregate signature is much faster than verifying the original signatures separately.

Aggregation examples

Two useful examples of how aggregate signatures are used in practice are in aggregate attestations and in sync committee aggregates.

Aggregate attestations

Aggregate attestations are a very compact way to store and prove which validators made a particular attestation.

Within each beacon chain committee at each slot, individual validators attest to their view of the chain, as described in the validator spec.

An Attestation object looks like this:

```
class Attestation(Container):
    aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    signature: BLSSignature
```

When making its attestation, the validator sets a single bit in the aggregation_bits field to indicate which member of the committee it is. That is sufficient, in conjunction with the slot number and the committee index, to uniquely identify the attesting validator in the global validator set.

The signature field is the validator's signature over the AttestationData in the data field.

This attestation will later be aggregated with other attestations from the committee that contain identical data. An attestation is added to an aggregate by copying over its bit from the aggregation_bits field and adding (in the sense of elliptic curve addition) its signature to the signature field. Aggregate attestations can be aggregated together in the same way, but only if their aggregation_bits lists are disjoint: we must not include a validator more than once. (In principle we could include individual validators multiple times, but then we'd need more than a single bit to track how many times, and the redundancy is not useful.)

This aggregate attestation will be gossiped around the network and eventually included in a block. At each step the aggregate signature will be verified.

To verify the signature, a node needs to reconstruct the list of validators in the committee, which it can do from the information in the AttestationData:

```
class AttestationData(Container):
    slot: Slot
    index: CommitteeIndex
    beacon_block_root: Root
...
```

Given the reconstructed list of committee members, the validating node filters the list according to which aggregation_bits are set in the attestation. Now it has the indices of all the validators that contributed to this attestation. The node retrieves the public keys of those validators from the beacon state and aggregates those keys together (by elliptic curve addition).

Finally, the aggregate signature, the aggregate public key, and the signing root of the data are fed into the standard BLS signature verification function. If all is well this will return True, else the aggregate attestation is invalid.

Sync aggregates

SyncAggregates are produced by a sync committee of 512 members.

```
class SyncAggregate(Container):
    sync_committee_bits: Bitvector[SYNC_COMMITTEE_SIZE]
    sync_committee_signature: BLSSignature
```

The current members of the SyncCommittee are stored in the beacon state in the following form:

```
class SyncCommittee(Container):
   pubkeys: Vector[BLSPubkey, SYNC_COMMITTEE_SIZE]
   aggregate_pubkey: BLSPubkey
```

Production and aggregation of sync committee messages differs slightly from attestations, but is sufficiently similar that I'll skip over it here.

The main points of interest are that the SyncCommittee object contains the actual public keys of all the members (possibly with duplicates), rather than validator indices. It also contains a pre-computed aggregate_pubkey field that is the aggregate of all the public keys in the committee.

The idea of this is to reduce the computation load for light clients, who will be the ones needing to verify the SyncAggregate signatures. Sync committees are expected to have high participation, with, say, 90% of the validators contributing. To verify the aggregate signature we need to aggregate the public keys of all the contributors. Starting from an empty set, that would mean 461 elliptic curve point additions (90% of 512). However, if we start from the *full* set, aggregate_pubkey, then we can achieve the same thing by *subtracting* the 10% that did not participate. That's 51 elliptic curve subtractions (which have the same cost as additions) and nine times less work.

Various topics

Domain separation and forks

Every signature that's used in the Eth2 protocol has a domain value mixed into the message before signing. This is taken care of by the compute_signing_root() function which both calculates the SSZ hash tree root of the object to be signed and mixes in the given domain.

```
def compute_signing_root(ssz_object: SSZObject, domain: Domain) -> Root:
    return hash_tree_root(SigningData(
        object_root=hash_tree_root(ssz_object),
        domain=domain,
    ))
```

The domain, in turn, is calculated by the compute_domain() function which combines one of ten domain types with a mash-up of the fork version and the genesis validators root.

Each of the extra quantities that's rolled into the message has a specific purpose.

- The domain type ensures that signatures made for one purpose cannot be re-used for a different purpose. Objects of different SSZ types are not guaranteed to have unique hash tree roots, and we would rather like to be able to tell the difference between them. The ten domain types are all the different ways signatures are used in the protocol.
- The genesis validators root uniquely identifies this particular beacon chain, distinguishing it from any other testnet or alternative chain. This ensures that signatures from different chains are always incompatible.
- The fork version identifies deliberate consensus upgrades to the beacon chain. Mixing the fork version into the message ensures that messages from validators that have not upgraded are invalid. They are out of consensus and have no information that is useful to us, so this provides a convenient way to ignore their messages. Alternatively, a validator may wish to operate on both sides of a contentious fork, and the fork version provides a way for them to do so safely.

The sole exception to the mixing-in of the fork version is signatures on deposits. Deposits are always valid, however the beacon chain gets upgraded.

Choice of groups

BLS signatures are based on two elliptic curve groups, G_1 and G_2 . Elements of G_1 are small (48 bytes when serialised), and their group arithmetic is faster; elements of G_2 are large (96 bytes when serialised) and their group arithmetic is slower, perhaps three times slower.

We can choose to use either group for public keys, as long as we use the other group for signatures: the pairing function doesn't care; everything still works if we swap the groups over. The original paper

describing BLS aggregate signatures has public keys in G_2 and signatures in G_1 , while for Ethereum 2 we made the opposite choice.

The main reason for this is that we want public key aggregation to be as fast as possible. Signatures are verified much more often than they are aggregated – by far the main load on beacon chain clients currently is signature verification – and verification requires public key aggregation. So we choose to have our public keys in the faster G_1 group. This also has the benefit of reducing the size of the beacon state, since public keys are stored in validator records. If we were to use the G_2 group for public keys, the beacon state would be about 35% larger.

The trade-off is that protocol messages and beacon chain blocks are larger due to the larger signature size

Fundamentally, verification of aggregate signatures is an "on-chain" activity that we wish to be as light as possible, and signature aggregation is "off-chain" so can be more heavyweight.

Proof of possession

There is a possible attack on the BLS signature scheme that we wish to avoid, the "rogue public key" attack.

Say your public key is pk_1 , and I have a secret key, sk_2 . But instead of publishing my true public key, I publish $pk_2' = [sk_2]g_1 - pk_1$ (that is, my real public key plus the inverse of yours). I can sign a message H(m) with my secret key to make $\sigma = [sk_2]H(m)$. I then publish this claiming that it is an aggregate signature that both you and I have signed.

Now, when verifying with my rogue public key and your actual public key, the claim checks out: it looks like you signed the message when you didn't: $e(g1, \sigma) = e(g_1, [sk_2]H(m)) = e([sk_2]g_1, H(m)) = e(pk_1 + pk_2', H(m))$.

One relatively simple defence against this – the one we are using in Ethereum 2 – is to force validators to register a "proof of possession" of the secret key corresponding to their claimed public key. You see, the attacker doesn't have and cannot calculate the sk'_2 corresponding to pk'_2 . The proof of possession can be done simply by getting all validators to sign their public keys on registration, that is, when they deposit their stakes in the deposit contract. If the actual signature validates with the claimed public key then all is well.

Threshold signatures

In addition to aggregation, the BLS scheme also supports threshold signatures. This is where a secret key is divided between N validators. For a predefined value of $M \leq N$, if M of the validators sign a message then a single joint public key of all the validators can be used to verify the signature.

Threshold signatures are not currently used within the core Ethereum 2 protocol. However, they are useful at an infrastructure level. For example, for security and resilience it might be desirable to split a validator's secret key between multiple locations. If an attacker acquires fewer than M shares then the key still remains secure; if up to N-M keystores are unavailable, the validator can still sign correctly. An operational example of this is Attestant's Dirk key manager.

Threshold signatures also find a place in Distributed Validator Technology, which I will write about in a different chapter.

Batch verification

The bilinearity of the pairing function allows for some pretty funky optimisations. For example, Vitalik has formulated a method for verifying a batch of signatures simultaneously – such as all the signatures contained in a block – that significantly reduces the number of pairing operations required. Since this technique constitutes a client-side optimisation rather than being a fundamental part of the protocol, I shall describe it properly in the Implementation chapter.

Quantum security

The security (unforgeability) of BLS signatures relies on, among other things, the hardness of something called the elliptic curve discrete logarithm problem (ECDLP)⁷⁸. Basically, given the public key $[sk]g_1$ it is computationally infeasible to work out what the secret key sk is.

The ECDLP is believed to be vulnerable to attack by quantum computers, thus our signature scheme may have a limited shelf-life.

Quantum-resistant alternatives such as zkSTARKs are known, but currently not as practical as the BLS scheme. The expectation is that, at some point, we will migrate to such a scheme as a drop-in replacement for BLS signatures.

In case someone overnight unveils a sufficiently capable quantum computer, EIP-2333 (which is a standard for BLS key generation in Ethereum) describes a way to generate a hierarchy of Lamport signatures. Lamport signatures are believed to be quantum secure, but come with their own limitations. In principle, we could make an emergency switch over to these to tide us over while implementing STARKs. But this would be extremely challenging in practice.

BLS library functions

As a reference, the following are the BLS library functions used in the Ethereum 2 specification. They are named for and defined by the draft BLS Signature Standard⁷⁹. Function names link to the definitions in the standard. Since we use the proof of possession scheme defined in the standard, our Sign, Verify, and AggregateVerify functions correspond to CoreSign, CoreVerify, and CoreAggregateVerify respectively.

- def Sign(privkey: int, message: Bytes) -> BLSSignature
 - Sign a message with the validator's secret (private) key.
- def Verify(pubkey: BLSPubkey, message: Bytes, signature: BLSSignature) -> bool
 - Verify a signature given the public key and the message.
- def Aggregate(signatures: Sequence[BLSSignature]) -> BLSSignature
 - Aggregate a list of signatures.
- def FastAggregateVerify(pubkeys: Sequence[BLSPubkey], message: Bytes, signature: BLSSignature) bool
 - Verify an aggregate signature given the message and the list of public keys corresponding to the validators that contributed to the aggregate signature.
- def AggregateVerify(pubkeys: Sequence[BLSPubkey], messages: Sequence[Bytes], signature: BLSSignature) -> bool
 - This is not used in the current spec but appears in the future Proof of Custody spec. It takes n messages signed by n validators and verifies their aggregate signature. The mathematics is similar to that above, but requires n+1 pairing operations rather than just two. But this is better than the 2n pairings that would be required to verify the unaggregated signatures.
- def KeyValidate(pubkey: BLSPubkey) -> bool
 - Checks that a public key is valid. That is, it lies on the elliptic curve, it is not the group's identity point (corresponding to the zero secret key), and it is a member of the G_1 subgroup of the curve. All these checks are important to avoid certain attacks. The group membership check is quite expensive but only ever needs to be done once per public key stored in the beacon state.

⁷⁸It's puzzling to me that this is called the discrete logarithm problem when we write groups additively, rather than the discrete division problem. But it's far from being the most confusing thing about elliptic curves.

⁷⁹This document does not have the full force of an IETF standard. For one thing, it remains a draft (that is now expired), for another it is an IRTF document, meaning that it is from a research group rather than being on the IETF standards track. Some context from Brian Carpenter, former IETF chair, > I gather that you are referring to an issue in draft-irtf-cfrg-bls-signature-04. That is not even an IETF draft; it's an IRTF draft, apparently being discussed in an IRTF Research Group. So it is not even remotely under consideration to become an IETF standard...

The Eth2 spec also defines two further BLS utility functions, eth_aggregate_pubkeys() and eth_fast_aggregate_verify() that I describe in the annotated spec.

See also

The main standards that we strive to follow are the following IRTF drafts:

- BLS Signatures
- Hashing to Elliptic Curves
- Pairing-Friendly Curves

Compact Multi-Signatures for Smaller Blockchains (Boneh, Drijvers, Neven) is the original paper that described efficient BLS multi-signatures. And Pragmatic signature aggregation with BLS is Justin Drake's proposal to use these signatures in an Ethereum 2 context.

For a gentle(ish) introduction to pairings, Vitalik's Exploring Elliptic Curve Pairings is very good. If you are looking for a very deep rabbit hole to explore, Pairings for Beginners by Craig Costello is amazing.

I've written a lengthy homage to the BLS12-381 elliptic curve that also covers some BLS signature topics.

Three EIPs are intended to govern the generation and storage of keys in practice:

- EIP-2333 provides a method for deriving a tree-hierarchy of BLS12-381 keys based on an entropy seed.
- EIP-2334 defines a deterministic account hierarchy for specifying the purpose of keys.
- EIP-2335 specifies a standard keystore format for storage and interchange of BLS12-381 keys.

There are several implementations of pairings on the BLS12-381 curve around, which can be used to implement the BLS signature scheme we use:

- The Blst library is the most commonly used by Eth2 client implementers.
- The noble-bls12-381 library is better documented and may be more enjoyable if you want to try playing around with these things.

Randomness

- Assigning beacon chain duties unpredictably is an important defence against some attacks.
- The beacon chain maintains a RANDAO to accumulate randomness.
- Duties such as proposing blocks, committee assignments, and sync committee participation are assigned based on the RANDAO, with a limited lookahead period.
- Block proposers verifiably contribute randomness to the RANDAO via BLS signatures over the epoch number.
- Validators are able to bias the RANDAO to a small extent, but this is not significant problem in practice.

Introduction

An element of randomness is an important part of a permissionless blockchain protocol, both for security and for fairness.

A protocol that is fully predictable could work well in a benign environment. But we must assume that our protocols will come under attack, and predictability provides attackers with opportunities - just as the bad guys in crime thrillers often take advantage of their victims' predictable routines.

An attacker with advance knowledge of which validators will be active in different roles has a significant foothold for mounting an attack. For example, to selectively mount denial of service attacks against future proposers, or to bribe members of a particular committee, or to register especially advantageous validator numbers for themselves allowing them to take over a future committee, or simply to censor transactions.⁸⁰

To quote from a paper by Brown-Cohen et al⁸¹,

Intuitively, it is good for protocols to be unpredictable in the sense that miners do not learn that they are eligible to mine a block until shortly before it is due to be mined. Many attacks, such as double-spending, or selfish-mining, can become much more profitable if miners know in advance when they become eligible to mine.

Unpredictability, arising from randomness, is an excellent first line of defence against many attacks.

Unpredictability in proof of work comes from the process used to mine blocks. A block is valid only if it satisfies a certain condition, and the only way to satisfy that condition is through trial and error. Miners make a random guess, test it, and try again if it's not correct - this is the "work" in proof of work. Only if the guess is correct is the block valid and the miner gets to extend the chain. As I write, the difficulty of the Ethereum PoW chain is around 12.5 Peta hashes. That means that mining an Ethereum block requires 1.25×10^{16} guesses on average. This is similar to the odds of rolling 21 dice until they all come up six on the same roll. It is fabulously unlikely, yet somewhere on the Ethereum network somebody manages to do it every 13 seconds or so. Since the process is uniform – nobody is better at guessing (rolling dice) than anyone else – it provides fairness. Every Giga hash per second is equivalent to every other Giga hash per second (although there are other sources of unfairness in proof of work). And since guessing is random it provides unpredictability, which mitigates the attacks mentioned above.

Randomness⁸² in Ethereum's proof of stake protocol is used to bring unpredictability to the selection of block proposers, and to the membership of the committees that attest to blocks and sign sync data.

In this section we will look at the way that randomness is introduced into the beacon chain, some ways in which it is used, and finally some issues with the current scheme.

The RANDAO

The beacon chain design has always used a RANDAO 83 mechanism to provide its in-protocol randomness. A RANDAO is simply an accumulator that incrementally gathers randomness from contributors. So, with each block, the proposer mixes in a random contribution to the existing RANDAO value.

To unpack that a little, the beacon chain maintains a RANDAO value. Every block included in the chain contains a verifiable random value provided by the validator that proposed it, its randao_reveal. As each block is processed the beacon chain's RANDAO value is mixed with the randao_reveal from the block. Thus, over time, the RANDAO accumulates randomness from all the block proposers.

If R_n is the RANDAO value after n contributions, and r_n is the nth randao_reveal, then the following holds. Here we are mixing in the new contribution using the xor function, \oplus . Alternatives might be to use a sum or a hash, but xor is simple and has useful properties.

$$R_n = r_n \oplus R_{n-1}$$

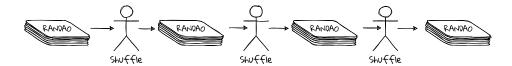
⁸⁰For a cute illustration of the perils of insufficient unpredictability, see <u>Issue 1446</u> on the specs repo: Manipulating deposit contract to gain an early majority. Hat-tip to <u>Paul Hauner</u>.

⁸¹ Formal Barriers to Longest-Chain Proof-of-Stake Protocols, Jonah Brown-Cohen, Arvind Narayanan, Christos-Alexandros Psomas, and S. Matthew Weinberg (2018). Quotation is from section 3.1.

⁸² I'm not going to distinguish the niceties of randomness and pseudo-randomness in this section. We are actually using pseudo-randomness seeded with (presumed) genuine randomness. It must be the case as it is impossible to come to consensus on genuine randomness. However, I will just call it "randomness" throughout.

⁸³ I'm not certain where the name RANDAO comes from, but it's modelled as a DAO (decentralised autonomous organisation) that deals in randomness. The Ethereum randao project from 2016 may be the origin of the name.

We can think of a RANDAO as being like a deck of cards that's passed round the table, each person shuffling it in turn: the deck gets repeatedly re-randomised. Even if one contributor's randomness is weak, the cumulative result has a high level of entropy.



We can imagine the RANDAO as a deck of cards that accumulates randomness over time as each participant shuffles the deck in turn.

Current and past RANDAO values are stored in the beacon state in the randao_mixes field. The current value is updated by process_randao with every block that the beacon chain processes. If there is no block in a slot then the RANDAO is not updated. In addition to the RANDAO's current value, EPOCHS_PER_HISTORICAL_VECTOR (minus one) past values of the RANDAO at the ends of epochs are also stored in the state. These can be used to recalculate past committee assignments, which allows historical attestations to be slashed even months later.

Source of randomness

Every block includes a field randao_reveal that is its proposer's contribution to be mixed in to the RANDAO.

This contribution needs to satisfy two properties: it should be unpredictable by any other node, yet it should be verifiable by all nodes.

"Verifiable" means that, although random (read pseudo-random), the RANDAO contribution value must not be arbitrary. The proposer must not be able to pick and choose its contribution, otherwise it will just choose a value that gives itself some sort of advantage. There must be a single valid contribution that the proposer can make in any given block, and all the other nodes must be able to verify that contribution.

The old: hash onions

Early ideas for verifiable randomness had each validator pre-committing to a "hash onion". Before joining the beacon chain a validator would generate a random number. When registering its initial deposit the validator would include the result of repeatedly cryptographically hashing that number a large number (thousands) of times as a commitment. Then when proposing a block the randao_reveal would be the pre-image of that commitment: one layer would be "peeled off the onion". Since a cryptographic hash is not invertible, only the proposer could calculate this value, but it's easily verifiable by everyone. Then the reveal gets stored as the new commitment and so on.

This scheme is viable, but has complexities and edge cases – for example, if a block gets orphaned, everybody (except the beacon chain) can now see the proposer's reveal – that make it clunky to implement in practice.

The new: BLS signatures

An alternative to the hash onion became available when we moved to using BLS signatures in the protocol. With the BLS scheme every validator already has a closely guarded random value: the secret key that it uses for signing blocks and attestations. As far as anyone knows the signatures produced are uniformly random.

The signature for an agreed message nicely satisfies our two desired properties for the RANDAO contribution. It is unpredictable to the other validators since they do not know the proposer's private key, but it is easily verifiable since all validators know the proposer's public key.

The elegance and simplicity of reusing the BLS key infrastructure for the RANDAO makes it a considerable improvement on the original hash onion design.

There is a further nice benefit to using BLS signatures that may not be obvious. The aggregation property of the signatures allows the contribution to be derived via a multi-party computation. That is, signatures from multiple validators can be combined into a threshold signature so that they can effectively act as a single validator. We do not use this property within the core Eth2 protocol, but it enables Distributed Validator Technology, which would be very difficult with the old hash onion approach.

For all these reasons, we now use a BLS signature as the entropy contribution to the RANDAO, that is, the randao_reveal.

Where does the entropy come from?

Evidently the predominant source of randomness in the Ethereum 2 protocol is the secret keys of the validators. If every validator key is generated uniformly randomly and independently then each contributes 256 bits of entropy to the overall pool. However, keys are sometimes not independently generated EIP-2333 provides a way to derive multiple validator keys from a single entropy seed, and large stakers are likely to have done this. Thus, the total entropy from N validator keys will be less than $N \times 256$ bits, but we don't know how much less.

Some other sources of entropy for the RANDAO are noted in EIP-4399.

- Missed or orphaned block proposals directly affect the RANDAO's output. Network conditions, node faults, or maintenance downtime can all lead to missed block proposals that have a degree of randomness.
- The total number of active validators in an epoch affects the selection of proposers which in turn affects participation in the RANDAO. Thus, deposits and exits (both voluntary and forced) contribute entropy.
- A validator's effective balance affects its likelihood of being selected to propose a block. Thus, changes in effective balances (perhaps due to one or more validators being offline for a period of time) add entropy.

Updating the RANDAO

When a validator proposes a block, it includes a field randao_reveal which has BLSSignature type. This is the proposer's signature over the epoch number, using its normal signing secret key.

The randao_reveal is computed by the proposer as follows, the privkey input being the validator's random secret key.

```
def get_epoch_signature(state: BeaconState, block: BeaconBlock, privkey: int) -> BLSSignature:
    domain = get_domain(state, DOMAIN_RANDAO, compute_epoch_at_slot(block.slot))
    signing_root = compute_signing_root(compute_epoch_at_slot(block.slot), domain)
    return bls.Sign(privkey, signing_root)
```

When a block is processed, the randao_reveal is mixed into the RANDAO like this:

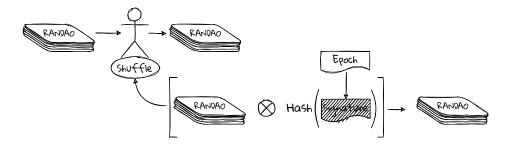
```
def process_randao(state: BeaconState, body: BeaconBlockBody) -> None:
    epoch = get_current_epoch(state)
# Verify RANDAO reveal
proposer = state.validators[get_beacon_proposer_index(state)]
signing_root = compute_signing_root(epoch, get_domain(state, DOMAIN_RANDAO))
assert bls.Verify(proposer.pubkey, signing_root, body.randao_reveal)
# Mix in RANDAO reveal
mix = xor(get_randao_mix(state, epoch), hash(body.randao_reveal))
state.randao_mixes[epoch % EPOCHS_PER_HISTORICAL_VECTOR] = mix
```

Two things are going on in the processing of the randao_reveal signature.

First, the signature is verified using the proposer's public key before being mixed in. This means that the proposer has almost no choice about what it contributes to the RANDAO: it either contributes a single verifiable value – the correct signature over the epoch number – or it withholds its block and contributes nothing. (Equivalently, a block with an incorrect reveal is invalid.)

⁸⁴I am indebted to Vasiliy Shapovalov for reminding me of this.

Second, the hash of the signature is mixed in to the beacon state's RANDAO using an xor operation. We apply the hash operation to reduce the length of the RANDAO accumulator from about 762 bits – the length of a compressed BLS signature, an inconvenient number of bits to work with – to 256 bits. The uniformity of the output of hash functions is also better established than that of BLS signatures.



What's really happening when the RANDAO is shuffled. The signature over the epoch number is the RANDAO reveal that the proposer includes in its block. This is hashed then mixed in to the existing RANDAO with an xor operation.

We could have mixed in the reveal by hashing it directly with the RANDAO accumulator, however we choose to mix it in via an xor operation. The combination of using the epoch number as the signed quantity and using xor to mix it in leads to a subtle, albeit tiny, improvement in attack-resistance of the RANDAO. Justin Drake explains in his notes:

Using xor in process_randao is (slightly) more secure than using hash. To illustrate why, imagine an attacker can grind randomness in the current epoch such that two of his validators are the last proposers, in a different order, in two resulting samplings of the next epochs. The commutativity of xor makes those two samplings equivalent, hence reducing the attacker's grinding opportunity for the next epoch versus hash (which is not commutative). The strict security improvement may simplify the derivation of RANDAO security formal lower bounds.

We will see shortly that it can be advantageous to an attacker to have control of the last slots of an epoch. Justin's point is that, under the current scheme, the attacker having validators V_0, V_1 in the two last slots of an epoch is equivalent to it having V_1, V_0 with respect to the randao_reveals. This fractionally reduces an attacker's choices when it comes to influencing the RANDAO. If we used hash rather than xor, or if we signed over the slot number rather than the epoch number, these orderings would result in different outcomes from each other, giving an attacker more choice and therefore more power.

Lookahead

We started this section with a discussion of unpredictability. Ideally, it should not be possible to predict the duties for any block proposer or committee member until the moment they become active. However, in practice, proposers and committee members need a little advance notice of their duties to allow them to join the right p2p network subnets and do whatever other preparation they need to do.

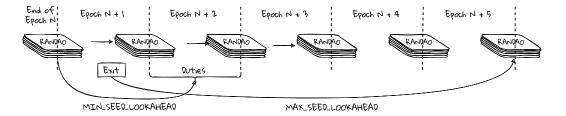
The RANDAO seed at the end of epoch N is used to compute validator duties for the whole of epoch N+2. This interval is controlled by MIN_SEED_LOOKAHEAD via the get_seed() function. Thus, validators have at least one full epoch to prepare themselves for any duties, but no more than two.

Under normal circumstances, then, an attacker is not able to predict the duty assignments more than two epochs in advance. However, if an attacker has a large proportion of the stake or is, for example, able to mount a DoS attack against block proposers for a while, then it might be possible for the attacker to predict the output of the RANDAO further ahead than MIN_SEED_LOOKAHEAD would normally allow. The attacker might then use this foreknowledge to strategically exit validators or make deposits⁸⁵ in order to gain control of a committee, or a large number of block proposal slots.

It's certainly not an easy attack. Nonetheless, it is easy to defend against, so we might as well do so.

⁸⁵ In the current protocol you'd need to predict the RANDAO for around 16 hours ahead for deposits to be useful in manipulating it, due to ETH1_FOLLOW_DISTANCE and EPOCHS_PER_ETH1_VOTING_PERIOD. However, at some point post-Merge, it may become possible to onboard deposits more-or-less immediately.

To prevent this, we assume a maximum feasible lookahead that an attacker might achieve, MAX_SEED_LOOKAHEAD and delay all activations and exits by this amount, which allows time for new randomness to come in via block proposals from honest validators, making irrelevant any manipulation by the entering or exiting validators. With MAX_SEED_LOOKAHEAD set to 4, if only 10% of validators are online and honest, then the chance that an attacker can succeed in forecasting the seed beyond (MAX_SEED_LOOKAHEAD - MIN SEED LOOKAHEAD) = 3 epochs is $0.9^{3\times32}$, which is about 1 in 25,000.



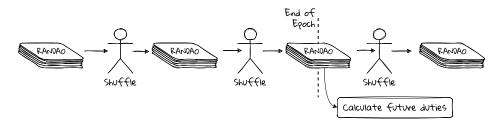
The RANDAO value at the end of epoch N is used to set duties for epoch N+2, which is controlled by MIN_SEED_LOOKAHEAD. A validator exiting in epoch N+1 remains active until at least the end of epoch N+5 (depending on the exit queue). This is controlled by MAX_SEED_LOOKAHEAD.

Single Secret Leader Election

As currently implemented, both the minimum and maximum lookaheads smell a little of engineering hackery. In a perfect design only the block proposer would know ahead of time that it has been chosen to propose in that slot. Once its block is revealed then the rest of the network would be able to verify that, yes, this was indeed the chosen proposer. This feature is called Single Secret Leader Election. We do not yet have it in the Ethereum protocol, and I shall write about it elsewhere. Meanwhile, some good progress is being made towards making it practical.

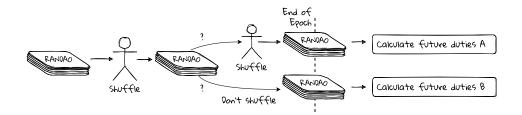
RANDAO biasability

The RANDAO value for an epoch is set at the end of the previous epoch, and duty assignments for the entire epoch (proposals and committee memberships) depend on that value. (Actually – due to MIN_SEED_LOOKAHEAD – on the RANDAO value at the end of the last-but-one epoch, but we'll overlook that in what follows.)



Future duty assignments for validators – block proposers, committee members, sync committee duty – are calculated based on the state of the RANDAO at the end of each epoch.

Thus, when a validator happens to be assigned to propose a block in the last slot of an epoch, it gains a small amount of control over the assignments for the next epoch. This is because it can choose to reveal its block, which mixes in its RANDAO reveal, or it can choose (at a cost) to withhold its block and keep the existing RANDAO value, knowing that there will be no subsequent RANDAO change before duties are calculated. In this way, a validator is able to exert a little influence over the proposer and committee assignments in the next epoch. This is called "one bit of influence" over the RANDAO as the validator has a choice of two outcomes.



The last proposer in an epoch has a choice. It can propose its block as usual, updating the RANDAO, resulting in a set of duty assignments A. Or it can withhold its block, leaving the RANDAO as-is, resulting in a set of duty assignments B. If outcome B gives the owner of the validator sufficient advantage to compensate for having missed a proposal, then it is an opportunity to "cheat".

If an attacker gets a string of proposals at the end of an epoch then it has more power. Having k consecutive proposals at the end of an epoch gives the attacker 2^k choices for the ultimate value of the RANDAO that will be used to compute future validator duties. In this scenario the attacker has "k bits of influence" over the RANDAO.

Biasability analyses

This section is fully optional. I got a bit carried away with the maths; it's fine to skip to the next section.

To make discussion of RANDAO biasability more concrete I shall try to quantify what it means in practice with a couple of examples. In each case the entity "cheating" or "attacking" has control over a proportion of the stake r, either directly or through some sort of collusion, and we will assume that the remaining validators are all acting independently and correctly. We will also assume, of course, that individual randao_reveals are uniformly random.

In the first example, I will try to gain control of the RANDAO by permanently acquiring proposals in the last slots of an epoch. In the second example I will try to improve my expected number of block proposals by biasing the RANDAO when I get the opportunity to do so. In both cases I will be selectively making and withholding proposals having computed the best outcome: a process of "grinding" the RANDAO.

These examples are intended only as illustrations. They are not academic studies, and there are lots of loose ends. It's very likely I've messed something up: probability is *hard*. I'd be very interested if anyone wanted to make them more rigorous and complete. Some related work, more simulation based, was previously done by Runtime Verification.

RANDAO takeover

If I control a proportion r of the total stake, how much can I boost my influence over the protocol by manipulating the RANDAO?

The ability to influence the RANDAO depends on controlling a consecutive string of block proposals at the end of an epoch. We shall call this property "having a tail", and the tail will have a length k from 0 to a maximum of 32, an entire epoch.

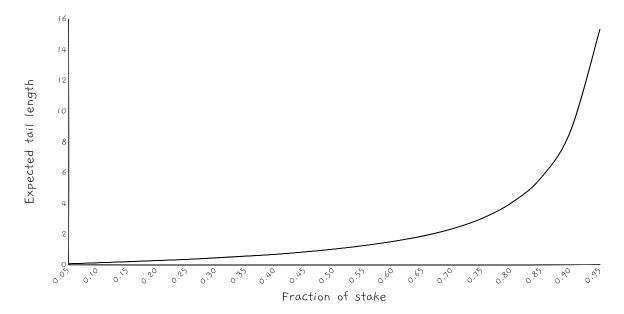
Our question can be framed like this: if I have a tail of length k in one epoch, what is my expected length of tail in the next epoch? With a tail of length k I have 2^k opportunities to reshuffle the RANDAO by selectively making or withholding block proposals. Can I grind through the possibilities to increase my tail length next time, and eventually take over the whole epoch?

In the absence of any manipulation, my probability of having a tail of length exactly k in any given epoch is $(1-r)r^k$ for k < 32, and r^{32} when k = 32. This is the chance that I make k proposals in the tail positions preceded by a proposal that I did not make.

$$q_k = \begin{cases} (1-r)r^k & 0 \le k < 32 \\ r^k & k = 32 \end{cases}$$

So the expected tail length for someone controlling a proportion r of the stake is,

$$E(r) = \sum_{n=1}^{32} nq_n = \sum_{n=1}^{31} n(1-r)r^n + 32r^{32}$$



The bottom axis is r, and the side axis is my expected proposals tail length E(r) assuming no RANDAO manipulation.

Now we will calculate $E^{(k)}(r)$, the expected length of tail I can achieve in the next epoch by using my previous tail of length k to grind the options.

Consider the case where I have a tail of length k=1 in some epoch. This gives me two options: I can publish my RANDAO contribution, or I can withhold my RANDAO contribution (by withholding my block). My strategy is to choose the longest tail for the next epoch that I can gain via either of these options.

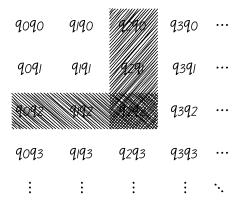
The probability, $p_j^{(1)}$, of gaining a tail of exactly length j as a result of having a tail of length 1 is,

$$p_j^{(1)} = 2\sum_{i=0}^{j-1} q_j q_i + q_j q_j = q_j \left(2\sum_{i=0}^{j-1} q_i + q_j\right)$$

We can think about this as follows. With k=1 we get two attempts, therefore q appears twice in each product. To calculate $p_j^{(1)}$ we need the sum over the all the combinations of the probability of getting a tail of length exactly j (that is, q_j) multiplied by the probability of getting a tail of j or less (that is, not getting a tail longer than j, otherwise we would have chosen that length instead of j).

Visually, calculating $p_2^{(1)}$ looks like the sum of the values in the shaded area of the next diagram.

This example with tail length k=1 results in a two-dimensional square since we have two possibilities to try. One way to calculate $p_j^{(1)}$ is to take the difference between the sum of all the products in the square side j+1 and the sum of all the products in the square side j.



The probability that we get a maximum tail length of exactly two with two attempts is the sum of the terms in the shaded areas. Despite the overlap, each term is included only once.

Thinking of it like this helps us to generalise to the cases when k > 1. In those cases we are dealing with a hyper-cube of dimension 2^k ; each element is the product of 2^k values of q. To calculate $p_j^{(k)}$ we can find the difference between the sum of all the products in the 2^k -dimensional cube side j + 1 and the sum of all the products in the 2^k -dimensional cube side j. This is tedious to write down and involves a mind-boggling number of calculations even for quite small k, but see my example code for an efficient a way to calculate it.

Now, finally, we can calculate the expected tail length in the next epoch given that we have a tail of length k in this epoch.

$$E^{(k)}(r) = \sum_{n=1}^{32} n p_n^{(k)}$$

Graphing this for various values of k we get the following. Note that the solid, k = 0, line is the same as E(r) above - the expected tail with no manipulation. That is, $E^{(0)}(r) = E(r)$ as you'd expect.

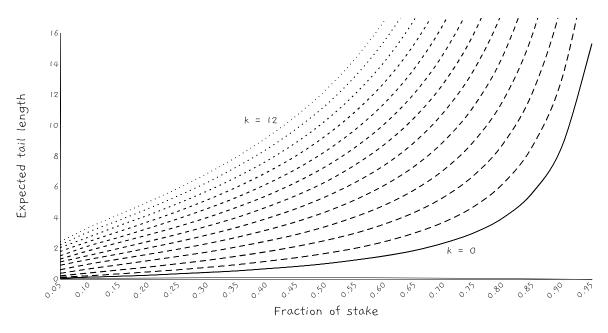
We see that, if I end up with any length of tail in an epoch, I can always grind my RANDAO contributions to improve my expected length of tail in the next epoch when compared with not grinding the RANDAO. And the longer the tail I have, the better the tail I can expect to have in the next epoch. These results are not surprising.

The important question is, under what circumstances can I use this ability in order to indefinitely increase my expected tail length, so that I can eventually gain full control of the RANDAO?

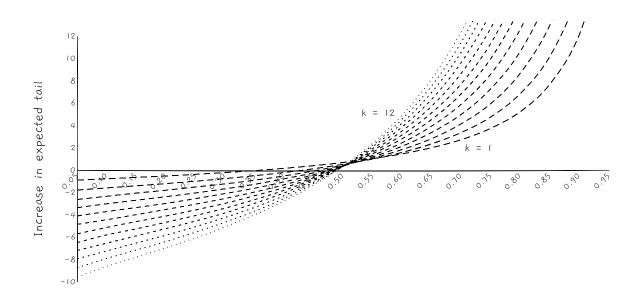
To investigate this, consider the following graph. Here, for each k line we have plotted $E^{(k)}(r) - k$. This allows us to see whether our expected tail in the next epoch is greater or less than our current tail. If $E^{(k)}(r) - k$ is negative then I can expect to have fewer proposals in the next epoch than I have in this one.

We can see that for r less than around 0.5, especially as k grows, we expect our tail length to shrink rather than grow, despite our best RANDAO grinding efforts. However, for r greater than 0.5, we expect our tail length to grow as a result of our grinding, whatever tail length we start with.

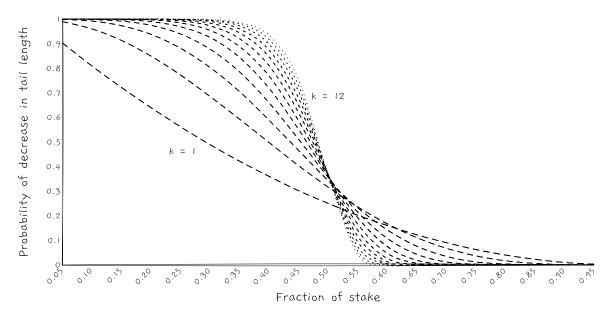
For completeness, we shouldn't only look at expectations, but also at probabilities. The following graph shows the probability that if I have a tail of length k then I will have a tail of length less than k in the next epoch. As k increases you can see that a step function is forming: for a proportion of stake less than about 50% it becomes practically certain that my tail will decrease in length from one epoch to the next despite my best efforts to grow it; conversely, for a proportion of stake greater than a little over 50% it becomes practically certain that I can maintain or grow my tail of block proposals.



The bottom axis is r, and the side axis is my subsequent expected proposals tail length, $E^{(k)}(r)$ given various values of tail length k that I can play with. Note that $E^{(0)}(r) = E(r)$ from the graph above.



The bottom axis is r, and the side axis is my subsequent expected proposals tail length minus my current tail length, $E^{(k)}(r) - k$ for various values of k.



The bottom axis is r, and the side axis is the probability that my best tail length in the next epoch is less than my current tail length for various values of tail length k.

Discussion of RANDAO takeover

What can we conclude from this? If I control less than about half the stake, then I cannot expect to be able to climb the ladder of increasing tail length: with high probability the length of tail I have will decrease rather than increase. Whereas, if I have more than half the stake, my expected length of tail increases each epoch, so I am likely to be able to eventually take over the RANDAO completely. With high enough r, the 2^k options I have for grinding the RANDAO overwhelm the probability of losing tail proposals. For large values of k it will not be practical to grind through all these options. However, we need to arrive at only one good combination in order to succeed, so we might not need to do the full calculation.

The good news is that, if attackers control more than half the stake, they have more interesting attacks available, such as taking over the LMD fork choice rule. So we generally assume in the protocol that any attacker has less than half the stake, in which case the RANDAO takeover attack appears to be infeasible.

As a final observation, we have ignored cases where two or more of the tail proposals are from the same validator. As discussed above, these proposals would each result in the same RANDAO contribution and reduce my grinding options. However, with a large number of validators in the system this is a reasonable approximation to make.

Code for calculating the length of tail with cheating

Here is the code for generating the data for the graphs above. The length of tail goes up to k = 12. Feel free to increase that, although it gets quite compute intensive. Twelve is enough to see the general picture.

```
def prob_tail_eq(r, k):
    return (1 - r) * r**k if k < N else r**k

# The sum of the products of all the q_i in the hypercube of side j and dim k
# Recursive is cooler, but written iteratively so that python doesn't run out of stack
def hyper(q, j, k):
    h = 1
    for n in range(1, k + 1):
        h = sum([q[i] * h for i in range(j)])
    return h</pre>
```

```
# Smoke test.
assert abs(hyper([0.9, 0.09, 0.009, 0.0009, 0.00009, 0.00001], 6, 32) - 1.0) < 1e-12
    = 32 # The number of slots per epoch
KMAX = 12 # The maximum length of prior tail we will consider
NINT = 20 \# The number of intervals of r between 0 and 1 to generate
expected = [[] for i in range(KMAX + 1)]
prob_dec = [[] for i in range(KMAX + 1)]
rs = [i / NINT for i in range(1, NINT)]
for r in rs:
   # q[j] = the probability of having a tail of exactly j in one attempt
    q = [prob tail eq(r, j) for j in range(N + 1)]
    for k in range(KMAX + 1):
        h = [hyper(q, j, 2**k) for j in range(N + 2)]
        \# p[j] = the probability that with a tail of k I can achieve a tail of j in the next epoch
        p = [h[j + 1] - h[j] \text{ for } j \text{ in } range(N + 1)]
        # The expected length of tail in the next epoch given r and k
        expected[k].append(sum([j * p[j] for j in range(N + 1)]))
        \# The probability of a decrease in tail length to < k
        prob_dec[k].append(h[k])
print(rs)
print(expected)
print(prob_dec)
```

Block proposals boost

For the second worked example I will try to improve the overall number of proposals that I get among my validators. Unlike in the first example, I will not be trying to maximise my advantage at any cost. I will only manipulate the RANDAO when I can do so without any net cost to myself.

Once again, I control a proportion r of the stake. I will only be considering tails of length zero or of length one - going beyond that gets quite messy, and my intuition is that for values of r less than a half or so it will make little difference.

Let q_j be my probability of getting exactly j proposals in an epoch without any manipulation of the RANDAO (different from the q in the first example, but related):

$$q_j = r^j (1-r)^{32-j} {32 \choose j}$$

My expected number of proposals per epoch when acting honestly is simple to compute,

$$E = \sum_{n=1}^{32} nq_n = 32r$$

Now I will try to bias the RANDAO to give myself more proposals whenever I have the last slot of an epoch, which will happen with probability r. Doing this, my expected number of proposals in the next epoch is as follows. The prime is to show that I am trying to maximise my advantage (cheat), and the subscript is to show that we are looking one epoch ahead.

$$E_1' = \sum_{n=1}^{32} n((1-r)q_n + rp_n)$$

Unpacking this, the first term in the addition is the probability, 1-r, that I did not have the last slot in the previous epoch (so I cannot do any biasing) combined with the usual probability q_n of having n proposals in an epoch.

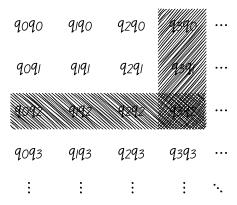
The second term is the probability, r, that I did have the last slot in the previous epoch combined with the probability p_n that I get either n proposals by proposing my block, or n+1 proposals by withholding my block. We need the plus one to make up for the block I would be withholding at the end of the previous epoch in order to get this outcome.

$$p_j = \begin{cases} \sum_{i=0}^j q_i (q_j + q_{j+1}) & 0 \le j < 32 \\ \sum_{i=0}^j q_i q_i & j = 32 \end{cases}$$

As before, we can illustrate this by considering the matrix of probabilities. With a tail of one I have two choices: to propose or to withhold. To achieve a net number of exactly j proposals we are looking for the combinations where either of the following holds.

- 1. Proposing gives me exactly j proposals and withholding gives no more than j+1 (that is, $\sum_{i=0}^{j+1} q_i q_j$). These are the elements in the horizontal bar in the diagram below.
- 2. Proposing gives me no more than j proposals and withholding gives me exactly j+1 (that is, $\sum_{i=0}^{j} q_{j+1}q_{i}$).⁸⁶ These are the elements in the vertical bar in the diagram below.

Note that the $q_{i+1}q_i$ element appears in both outcomes, but must be included only once.



The probability that we get a net number of exactly two proposals with two attempts is the sum of the terms in the shaded areas. Despite the overlap, each term is included only once.

We can iterate this epoch by epoch to calculate the maximum long-term improvement in my expected number of proposals. The probability that I gain the last slot of epoch N is $E'_N/32$.

$$E_{N+1}' = \sum_{n=1}^{32} n \left((1 - \frac{E_N'}{32}) q_n + \frac{E_N'}{32} p_n \right)$$

The maximum percentage gain in block proposals that I can acquire is shown in the following graph.

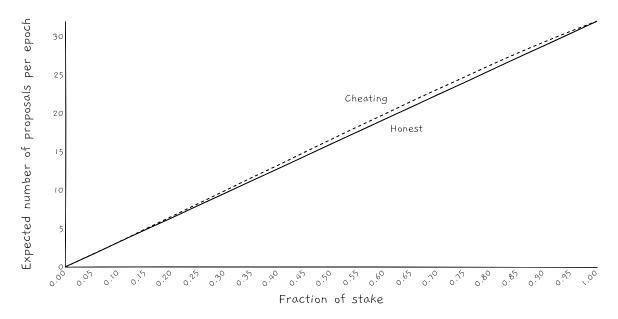
Code for calculating the expected number of proposals with cheating

The following Python code calculates E'_N to convergence.

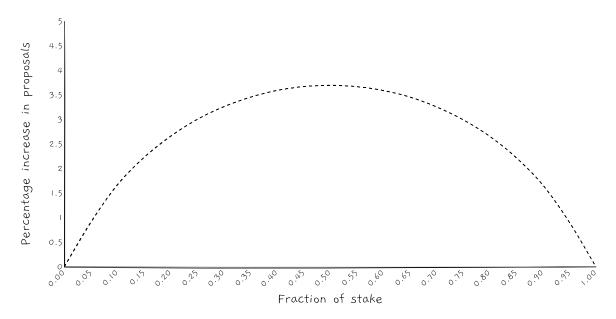
```
def fac(n):
    return n * fac(n - 1) if n else 1

def choose(n, k):
    return fac(n) / fac(k) / fac(n - k)
```

 $^{^{86}}$ You can see why I am restricting this example to tails of length just zero or one: I don't want to think about what this looks like in a 2^k dimensional space.



The solid line is E, the expected number of block proposals per epoch for a proportion of the stake that does not seek to bias the RANDAO. The dashed line is E', the long-term expected number of block proposals per epoch for a proportion of the stake that coordinates to bias the RANDAO in its favour.



The long-term percentage increase in the expected number of proposals per epoch that can be gained by a proportion of the stake coordinating to bias the RANDAO. An entity with 25% of the stake can gain an extra 2.99% of proposals (8.24 per epoch rather than exactly 8), assuming that the remaining stakers are uncoordinated.

```
def prob(n, k, r):
    return r**k * (1 - r)**(n - k) * choose(n, k)

nintervals = 20
for idx in range(1, nintervals + 1):
    r = r0 = idx / nintervals
    q = [prob(32, j, r0) for j in range(33)]

p = []
    for j in range(33):
        p.append(sum([q[i] * q[j] + (q[j + 1] * q[i] if (j < 32) else 0) for i in range(j + 1)]))

# Iterate to convergence
e = 0
while (e == 0 or abs(e - e_old) > 0.000001):
        e_old = e
        e = sum([i * (q[i] * (1 - r) + p[i] * r) for i in range(33)])
        r = e / 32

print(r0, r0 * 32, e, 100 * (e / (r0 * 32) - 1))
```

Discussion of proposals boost

In the above analysis we considered only the effect of using the last slot of an epoch to bias the RANDAO and saw that an entity with any amount of stake can fractionally improve its overall expected number of block proposals, assuming that everyone else is acting honestly.

The expected gain may be higher if we consider using the two last slots, or the k last slots, especially if combined with the previous tail-extension attack. But I expect that for r less than a half or so any further improvement will be very small.

Verifiable delay functions

We've seen that, although the RANDAO is biasable, it is not so biasable as to break the protocol: for our purposes the randomness is "good enough".

Nonetheless, it is interesting to explore how it might be improved, especially as, with The Merge, the RANDAO value is now available to Ethereum's smart contract layer. Randomness biasability in a large lottery contract, for example, could be more of a problem than biasability in the consensus protocol.

The long-term fix for biasability is to use a verifiable delay function (VDF). A VDF is guaranteed to be slow to compute its output, but that output can be verified quickly. In practice the VDF is a calculation run on a specialised hardware device that is assumed to have a performance within a small factor of the theoretical maximum performance. So, a VDF might output a result in, say, 20 seconds with the assumption that the best that any other device could do is to obtain the result in, say, 5 seconds.

The idea is that RANDAO updates would come from the output of the VDF. A proposer would have to decide whether to commit its randao_reveal before it is possible for it to compute the actual contribution: the future output of the VDF. This eliminates any opportunistic biasing of the RANDAO.

Only one VDF needs to be active at any time on the network since it can publish its result for quick verification by all the other nodes.

Although a lot of work has been done on designing and specifying VDFs there is no active plan to implement one in Ethereum at this time. If anything, recent results on the difficulty of constructing VDF functions suggest that the prospect of an in-protocol VDF is receding at this time.

See also

Vitalik has some notes on randomness in his Annotated Ethereum 2.0 Spec. His article Validator Ordering and Randomness in PoS summarises some early thinking on the options for random validator selection

in proof of stake⁸⁷.

On RANDAO biasability, Runtime Verification did an analysis in 2018 that both complements and goes deeper than the sketches I presented in this section. There is both a statistical model and a thorough write-up of their work.

A search for RANDAO on ethresear.ch yields quite a few articles discussing various issues with it, and proposing some solutions (none of which we have adopted).

A good place to start exploring verifiable delay functions is the VDF Alliance site.

Shuffling

- Shuffling is used to randomly assign validators to committees and choose block proposers.
- Ethereum 2 uses a "swap-or-not" shuffle.
- Swap-or-not is an oblivious shuffle: it can be applied to single list elements and subsets.
- This makes it ideal for supporting light clients.

Introduction

Shuffling is used to randomly assign validators to committees, both attestation committees and sync committees. It is also used to select the block proposer at each slot.

Although there are pitfalls to be aware of, shuffling is a well understood problem in computer science. The gold standard is probably the Fisher–Yates shuffle. So why aren't we using that for Eth2? In short: light clients.

Other shuffles rely on processing the entire list of elements to find the final ordering. We wish to spare light clients this burden. Ideally, they should deal with only the subsets of lists that they are interested in. Therefore, rather than Fisher–Yates, we are using a construction called a "swap-or-not" shuffle. The swap-or-not shuffle can tell you the destination index (or, conversely, the origin index) of a single list element, so is ideal when dealing with subsets of the whole validator set.

For example, formally committees are assigned by shuffling the full validator list and then taking contiguous slices of the resulting permutation. If I only need to know the members of committee k, then this is very inefficient. Instead, I can run the swap-or-not shuffle backwards for only the indices in slice k to find out which of the whole set of validators would be shuffled into k. This is much more efficient.

Swap-or-not Specification

The algorithm for shuffling in the specification deals with only a single index at a time.

```
def compute_shuffled_index(index: uint64, index_count: uint64, seed: Bytes32) -> uint64:
    """
    Return the shuffled index corresponding to ``seed`` (and ``index_count``).
    """
    assert index < index_count

# Swap or not (https://link.springer.com/content/pdf/10.1007%2F978-3-642-32009-5_1.pdf)
# See the 'generalized domain' algorithm on page 3</pre>
```

 $^{^{87}}$ This article seems only to be available now on the Internet Archive. I am grateful to Patrick McCorry for tracking it down.

```
for current_round in range(SHUFFLE_ROUND_COUNT):
    pivot = bytes_to_uint64(hash(seed + uint_to_bytes(uint8(current_round)))[0:8]) % index_count
    flip = (pivot + index_count - index) % index_count
    position = max(index, flip)
    source = hash(
        seed
            + uint_to_bytes(uint8(current_round))
            + uint_to_bytes(uint32(position // 256))
    )
    byte = uint8(source[(position % 256) // 8])
    bit = (byte >> (position % 8)) % 2
    index = flip if bit else index
```

An index position in the list to be shuffled, index, is provided, along with the total number of indices, index_count, and a seed value. The output is the index that the initial index gets shuffled to.

The hash functions used to calculate pivot and source are deterministic, and are used to generate pseudorandom output from the inputs: given the same input, they will generate the same output. So we can see that, for given values of index, index_count, and seed, the routine will always return the same output.

The shuffling proceeds in rounds. In each round, a pivot index is pseudo-randomly chosen somewhere in the list, based only on the seed value and the round number.

Next, an index flip is found, which is pivot - index, after accounting for wrap-around due to the modulo function. The important points are that, given pivot, every index maps to a unique flip, and that the calculation is symmetrical, so that flip maps to index.

- With index_count = 100, pivot = 70, index = 45, we get flip = 25.
- With index count = 100, pivot = 70, index = 82, we get flip = 88.

As the last step in the round, a decision is made whether to keep the index as-is, or to update it to flip. This decision is pseudo-randomly made based on the values of seed, the round number, and the higher of index and flip.

Note that basing the swap-or-not decision on the higher of index and flip brings a symmetry to the algorithm. Whether we are considering the element at index or the element at flip, the decision whether to swap the elements or not will be the same. This is the key to seeing the that full algorithm delivers a shuffling (permutation) of the original set.

The algorithm proceeds with the next iteration based on the updated index.

It may not be immediately obvious, but since we are deterministically calculating flip based only on the round number, the shuffle can be run in reverse simply by running from SHUFFLE_ROUND_COUNT - 1 to 0. The same swap-or-not decisions will be made in reverse. As described above, this reverse shuffle is perfect for finding which validators ended up in a particular committee.

A full shuffle

To get an intuition for how this single-index shuffle can deliver a full shuffling of a list of indices, we can consider how the algorithm is typically implemented in clients when shuffling an entire list at once.

As an optimisation, the loop over the indices to be shuffled is brought inside the loop over rounds. This hugely reduces the amount of hashing required since the pivot is fixed for the round (it does not depend on the index) and the bits of source can be reused for 256 consecutive indices, since the hash has a 256-bit output.

For each round, we do the following.

1. Choose a pivot and find the first mirror index

First, we pick a pivot index p. This is pseudo-randomly chosen, based on the round number and some other seed data. The pivot is fixed for the rest of the round.

With this pivot, we then pick the mirror index m_1 halfway between p and 0. That is, $m_1 = p/2$. (We will simplify by ignoring off-by-one rounding issues for the purposes of this explanation.)



The pivot and the first mirror index.

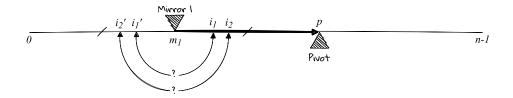
2. Traverse first mirror to pivot, swapping or not

For each index between the mirror index m_1 and the pivot index p, we decide whether we are going to swap the element or not.

Consider the element at index i. If we choose not to swap it, we just move on to consider the next index.

If we do decide to swap, then we exchange the list element at i with that at i', its image in the mirror index. That is, i is swapped with $i' = m_1 - (i - m_1)$, so that i and i' are equidistant from m_1 . In practice, we don't exchange the elements at this point, we just update the indices $i \to i'$, and $i' \to i$.

We make the same swap-or-not decision for each index between m_1 and p.

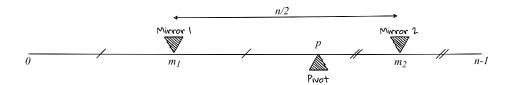


Swapping or not from the first mirror up to the pivot.

The decision whether to swap or not is based on hashing together the random seed, the round number, and some position data. A single bit is extracted from this hash for each index, and the swap is made or not according to whether this bit is one or zero.

3. Calculate the second mirror index

After considering all the indices i from m_1 to p, mirroring in m_1 , we now find a second mirror index at m_2 , which is the point equidistant between p and the end of the list: $m_2 = m_1 + n/2$.



The second mirror index.

4. Traverse pivot to second mirror, swapping or not

Finally, we repeat the swap-or-not process, considering all the points j from the pivot, p to the second mirror m_2 . If we choose not to swap, we just move on. If we choose to swap then we exchange the element at j with its image at j' in the mirror index m_2 . Here, $j' = m_2 + (m_2 - j)$.

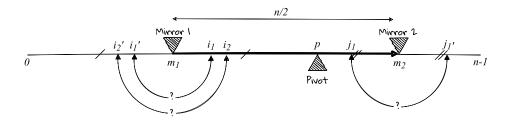


Swapping or not from the pivot to the second mirror.

Putting it all together

At the end of the round, we have considered all the indices between m_1 and m_2 , which, by construction, is half of the total indices. For each index considered, we have either left the element in place, or swapped the element at a distinct index in the other half. Thus, all the indices have been considered exactly once for swapping.

The next round begins by incrementing (or decrementing for a reverse shuffle) the round number, which gives us a new pivot index, and off we go again.



The whole process running from one mirror to the other in a single round.

Discussion

A key insight

When deciding whether to swap or not for each index, the algorithm cleverly bases its decision on the higher of the candidate index or its image in the mirror. That is, i rather than i' (when below the pivot), and j' rather than j (when above the pivot). This means that we have flexibility when running through the indices of the list: we could do 0 to m_1 and p to m_2 as two separate loops, or do it with a single loop from m_1 to m_2 as I outlined above. The result will be the same: it doesn't matter if we are considering i or its image i'; the decision whether to swap or not has the same outcome.

The number of rounds

In Ethereum 2.0 we do 90 rounds of the algorithm per shuffle, set by the constant SHUFFLE_ROUND_COUNT. The original paper on which this technique is based suggests that $6 \lg N$ rounds is required "to start to see a good bound on CCA-security", where N is the list length. In his annotated spec Vitalik says "Expert cryptographer advice told us $\sim 4 \log_2 N$ is sufficient for safety". The absolute maximum number of validators in Eth2, and hence the maximum size of the list we would ever need to shuffle, is about 2^{22} (4.2 million). On Vitalik's estimate that gives us 88 rounds required, on the paper's estimate, 92 rounds (assuming that \log is the natural \log in the right ballpark, especially as we are very, very unlikely to end up with that many active validators.

It might be interesting to make the number of rounds adaptive based on list length. But we don't do that; it's probably an optimisation too far.

Fun fact: when Least Authority audited the beacon chain specification, they initially found bias in the shuffling used for selecting block proposers (see Issue F in their report). This turned out to be due to mistakenly using a configuration that had only 10 rounds of shuffling. When they increased it to the 90 we use for mainnet, the bias no longer appeared.

(Pseudo) randomness

The algorithm requires that we select a pivot point randomly in each round, and randomly choose whether to swap each element or not in each round.

In Eth2, we deterministically generate the "randomness" from a seed value, such that the same seed will always generate the same shuffling.

The pivot index is generated from eight bytes of a SHA256 hash of the seed concatenated with the round number, so it usually changes each round.

The decision bits used to determine whether to swap elements are bits drawn from SHA256 hashes of the seed, the round number, and the index of the element within the list.

Efficiency

This shuffling algorithm is much slower than Fisher–Yates. That algorithm requires N swaps. Our algorithm will require 90N/4 swaps on average to shuffle N elements.

We should also consider the generation of pseudo-randomness, which is the most expensive part of the algorithm. Fisher–Yates needs something like $N\log_2 N$ bits of randomness, and we need $90(\log_2 N + N/2)$ bits, which, for the range of N we need in Eth2, is many more bits (about twice as many when N is a million).

Why swap-or-not?

Why would we use such an inefficient implementation?

Shuffling single elements

The brilliance is that, if we are interested in only a few indices, we do not need to compute the shuffling of the whole list. In fact, we can apply the algorithm to a single index to find out which index it will be swapped with.

So, if we want to know where the element with index 217 gets shuffled to, we can run the algorithm with only that index; we do not need to shuffle the whole list. Moreover, if we want to know the converse, which element gets shuffled into index 217, we can just run the algorithm backwards for element 217 (backwards means running the round number from high to low rather than low to high).

In summary, we can compute the destination of element i in O(1) operations, and the source of element i' (the inverse operation) also in O(1), not dependent on the length of the list. Shuffles like the Fisher–Yates shuffle do not have this property and cannot work with single indices, they always need to iterate the whole list. The technical term for a shuffle having this property is that it is *oblivious* (to all the other elements in the list).

Keeping light clients light

This property is important for light clients. Light clients are observers of the Eth2 beacon chain that do not store the entire state, but do wish to be able to securely access the chain's data. As part of verifying that they have the correct data – that no-one has lied to them – it is necessary to compute the committees that attested to that data. This means shuffling, and we don't want light clients to have to hold and shuffle the entire list of validators. By using the swap-or-not shuffle, light clients need only to consider the small subset of validators that they are interested in, which is vastly more efficient overall.

See also

- The initial discussion about the search for a good shuffling algorithm is Issue 323 on the specs repo.
- The winning algorithm was announced in Issue 563.
- The original paper describing the swap-or-not shuffle is Hoang, Morris, and Rogaway, 2012, "An Enciphering Scheme Based on a Card Shuffle". See the "generalized domain" algorithm on page 3.

Committees

- Committees are subsets of the full set of active validators that are used to distribute the overall workload.
- Beacon committees manage attestations for the consensus protocol; sync committees are discussed elsewhere.
- Having 64 beacon committees at each slot is a relic of previous Eth2 designs.
- Nonetheless, multiple committees per slot allow us to parallelise attestation aggregation.
- Beacon committee membership is random and transient.
- A target minimum committee size of 128 protects them against capture.

Introduction

One of the challenges of building a highly scalable consensus protocol is organising the work involved so as not to overwhelm the network or individual nodes.

A goal of the Ethereum 2 proof of stake protocol is to achieve economic finality. In the current design (though see below for discussion of single slot finality) this requires us to gather votes from at least two-thirds of the validator set, and we must do this twice: once to justify an epoch, and once again to finalise it.

If the whole validator set were to attest simultaneously, the number of messages on the network would be immense, and the amount of work required of beacon nodes too much for modest hardware. This is where committees help. The work of attesting is divided among subsets of the validator set (committees) and spread across an epoch (6.4 minutes). Each validator participates in only one of the committees.

The Altair spec introduced two types of committees, beacon committees and sync committees, each having quite a different function. We will focus on beacon committees in this section, and deal with sync committees in a later section.

The current beacon committee structure was strongly influenced by a previous roadmap that included in-protocol data sharding. That design is now deprecated, yet a remnant of it remains in our 64 beacon committees per slot. These were originally intended to map directly to 64 shards as "crosslink committees" but no longer have that function. Nonetheless, beacon committees still serve a useful purpose in parallelising the aggregation of attestations. Whether 64 remains the right number of committees per slot has not been analysed to my knowledge. The trade-off is that fewer beacon committees would reduce the amount of block space needed for aggregate attestations, but would increase the time needed for aggregators to do their work.

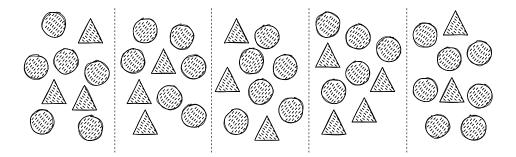
In any case, logically, all of the committees in a slot now act as a single large super-committee, all voting on the same information.

Committee assignments

Beacon committees are convened to vote exactly once and then disbanded immediately - they are completely transient. By contrast, a sync committee lasts for 256 epochs (a little over 27 hours), and votes 8192 times during that period.

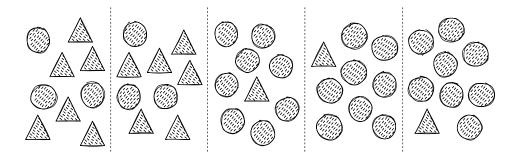
During an epoch, every active validator is a member of exactly one committee, so all the epoch's committees are disjoint. At the start of the next epoch, all the existing committees are disbanded and the active validator set is divided into a fresh set of committees.

The composition of the committees for an epoch is fully determined at the start of an epoch by (1) the active validator set for that epoch, and (2) the RANDAO seed value at the start of the previous epoch.



Here we have divided thirty circles and fifteen triangles into five committees at random. The attacking triangles do not have a majority in any committee.

We assign validators to committees randomly in order to defend against a minority attacker being able to capture any single committee. If committee assignments were not random, or were calculable long in advance, then it might be possible for an attacker with a minority of validators to organise them so that they became a supermajority in some committees. They might do this by manipulating the entries and exits of their validators, for example.



It would be improbable for the triangles to gain a 2/3 supermajority in a committee purely by chance. But if the attacker could manipulate the assignments then they might gain a supermajority in some committees, such as the first two here.

The committee sizes used in the Eth2 protocol were chosen to make the takeover of a committee by a minority attacker extremely unlikely. See target committee size, below, for further analysis of this.

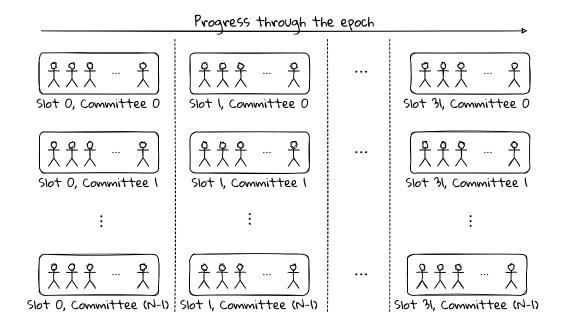
The number of committees

The protocol adjusts the total number of committees in each epoch according to the number of active validators. The goals are,

- 1. to have the same number of committees per slot throughout the epoch (so the number of committees in an epoch is always a multiple of SLOTS_PER_EPOCH),
- 2. to have the largest number of committees that ensures that each committee has at least TARGET_COMMITTEE SIZE members, and
- 3. to have a maximum of MAX_COMMITTEES_PER_SLOT committees per slot.

Clearly, the first goal is not achievable if there are fewer than SLOTS_PER_EPOCH validators – is a committee a committee if nobody is in it? – and the second goal is not achievable if there are fewer than SLOTS_PER_EPOCH * TARGET_COMMITTEE_SIZE (4096) validators. The protocol could hardly be considered secure with fewer than 4096 validators, so this is not a significant issue in practice.

The number of committees per slot is calculated by the spec function $get_committee_count_per_slot()$. This can be simplified for illustrative purposes, given the number n of active validators in the epoch, as



Every slot in an epoch has the same number of committees, N, up to a maximum of MAX_COMMITTEES_PER_SLOT. Every active validator in the epoch appears in exactly one committee, so the committees are all disjoint.

```
MAX_COMMITTEES_PER_SLOT = 64
SLOTS_PER_EPOCH = 32
TARGET_COMMITTEE_SIZE = 128
def committees_per_slot(n):
    return max(1, min(MAX_COMMITTEES_PER_SLOT, n // SLOTS_PER_EPOCH // TARGET_COMMITTEE_SIZE))
```

This generates a committee structure that evolves as per the following table as the number of validators grows or shrinks.

$n \min$	$n \max$	Committees / slot	Members per committee	Min	Max
0	31	1	Some committees have zero members	0	1
32	4095	1	$\lceil n/32 \rceil$ or $\lfloor n/32 \rfloor$, which is below TARGET_COMMITTEE_SIZE	1	128
4096	262143	$N=\lfloor n/4096\rfloor$	$\lceil n/(32N) \rceil$ or $\lfloor n/(32N) \rfloor$	128	256
262144	4194304	64	$\lceil n/2048 \rceil$ or $\lfloor n/2048 \rfloor$	128	2048
4 194 305	-	64	Things break Note that this can never happen in practice.	-	-

The numbers at the various thresholds in this table are calculated from the spec constants:

- 32 is SLOTS_PER_EPOCH.
- 4096 is SLOTS_PER_EPOCH * TARGET_COMMITTEE_SIZE. This is the point at which all the committees achieve their target minimum size.
- 262,144 is SLOTS_PER_EPOCH * TARGET_COMMITTEE_SIZE * MAX_COMMITTEES_PER_SLOT. We have reached the maximum number of committees per slot (64). We no longer add new committees as the validator set grows, we just make the committees larger.

• 4,194,304 is SLOTS_PER_EPOCH * MAX_VALIDATORS_PER_COMMITTEE * MAX_COMMITTEES_PER_SLOT. There is not enough Ether in existence to allow us to reach this number of active validators. The limit exists in protocol to enable us to specify a maximum size for the aggregation_bits SSZ Bitlist type in attestations.

Committee index

Each of the N committees within a slot has a committee index from 0 to N-1. I will call this i in what follows and refer to it as the slot-based index. This slot-based index is included in committees' attestations via the AttestationData object,

class AttestationData(Container):
 slot: Slot
 index: CommitteeIndex
LMD GHOST vote
 beacon_block_root: Root
FFG vote
 source: Checkpoint
 target: Checkpoint

The slot and the committee index within that slot together uniquely identify a committee, and together with the RANDAO value, its membership.

Since all committees in a slot are voting on exactly the same information (source, target, and head block), the index is the only thing that varies between the aggregate attestations produced by the slot's committees (assuming that most of the validators have the same view of the network). This prevents the attestations from the slot's committees being aggregated further, so we will generally end up with N aggregate attestations per slot that we must store in a beacon block.

If it were not for the index then all these N aggregate attestations could be further aggregated into a single aggregate attestation, combining the votes from all the validators voting at that slot.

As a thought experiment we can calculate the potential space savings of doing this. Given a committee size of k and N committees per slot, the current space required for N aggregate Attestation objects is $N*(229+\lfloor k/8\rfloor)$ bytes. If we could remove the committee index from the signed data and combine all of these into a single aggregate Attestation the space required would be $221+\lfloor kN/8\rfloor$ bytes. So we could save 229N-221 bytes per block, which is 14.4 KB with the maximum 64 committees. This seems nice to have, but would likely make the committee aggregation process more complex.

There is another index that appears when assigning validators to committees in compute_committee(): an epoch-based committee index that I shall call j. The indices i and j are related as $i = \mod(j, N)$ and j = Ns + i where s is the slot number in the epoch.

The size of committees

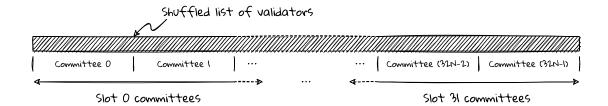
Validators are divided among the committees in an epoch by the compute_committee() function.

Given the epoch-based index j, compute_committee() returns a slice of the full, shuffled validator set as the committee membership. Within the shuffled list, the index of the first validator in the committee is $\lfloor nj/32N \rfloor$, and the index of the last validator in the committee is $\lfloor n(j+1)/32N \rfloor - 1$. So the size of each committee is either $\lfloor n/32N \rfloor$ or $\lceil n/32N \rceil$. In any case, the committee sizes within an epoch differ by at most one.

In simplified form the compute_committee() calculation looks like this. N is the number of committees per slot, n is the total number of active validators, and j is the epoch-based committee index,

```
def compute_committee_size(n, j, N): 
 start = n * j // (32 * N)
end = n * (j + 1) // (32 * N)
return end - start
```

The length of the vector returned will be either n // (32 * N) or 1 + n // (32 * N). The function compute_shuffled_index() is described in the previous section.



Conceptually, to calculate the committee assignments for an epoch, the entire active validator set is shuffled into a list of length n, then sliced into 32N committees of as close to the same size as possible. N is the number of committees per slot. The epoch-based committee number, j, is shown.

In the caption to the diagram above I said that this is "conceptually" how committee membership is determined. In practice, due to our use of an oblivious shuffle, the membership of an individual committee can be calculated without shuffling the entire validator set; the result will be the same.

Target committee size

To achieve a desirable level of security, committees need to be larger than a certain size. This makes it infeasible for an attacker to randomly end up with a super-majority in a committee even if they control a significant number of validators. The target here is a kind of lower-bound on committee size. If there are not enough validators for all committees to have at least TARGET_COMMITTEE_SIZE (128) members, then, as a first measure, the number of committees per slot is reduced to maintain this minimum. Only if there are fewer than SLOTS_PER_EPOCH * TARGET_COMMITTEE_SIZE (4096) validators in total will the committee size be reduced below TARGET_COMMITTEE_SIZE. With so few validators the system would be insecure in any case.

Given a proportion of the validator set controlled by an attacker, what is the probability that the attacker ends up controlling a two-thirds majority in a uniformly randomly selected committee drawn from the full set of validators? Vitalik calculated 111 to be the minimum committee size required to maintain a 2^{-40} chance (one-in-a-trillion) of an attacker with one third of the validators gaining by chance a two-thirds majority in any one committee. The value 128 was chosen as being the next higher power of two.

If an attacker has a proportion p of the validator set, then the probability of selecting a committee of n validators that has k or more validators belonging to the attacker is,

$$\sum_{i=k}^n p^i \big(1-p\big)^{n-i} {n \choose i}$$

Using this we can calculate that, in fact, 109 members is sufficient to give only a 2^{-40} chance of an attacker with one third of the validators gaining a two-thirds majority by chance.

Code for calculating the target committee size

The following is Vitalik's Python code for calculating the probabilities.

```
def fac(n):
    return n * fac(n-1) if n else 1

def choose(n, k):
    return fac(n) / fac(k) / fac(n-k)

def prob(n, k, p):
    return p**k * (1-p)**(n-k) * choose(n,k)

def probge(n, k, p):
    return sum([prob(n,i,p) for i in range(k,n+1)])
```

Armed with this we find that the minimum committee size to avoid a two-thirds majority with a 2^{-40} probability is 109 rather than 111.

```
>>> probge(108, 72, 1.0 / 3) < 2**-40 False  
>>> probge(109, 73, 1.0 / 3) < 2**-40 True
```

In any case, a committee size of 128 is very safe against an attacker with 1/3 of the stake:

```
>>> probge(128, 86, 1.0 / 3) 5.551560731791749e-15
```

Odds of one-in-trillion may sound like over-engineering, but we must also consider that an attacker might gain some power over the RANDAO, so some safety margin is desirable.

Notwithstanding all of this, in the current beacon chain design the minimum target committee size is irrelevant as committees never operate alone. As long as we have at least 8192 active validators, each slot has multiple committees all operating together, and it is their aggregate size that confers security, not the size of any individual committee. As previously mentioned, the current committee design is influenced by an old data sharding model that is now superseded. Nonetheless, individual committees might find a role in future versions of the protocol, so the minimum target size is worth preserving.

See also

In his survey article, Paths toward single-slot finality, Vitalik considers what it would take to introduce a single "super-committee" at each slot to replace the existing beacon committees. The super-committee would be a large enough subset of the whole validator set to achieve a satisfactorily secure level of finality within a single (extended, 16 second or longer) slot.

Aggregator Selection

- In each committee, a subset of validators is selected to perform aggregation of the committee's messages. This improves scaling.
- Selection of aggregators is probabilistic based on BLS signatures.
- This selection method preserves both secrecy and easy verifiability of the identity of the aggregators.

Introduction

In both beacon committees and sync committees validators create and sign their own votes (Attestations and SyncCommitteeMessages respectively). These votes must be aggregated into a much smaller number of aggregate signed votes, ideally into a single aggregate signature over a single vote, before being included in beacon blocks.

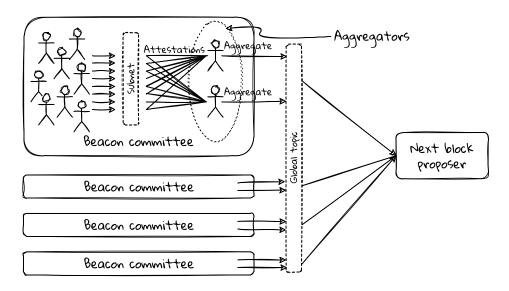
The goals of aggregation are three-fold: to reduce the signature verification load on the next block proposer, to reduce the network load on the global gossip channel, and to reduce the amount of block space required to store the signatures.

In the current beacon chain design, voting is done in committees with the goal of getting a majority of committee members to sign off on the same vote, although in practice there might be a number of different votes depending on the network views of the individual committee members. In any case, members of different committees are signing different data that cannot be aggregated across committees.

The process of aggregation is as follows:

- 1. Committee members sign their votes (Attestations or SyncCommitteeMessages depending on which type of committee we are considering) and broadcast them to a peer-to-peer subnet that the whole committee is subscribed to.
- 2. A subset of the committee is selected to be aggregators for that committee.
- 3. The aggregators listen on the subnet for votes, then aggregate all the votes they receive that agree with their own view of the network into a single aggregate vote (aggregate Attestation or SyncCommitteeContribution).
- 4. Each aggregator wraps its aggregate vote with a proof that it was indeed an aggregator for that committee, and it signs the resulting data (SignedAggregateAndProof or SignedContributionAndProof)
- 5. Finally, the aggregator broadcasts its aggregated vote and proof to a global channel to be received by the next block proposer.

This section is concerned with steps 2 and 4: how the aggregators are selected for duty, and how they prove that they were indeed selected.



Within a beacon committee, all members send their individual attestations to a gossip subnet. Aggregators are a chosen subset of the committee who listen to the subnet and aggregate the attestations they receive. The aggregators broadcast their aggregates to the global channel for the next block proposer to pick up.

Aggregator selection desiderata

Aggregator selection has been designed with three properties in mind.

First, the size of the resulting aggregator set. With very high probability we want a small, non-empty subset of the committee to be selected in order that we have a very high chance of selecting at least one honest, well-connected aggregator. It doesn't matter too much if our set of aggregators is slightly on the large side, but we really want to avoid having no aggregators at all. Bearing in mind that there's a chance of validators being down or malicious, selecting only one or two aggregators is also risky.

Second, secrecy. We'd prefer that nobody be able to calculate who the aggregators are until after they have broadcast their aggregations. This helps to avoid denial of service (DoS) attacks. Disrupting consensus would be much simpler via a network DoS attack against a small number of aggregators than against a whole committee. The secrecy property prevents this.

Third, verifiability. We want it to be easy to verify a claim that a particular validator was selected to be an aggregator. The rationale for this is explained in the p2p spec. Basically, without verifiability it would be a good strategy for all the validators in the committee to make and broadcast aggregate

attestations to ensure that at least one aggregate includes their own attestation. This would destroy the benefits of the whole aggregator scheme.

Aggregator selection details

The current aggregation strategy was introduced in PR 1440 and is described in the Honest Validator specs for beacon committees and sync committees.

It turns out that we can straightforwardly satisfy our three desirable properties of size, secrecy, and verifiability using BLS signatures. The algorithm is quite simple. Each validator in the committee generates a verifiable random number; if that random number modulo another number is zero then it is an aggregator, otherwise it is not an aggregator.

The validator creates its verifiable random number by making a signature over the current slot number using its normal secret signing key, and then hashing the signature. We assume that the result of this is uniformly random; we have no reason to suspect it isn't.

Any validator whose random number modulo <code>len(committee)</code> // <code>TARGET_AGGREGATORS_PER_COMMITTEE</code> equals zero is then an aggregator. This modulus is chosen to provide an average of 16 aggregators per beacon committee.

The following are the spec functions for determining which validators are the aggregators in beacon committees.

This approach provides secrecy since it relies on the validator's secret key: no-one else can determine whether or not I am an aggregator until after I have published the proof. And it provides verifiability since, once the proof is published, it is easy to check the validity of the signature using the validator's public key.

What about the size criterion?

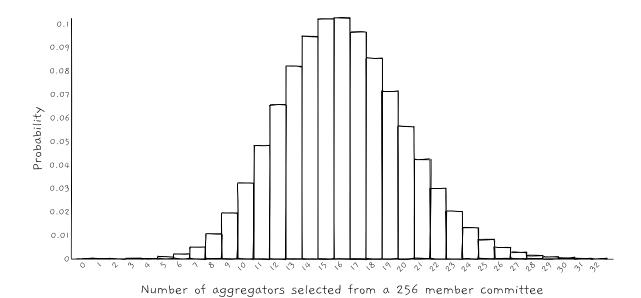
Beacon committee aggregators

Assuming that BLS signatures are uniformly random, then in a committee of size N each validator will have a probability of being selected of TARGET_AGGREGATORS_PER_COMMITTEE / N (ignoring the integer arithmetic). So in expectation we will have TARGET_AGGREGATORS_PER_COMMITTEE (16) aggregators per committee.

The probability of having zero aggregators is $(1-\frac{16}{N})^N$. For the minimum target committee size of N=128 this is 1 in 26 million, and for the maximum committee size of N=2048, 1 in 9.5 million. So we would expect to see a beacon committee with no aggregators about once every 13,000 epochs (8 weeks) in the former case and once every 5000 epochs (3 weeks) in the latter. Each committee comprises only a fraction 1/2048 of the total validator set, so occasionally having no aggregator is insignificant for the protocol, but it is unfortunate for those in that committee who will most likely not have their attestations included in a block as a result.

Sync committee aggregators

Sync committees operate similarly. Each committee has 512 members that are divided across four independent subnets. The target is to have 16 aggregators per subnet as above, with the aggregators changing in each slot.



The probability of having k aggregators in a beacon committee of size 256. The expected number is 16.

The TARGET_AGGREGATORS_PER_SYNC_SUBCOMMITTEE value was increased from 4 to 16 ahead of the implementation of sync committees. This was based on an analysis showing that, by targeting only four aggregators, there would be an unacceptably high chance of having no aggregators on a sync committee subnet.

Incentivisation

Aggregators are not directly incentivised by the protocol: there are no explicit rewards or penalties for performing or not performing aggregation duties.

However, there are implicit incentives. For one, if I produce a high quality aggregate signature it helps to ensure that my own signature is included in a block (there's a chance that someone else's aggregate may not include my signature). For another, since overall attestation rewards scale in proportion to participation (inclusion of attestations in blocks), aggregators benefit alongside all the other validators from slightly higher rewards when they make high quality aggregates that include many votes.

See also

Hsiao-Wei Wang has documented the original research around aggregator selection.

This aggregation strategy presents a difficulty for building distributed validator technology (DVT). One approach to implementing DVT is for the multiple validators representing a single validator to operate independently, alongside a middleware that combines their signed attestations. This works because BLS signatures are additive: each validator has part of the key, and the signed attestations can be combined with a threshold signature scheme into a signature from the full key. However, the process of hashing the (combined) signature can't be done in a distributed way, so it is difficult for the individual validators to determine whether the collective validator has been selected to be an aggregator or not. Oisín Kyne's ethresear.ch article explores this problem and suggests a solution, which appears (slightly modified) in the proposed addition of two endpoints to the Beacon API spec.

SSZ: Simple Serialize

- The beacon chain uses a novel serialisation method called Simple Serialize (SSZ).
- After much debate we chose to use SSZ for both consensus and communication.
- SSZ is not self-describing; you need to know in advance what you are descrialising.
- An offset scheme allows fast access to subsets of the data.
- SSZ plays nicely with Merkleization and generalised indices in Merkle proofs.

Introduction

Serialisation is the process of taking structured information (in our case, a data structure) and transforming it into a representation that can be stored or transmitted.

A cooking recipe is a kind of serialisation. I can write down a method for cooking something in such a way that you and others can recreate the method to cook the same thing. The recipe can be written in a book, appear online, even be spoken and memorised – this is serialisation. Using the recipe to cook something is describing is described by the cook something is described by the cook is cook to cook the cook in the cook is cook to cook the cook in the cook is cook to cook in the cook

Serialisation is used for three main purposes on the beacon chain.

- 1. Consensus: if you and I each have information in a data structure, such as the beacon state, how can we know if our data structures are the same or not? Serialisation allows us to answer this question, as long as all clients use the same method. Note that this is also bound up with Merkleization.
- 2. Peer-to-peer communication: we need to exchange data structures over the Internet, such as attestations and blocks. We can't transmit structured data as-is, it must be serialised for transmission and descrialised at the other end. All clients must use the same p2p serialisation, but it doesn't need to be the same as the consensus serialisation.
- 3. Similarly, data structures need to be serialised for users accessing a beacon node's API. Clients are free to choose their own API serialisation. For example, the Prysm client has an API that uses Protocol Buffers (which is being deprecated now that we have agreed a common API format that uses both SSZ and JSON).

In addition, data must be serialised before being written to disk. Each client is free to do this internally however they wish.

Ethereum 2.0 uses a bespoke serialisation scheme called Simple Serialize, or more commonly just "SSZ"⁸⁸, for all of these purposes.

History

It seems like we spent months over the end of 2018 and the start of 2019 talking about serialisation, and the story below is highly simplified. But I think it's worth recording some of the considerations and design decisions.

Ethereum 1 has always used a serialisation format called RLP (recursive length prefix). This was deemed unsuitable for Ethereum 2, largely because it is regarded as overly complex.⁸⁹

So, we had the freedom to choose a new serialisation protocol. What kind of decision points did we consider?

 $^{^{88} \}mathrm{Thus}$ enshrining that ugly "z" in the full name, and the ghastly "ess-ess-zee" pronunciation.

⁸⁹Vitalik, "As the inventor of RLP, I'm inclined to prefer SSZ", and again, "RLP honestly sucks" (with some explanation as to why!).

Serialisation for consensus

Starting with serialisation in the consensus protocol, the first big question was whether to adopt an existing off-the-shelf protocol or to roll our own.

One major issue with many existing schemes is that they do not guarantee that the serialisation is deterministic: they sometimes re-order fields in unpredictable ways. This makes them totally unsuitable for consensus; the same data must result in the same output every time.

A more general concern was around using third-party libraries in a consensus-critical situation. Back in 2014, Vitalik wrote a justification, titled Why not use X?, of Ethereum implementing its own technology (such as RLP) for so many things. Here's an excerpt:

One of our core principles in Ethereum is simplicity; the protocol should be as simple as possible, and the protocol should not contain any black boxes. Every single feature of every single sub-protocol should be precisely 100% documented on the whitepaper or wiki, and implemented using that as a specification.

Certainly, with respect to serialisation, some third-party libraries are far more generic than we need, which can lead to issues. Others don't map nicely to the data types that we want to use.

In view of these concerns, momentum was in favour of adopting a bespoke, tightly specified serialisation method. It was the development of Merkleization on top of SSZ that cemented this, making SSZ (in some form) the clear leader for consensus serialisation.

Serialisation for communications

That decision made, the next big question was whether to use the same scheme for both consensus serialisation and peer-to-peer communications serialisation (the "wire-protocol"). This was finely balanced, and good arguments were made in favour of using Protocol Buffers for p2p communication and SSZ for consensus.

Discussion around this was extensive (see the references below), but we eventually decided to use SSZ for p2p communications.

The factors that tipped the balance in favour of SSZ for communications were (1) a desire to maintain only one serialisation library, and (2) some possible performance benefit.

On the first of these, there is a bias in Ethereum 2 to favour "simplicity over efficiency". Maintaining two serialisation libraries is arguably more overhead than any potential gain from using different ones. Having said that, RLP is still used in Eth2's discovery layer (since it is shared with Eth1), so this argument loses some of its force.

On the second, when we receive an object over the wire, often the first thing we will want to do is to serialise it to calculate its data root for consensus. If we receive it already serialised in the right format then it saves a deserialise/reserialise round trip.

SSZ does not make any effort to compact or compress the serialised data, and there were concerns that this might make it inefficient for the wire transfer protocol. These concerns were alleviated by adding Snappy compression on the wire, as is already done in Ethereum 1.

SSZ development

SSZ is based on Ethereum's smart contract ABI, but with 4-byte position and size records rather than 32-byte, and different basic data types. It will immediately feel familiar to anyone who has fiddled with that. The rudiments of SSZ were laid down by Vitalik in August 2017.

The initial, more developed, spec for SSZ was merged into the beacon chain repository in October 2018, with the Container type being added a month later.

A big step forward in the utility of SSZ, and what established it as the serialisation protocol of choice for consensus, was the development of Merkleization (also known as tree hashing), first discussed in October 2018 and adopted into the spec in November.

Also in November 2018 we agreed to switch the byte ordering for integer types from big-endian to little-endian at the request of the Nimbus team. This means that the 32-bit number representing 66 decimal

is now serialised as 0x42000000 rather than 0x00000042. The main motivation for the change was to map better to byte-ordering in typical microprocessors.

April 2019 saw a major change to SSZ with the adoption of offsets. This came from a scheme, Simple Offset Serialisation, previously proposed by Péter Szilágyi. The idea is to split the objects we are serialising according to whether they are fixed length or variable length. The serialisation then has two sections. The first section contains both actual serialisations of any fixed length objects, and pointers (offsets) to the serialisations of any variable length objects. The second section contains the serialisations of the variable length objects. The motivation for this is to allow fast access to arbitrary parts of the serialised data without having to describe the whole structure.

There was one final substantial re-work of the SSZ spec in June 2019 in which SSZ lists were required to have a maximum length specified, and bitlist and bitvector types were added.

Overview

The specification of SSZ is maintained in the main consensus specs repo, and that's the place to go for all the details. I will only be presenting an introductory overview here, with a few examples.

The ultimate goal of SSZ is to be able to represent complex internal data structures such as the BeaconState as strings of bytes.

The formal properties that we require for SSZ to be useful for both consensus and communications are as defined in the SSZ formal verification exercise. Given objects O_1 and O_2 , both of type T, we require that SSZ be

- 1. involutive: deserialise $\langle T \rangle$ (serialise $\langle T \rangle (O_1) = O_1$ (required for communications), and
- 2. injective: $\operatorname{serialise}\langle T\rangle(O_1)=\operatorname{serialise}\langle T\rangle(O_2)$ implies that $O_1=O_2$ (required for consensus).

The first property says that when we serialise an object of a certain type then describing the result, we end up with an object identical to the one we started with. This is essential for the communications protocol.

The second says that if we serialise two objects of the same type and get the same result then the two objects are identical. Equivalently, if we have two different objects of the same type then their serialisations will differ. This is essential for the consensus protocol.

Beyond those basic functional requirements, other goals for SSZ are to be (relatively) simple, to create (fairly) compact serialisations, and to be compatible with Merkleization. It is also useful to be able to quickly access specific bits of data within the serialisation without deserialising the entire object. The adoption of offsets into SSZ improved its performance in that respect.

Unlike RLP, SSZ is not self-describing. You can decode RLP data into a structured object without knowing in advance what that object looks like. This is not the case for SSZ: you must know in advance exactly what you are describing. In practice this has not been a problem for Eth2: we always know in advance what class of object a particular describined blob of data corresponds to. A consequence of this is that, while in RLP two objects of different types cannot serialise to the same output, in SSZ they can. We'll see an example of this shortly.

Specification

I don't plan to go into every last detail of SSZ – that's what the specification is for – rather, we'll take a general overview and then dive into a worked example.

The building blocks of SSZ are its basic types and its composite types.

Basic types

SSZ's basic types are very simple and limited, comprising only the following two classes.

- Unsigned integers: a uintN is an N-bit unsigned integer, where N can be 8, 16, 32, 64, 128 or 256.
- Booleans: a boolean is either True or False.

The serialisation of basic types lives up to the "simple" name:

- uintN types are encoded as the little-endian representation in N/8 bytes. For example, the decimal number 12345 (0x3039 in hexadecimal) as a uint16 type is serialised as 0x3930 (two bytes). The same number as a uint32 type is serialised as 0x39300000 (four bytes).
- boolean types are always one byte and serialised as 0x01 for true and 0x00 for false.

I have embedded some examples in the following descriptions. You can run them yourself if you set up the Eth2 spec as per the instructions in the Appendices. The examples can be run via the Python REPL or by putting the commands in a file (I show both approaches).

```
>>> from eth2spec.utils.ssz.ssz_typing import uint64, boolean
>>> uint64(0x0123456789abcdef).encode_bytes().hex()
'efcdab8967452301'
>>> boolean(True).encode_bytes().hex()
'01'
>>> boolean(False).encode_bytes().hex()
'00'
```

Composite types

Composite types hold combinations of or multiples of smaller types. The spec defines the following composite types: vectors, lists, bitvectors, bitlists, unions, and containers. I will skip unions in the following as they are not currently used in Ethereum 2.

Vectors

A vector is an ordered fixed-length homogeneous collection with exactly N values. "Homogeneous" means that all the elements of a vector must be of the same type, but they do not need to be of the same size. For example, we could have a vector containing lists that each have different numbers of elements.

In the SSZ spec a vector is denoted by Vector[type, N]. For example Vector[uint8, 32] is a 32 element list of uint8 types (bytes). The type can be anything, including other vectors or even containers.

Vectors provide a simple example of needing to know what kind of object you are descrialising before you attempt it. In the following example, the same string of bytes encodes both a four element set of two-byte integers, and an eight element set of one-byte integers. When we descrialise this we need to know which of these (or many other possibilities) we are expecting to get.

```
>>> from eth2spec.utils.ssz.ssz_typing import uint8, uint16, Vector
>>> Vector[uint16, 4](1, 2, 3, 4).encode_bytes().hex()
'0100020003000400'
>>> Vector[uint8, 8](1, 0, 2, 0, 3, 0, 4, 0).encode_bytes().hex()
'0100020003000400'
```

Fun fact: in early versions of the SSZ spec, vectors were called tuples.

Lists

A list is an ordered variable-length homogeneous collection with a maximum of N values.

In the SSZ spec a list is denoted by List[type, N]. For example, List[uint64, 100] is a list containing anywhere between zero and one hundred uint64 types.

The maximum length parameter, N, on lists is not used in serialisation or deserialisation. It is used, however, in Merkleization, and in particular enables generalised indices in Merkleization.

Both vectors and lists have the same serialisation when they are treated as stand-alone objects:

```
>>> from eth2spec.utils.ssz.ssz_typing import uint8, List, Vector
>>> List[uint8, 100](1, 2, 3).encode_bytes().hex()
'010203'
>>> Vector[uint8, 3](1, 2, 3).encode_bytes().hex()
'010203'
```

So why not use lists everywhere? Since lists are variable sized objects in SSZ they are encoded differently from fixed sized vectors when contained within another object, so there is a small overhead. The container Foo holding the variable sized list is encoded with an extra four-byte offset at the start. We'll see why a bit later.

Bitvectors

A bitvector is an ordered fixed-length collection of boolean values with N bits. In the SSZ spec, a bitvector is denoted by Bitvector[N].

It is not obvious from the spec, but bitvectors use little-endian bit format:

```
>>> from eth2spec.utils.ssz.ssz_typing import Bitvector
>>> Bitvector[8](0,0,0,0,0,0,1).encode_bytes().hex()
'80'
```

Bitvectors are encoded into the minimum necessary number of whole bytes (N // 8) and padded with zeroes in the high bits if N is not a multiple of 8.

As noted in the spec, functionally we could use either Vector[boolean, N] or Bitvector[N] to represent a list of bits. However, the latter will have a serialisation up to eight times shorter in practice since the former will use a whole byte per bit.

```
>>> from eth2spec.utils.ssz.ssz_typing import Vector, Bitvector, boolean
>>> Bitvector[5](1,0,1,0,1).encode_bytes().hex()
'15'
>>> Vector[boolean,5](1,0,1,0,1).encode_bytes().hex()
'0100010001'
```

The same consideration applies for lists and bitlists.

Bitlists

A bitlist is an ordered variable-length collection of boolean values with a maximum of N bits. In the SSZ spec, a bitlist is denoted by Bitlist[N].

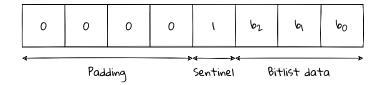
An interesting feature of bitlists⁹⁰ is that they use a sentinel bit to indicate the length of the list. The number of whole bytes in the bitlist is easily derived from the offsets in the serialisation, but that doesn't give us the precise number of bits. For example, in a naive scheme 13 bits would be serialised into two bytes, so we would only know that the actual list length is somewhere between 9 and 16 bits.

To resolve this problem, bitlist serialisation adds an extra 1 bit at the end of the list (which becomes the highest-order bit in the little-endian encoding). The exact length of the bitlist can then be found by ignoring any consecutive high-order zero bits and then stripping off the single sentinel bit.

As an example, this bitlist with three elements is encoded into a single byte. To descrialise this, we take the total length in bits (eight), skip the four high-order zero bits, skip the sentinel bit, and then our list comprises the remaining three bits. Equivalently, the bitlist length is the index of the highest 1 bit in the serialisation.

⁹⁰Though not entirely uncontroversial. Basically, if the application layer already knows what length of bitlist it expects – which it generally does in Eth2, since although committee sizes change, the sizes are known – then we could in principle dispense with the sentinel bit.

```
>>> from eth2spec.utils.ssz.ssz_typing import Bitlist
>>> Bitlist[100](0,0,0).encode_bytes().hex()
'08'
```



The sentinel bit indicates the end of the bitlist. All bits beyond the sentinel are zero.

As a consequence of the sentinel, we require an extra byte to serialise a bitlist if its actual length is a multiple of eight (irrespective of the maximum length). This is not the case for a bitvector.

```
>>> Bitlist[8](0,0,0,0,0,0,0).encode_bytes().hex()
'0001'
>>> Bitvector[8](0,0,0,0,0,0,0,0).encode_bytes().hex()
'00'
```

Containers

A container is an ordered heterogeneous collection of values. Basically, a container can contain any arbitrary mix of types, including containers.

We define containers using Python's dataclass notation with key-type pairs. For example, this is a Deposit container. In the following examples I have indicated the underlying types in the appended comments.

```
class Deposit(Container):
    proof: Vector[Bytes32, DEPOSIT_CONTRACT_TREE_DEPTH + 1] # Vector[Vector[uint8, 32], N]
    data: DepositData
```

The Deposit container contains a DepositData container which is defined as follows.

```
class DepositData(Container):
   pubkey: BLSPubkey  # Bytes48 / Vector[uint8, 48]
   withdrawal_credentials: Bytes32 # Vector[uint8, 32]
   amount: Gwei  # uint64
   signature: BLSSignature  # Bytes96 / Vector[uint8, 96]
```

We'll see how containers are serialised in the worked example, below.

Fixed and variable size types

SSZ distinguishes between fixed size and variable size types, and treats them differently when they are contained within other types.

- Variable size types are lists, bitlists, and any type that contains a variable size type.
- Everything else is fixed size.

This distinction is important when we serialise a compound type. The serialised output is created in two parts, as follows.

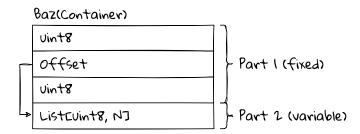
- 1. The serialisation of fixed length types, along with 32-bit offsets to any variable length types.
- 2. The serialisation of any variable length types.

This split between a fixed length part and a variable length part came about as a result of the offset encoding described earlier: it allows fast access to specific fields within a serialised data structure without needing to describe the whole thing.

As an example, consider the following container. It has a single fixed length uint8 type, followed by a variable length List[uint8,10] type, followed again by a fixed length uint8.

We see that the serialisation contains an unexpected 0x06 byte and some zero bytes. To see where they come from I'll break down the output as follows, where the first column is the byte number in the serialised string.

In Part 1, instead of directly encoding the variable size list in place, it is replaced with a pointer (an offset) to its serialisation in Part 2. So, for any container, the size of Part 1 is known and fixed no matter what kinds of variable size types are present. The actual lengths of the variable size objects can be deduced from the offsets in Part 1 and the overall length of the serialisation string.



Serialisation of the Baz container. Fixed size parts are done first, with an offset specified for the variable size List data.

It's not only containers that use this format, it applies to any type that contains variable size types. Here's a vector whose elements are lists. As an exercise for the reader I'll leave you to decode what's going on here.

```
>>> from eth2spec.utils.ssz.ssz_typing import uint8, List, Vector
>>> Vector[List[uint8,3],4]([1,2],[3,4,5],[],[6]).encode_bytes().hex()
'1000000012000000150000001500000010203040506'
```

Aliases

Just quoting directly from the SSZ spec here for completeness⁹¹:

For convenience we alias:

- bit to boolean
- byte to uint8 (this is a basic type)

⁹¹An instructive discussion of the wisdom or otherwise of aliasing byte to uint8 was sparked when we began defining a canonical JSON mapping for SSZ data. The words "fight to the death" were used.

- BytesN and ByteVector[N] to Vector[byte, N] (this is not a basic type)
- ByteList[N] to List[byte, N]

In the main beacon chain spec, a bunch of custom types are also defined in terms of the standard SSZ types and aliases. For example, Slot is an SSZ uint64 type, BLSPubkey is an SSZ Bytes48 type, and so on.

Default values

Finally, each type has a default value. Once again directly from the SSZ spec:

Type	Default Value
uintN	0
boolean	False
Container	[default(type) for type in container]
<pre>Vector[type, N]</pre>	<pre>[default(type)] * N</pre>
<pre>Bitvector[N]</pre>	[False] * N
List[type, N]	[]
Bitlist[N]	[]

Worked example

Let's explore a worked example to gather all of this together. I'd rather use a real example than make up a synthetic object, so we are going to look at the aggregate IndexedAttestation that was included in the beacon chain block at slot 3080831, at position 87 within the block. (It would actually have been an Attestation object in the block, but those bitlists are fiddly, so we'll look at the equivalent IndexedAttestation.)

The data structures

The IndexedAttestation container looks like this.

```
class IndexedAttestation(Container):
    attesting_indices: List[ValidatorIndex, MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    signature: BLSSignature

It contains an AttestationData container,
class AttestationData(Container):
```

slot: Slot
index: CommitteeIndex

beacon_block_root: Root source: Checkpoint target: Checkpoint

which in turn contains two Checkpoint containers,

```
class Checkpoint(Container):
    epoch: Epoch
    root: Root
```

The serialisation

Now we have enough information to build the ${\tt IndexedAttestation}$ object and calculate its SSZ serialisation.

```
from eth2spec.utils.ssz.ssz_typing import *
from eth2spec.capella import mainnet
from eth2spec.capella.mainnet import *
attestation = IndexedAttestation(
   attesting_indices = [33652, 59750, 92360],
   data = AttestationData(
       slot = 3080829,
       index = 9,
       beacon\_block\_root = '0x4f4250c05956f5c2b87129cf7372f14dd576fc152543bf7042e963196b843fe6',
       source = Checkpoint (
           epoch = 96274.
           root = '0xd24639f2e661bcladcbe7157280776cf76670fff0fee0691f146ab827f4f1ade'
       ),
       target = Checkpoint(
           epoch = 96275,
           root = '0x9bcd31881817ddeab686f878c8619d664e8bfa4f8948707cba5bc25c8d74915d'
       )
   ),
   signature = '0xaaf504503ff15ae86723c906b4b6bac91ad728e4431aea3be2e8e3acc888d8af'
               + '5dffbbcf53b234ea8e3fde67fbb09120027335ec63cf23f0213cc439e8d1b856'
               + 'c2ddfc1a78ed3326fb9b4fe333af4ad3702159dbf9caeb1a4633b752991ac437'
)
print(attestation.encode_bytes().hex())
The resulting serialised blob of data that represents this IndexedAttestation object is (in hexadecimal):
e40000007d022f00000000000090000000000004f4250c05956f5c2b87129cf7372f14dd576fc15
2543bf7042e963196b843fe61278010000000000d24639f2e661bc1adcbe7157280776cf76670fff
```

This can be transmitted as a string of bytes over the wire and, knowing at the other end that it represents an IndexedAttestation, reconstituted into an identical copy.

The serialisation unpacked

00000000c868010000000000

To make sense of this, we'll break down the serialisation into its parts. The first column is the byte-offset from the start of the byte string (in hexadecimal). Before each line I've indicated which part of the data structure it corresponds to, and I've translated the type aliases into their basic underlying SSZ types. Remember that all integer types are little-endian, so 7d022f0000000000 is the hexadecimal number 0x2f027d, which is 3080829 in decimal (the slot number).

```
Start of Part 1 (fixed size elements)
4-byte offset to the variable length attestation.attesting_indices starting at 0xe4
00 e4000000

attestation.data.slot: Slot / uint64
04 7d022f00000000000

attestation.data.index: CommitteeIndex / uint64
0c 09000000000000000

attestation.data.beacon_block_root: Root / Bytes32 / Vector[uint8, 32]
14 4f4250c05956f5c2b87129cf7372f14dd576fc152543bf7042e963196b843fe6

attestation.data.source.epoch: Epoch / uint64
34 12780100000000000

attestation.data.source.root: Root / Bytes32 / Vector[uint8, 32]
```

8948707 cba5bc25c8d74915 daaf504503ff15ae86723c906b4b6bac91ad728e4431aea3be2e8e3acc888d8af5dffbbcf53b234ea8e3fde67fbb09120027335ec63cf23f0213cc439e8d1b856c2ddfc1a78ed3326fb9b4fe333af4ad3702159dbf9caeb1a4633b752991ac437748300000000000066e90000

```
attestation.data.target.epoch: Epoch / uint64
5c 1378010000000000

attestation.data.target.root: Root / Bytes32 / Vector[uint8, 32]
64 9bcd31881817ddeab686f878c8619d664e8bfa4f8948707cba5bc25c8d74915d

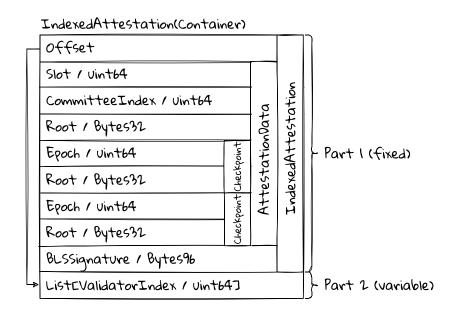
attestation.signature: BLSSignature / Bytes96 / Vector[uint8, 96]
84 aaf504503ff15ae86723c906b4b6bac91ad728e4431aea3be2e8e3acc888d8af
a4 5dffbbcf53b234ea8e3fde67fbb09120027335ec63cf23f0213cc439e8d1b856
c4 c2ddfc1a78ed3326fb9b4fe333af4ad3702159dbf9caeb1a4633b752991ac437
```

3c d24639f2e661bc1adcbe7157280776cf76670fff0fee0691f146ab827f4f1ade

```
Start of Part 2 (variable size elements)
attestation.attesting_indices: List[uint64, MAX_VALIDATORS_PER_COMMITTEE]
e4 7483000000000000066e900000000000868010000000000
```

The first thing to notice is that the attesting_indices list is variable size, so it is represented in Part 1 by an offset pointing to where the actual data is. In this case, at 0xe4 bytes (228 bytes) from the start of the serialised data. The actual length of the list can be calculated as the length of the whole string (252 bytes) minus 228 bytes (the start of the list) divided by 8 bytes, one per element. And so, we recover our list of three validator indices.

All the remaining items are fixed size, and are encoded in-place, including recursively encoding the fixed size AttestationData object, and its fixed size Checkpoint children.



 $Serialisation\ of\ the\ {\tt IndexedAttestation}\ container.$

Multiple variable size objects

It is instructive to see how container with multiple variable size child objects is serialised. For this example we will make an AttesterSlashing object that contains two of the above IndexedAttestation objects. This is a contrived example; the slashing report is not valid since the contents are duplicates.

An AttesterSlashing container is defined as follows,

```
class AttesterSlashing(Container):
   attestation_1: IndexedAttestation
   attestation_2: IndexedAttestation
```

which we can populate and serialise like this, using our previously defined IndexedAttestation object, attestation.

```
slashing = AttesterSlashing(
   attestation_1 = attestation,
   attestation_2 = attestation
)
print(slashing.encode_bytes().hex())
```

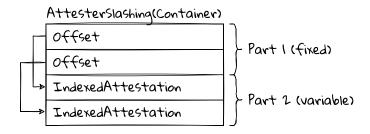
From this we get the following serialisation, again shown with the byte-offset within the byte string in the first column.

```
Start of Part 1 (fixed size elements)
0000 08000000
0004 04010000

Start of Part 2 (variable size elements)
0008 e4000007d022...
0104 e4000007d022...
```

This time we have two variable length types, so they are both replaced by offsets pointing to the start of the actual variable length data which appears in Part 2. The length of attestation_1 is calculated as the difference between the two offsets, and the length of attestation_2 is calculated as the length from its offset to the end of the string.

Another thing to note is that, since attestation_1 and attestation_2 are identical, their serialisations within this compound object are identical, *including* their internal offsets to their own variable length parts. That is, both attestations have variable length data at offset <code>0xe4</code> within their own serialisations; the offset is relative to the start of each sub-object's serialisation, not the entire string. This property simplifies recursive serialisation and deserialisation: a given object will have the same serialisation no matter what context it is found in.



Serialisation of the AttesterSlashing container.

See also

The SSZ specification is the authoritative source. There is also a curated list of SSZ implementations.

The historical discussion threads around whether to use SSZ for both consensus and p2p serialisation or not are a goldmine of insight and wisdom.

- Possibly the first substantial discussion around which serialisation scheme to adopt. It covers various alternatives, touches on the p2p vs. consensus issues, and rehearses some of the desirable properties.
- An early discussion of SSZ went over some of the issues and led into the discussion below.
- Proposal to use SSZ for consensus only.
- Piper Merriam's Everything You Never Wanted To Know About Serialization remains a good summary of many of the considerations.

Other SSZ resources:

- SSZ encoding diagrams by Protolambda.
- Formal verification of the SSZ specification: Notes and Code.

- An excellent SSZ explainer by Raul Jordan with a deep dive into implementing it in Golang. (Note that the specific library referenced in the article has now been deprecated in favour of fastssz.)
- An interactive SSZ serialiser/deserialiser by ChainSafe with all the containers for the various consensus layer upgrades available to play with. On the "Deserialize" tab you can paste the data from the IndexedAttestation above and verify that it deserialises correctly (you'll need to remove line breaks).

Hash Tree Roots and Merkleization

- A hash tree root provides a succinct cryptographic digest of an SSZ data structure.
- Calculating the hash tree root involves recursively Merkleizing the data structure.
- Merkleization is tightly coupled to SSZ and is defined in the same spec.
- The use of hash tree roots enables large parts of the beacon state to be cached, making it practical to operate with a monolithic beacon state.
- Eth2's Merkleization approach facilitates generalised indices and Merkle proofs which are important for light clients.

Introduction

While discussing SSZ, I asserted that serialisation is important for consensus without going into the details. In this section we will unpack that and take a deep dive into how Ethereum 2 nodes know that they share a view of the world.

Let's say that you and I want to compare our beacon states to see if we have an identical view of the state of the chain. One way we could do this is by serialising our respective beacon states and sending them to each other. We could then compare them byte-by-byte to check that they match. The problem with this is that the serialised beacon state at the time of writing is over 41 MB in size and takes several seconds to transmit over the Internet. This is completely impractical for a global consensus protocol.

What we need is a *digest* of the state: a brief summary that is enough to determine with a very high degree of confidence whether you and I have the same state, or whether they differ. The digest must also have the property that no-one can fake it. That is, you can't convince me that you have the same state as I do while actually having a different state.

Thankfully, such digests exist in the form of cryptographic hash functions. These take a (potentially) large amount of input data and mangle it up into a small number of bytes, typically 32, that for all practical purposes uniquely fingerprint the data.

Armed with such a hash function⁹² we can improve on the previous idea. You and I separately serialise our beacon states and then hash (apply the hash function to) the resulting strings. This is much faster than sending all the data over the network. Now we only need to exchange and compare our very short 32-byte hashes. If they match then we have the same state; if they don't match then our states differ.

This process is very common, and was an early candidate for consensus purposes in Ethereum 2, though it was apparent fairly early that there might be better ways.

A problem with this approach is that, if you modify any part of the state – even a single bit – then you need to recalculate the hash of the entire serialised state. This is potentially a huge overhead. It was dealt with in early versions of the spec by splitting the beacon state into two parts: a slowly changing "crystallised" state that would rarely need re-hashing, and a smaller fast changing "active"

 $^{^{92}}$ See the Annotated Spec for the saga of Eth2's hash function, and how we ended up with SHA256.

state. However, this division of the state was a bit arbitrary and began to compromise some other parts of the design.

Ultimately, the split state approach was abandoned in favour of a method called "tree hashing", which is built on a technique called Merkleization⁹³. The remainder of this section explores this approach.

Tree hashing brings two significant advantages over other methods of creating a beacon state digest.

The first advantage is performance. On the face of it, tree hashing is quite inefficient since it requires hashing around double the amount of data to calculate the digest (the root) of a structure compared with the other method of simply hashing the entire serialisation. However, the way that hash trees are constructed in Ethereum 2 allows us to cache the roots of entire subtrees that have not changed. So, for example, by design the list of validator records in the state does not change frequently. As a result we can cache the hash tree root of the list and do not need to recalculate it every time we recalculate the entire beacon state root. Overall this feature results in a huge reduction in the total amount of hashing required to calculate state roots, and is an important part of making the beacon chain protocol usable in practice.

The second advantage is light-client support. Indeed, the original motivation for implementing tree hashing was only about supporting light clients. Tree hashing enables efficient Merkle proofs that allow subsets of the beacon state to be provided to light clients. As long as a light client has the hash tree root by some means it can use the proofs to verify that the provided data is correct.

We will first recap Merkle trees, then extend them to Merkleization, and finally look at the construction of the hash tree root, which is our ultimate goal.

Terminology

The SSZ specification uses the term "Merkleization" to refer to both

- the operation of finding the root of a Merkle tree given its leaves, and
- the operation of finding the hash tree root of an SSZ object.

For didactic purposes I've chosen to distinguish between these more precisely. In the following sections I'll be calling the first "Merkleization", and the second "calculating a hash tree root".

With these definitions, calculating the hash tree root of an SSZ object uses Merkleization, potentially multiple steps of it, but also involves other steps such packing, chunking, and length mix-ins. Moreover, Merkleization always works with full binary trees (the number of leaves is a power of two), whereas hash tree roots can be derived from much more complex binary tree structures.

Merkle Trees

To understand Merkleization we first need to understand Merkle trees. These are not at all new, and date back to the 1970s.

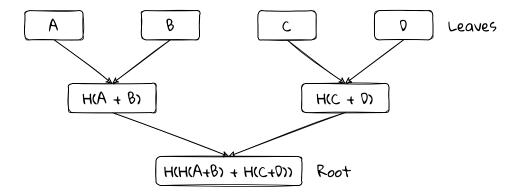
The idea is that we have a set of "leaves", which is our data, and we iteratively reduce those leaves down to a single, short root via hashing. This reduction is done by hashing the leaves in pairs to make a "parent" node. We repeat the process on the parent nodes to make grandparent nodes, and so on to build a binary tree structure that culminates in a single ancestral root. In Merkleization we will be dealing only with structures that have a power of two number of leaves, so we have a full binary tree.

In the following diagram, the leaves are our four blobs of data, A, B, C, and D. These can be any string of data, though in Merkleization they will be 32 byte "chunks". The function H is our hash function, and the operator + concatenates strings. So H(A+B) is the hash of the concatenation of strings A and B^{94} .

⁹³The name Merkleization derives from Merkle trees, which in turn are named for the computer scientist Ralph Merkle.

I believe the noun "Merkleization", though, is ours. I've adopted the majority preferred spelling, which is also the version that made it into the SSZ spec. The ugly version won despite my best efforts.

⁹⁴For some reason, in computer science, trees are traditionally depicted the other way up. Call me eccentric, but I like my trees to have their leaves at the top and their roots at the bottom.



Example of a Merkle tree.

In the Eth2 implementation, each box in the diagram is a 32-byte string of data: either a 32-byte leaf, or the 32-byte output of the hash function. Thus, we obtain the 32-byte root of the tree, which is a "digest" of the data represented by the leaves. The root uniquely represents the data in the leaves; any change in the leaves leads to a different root.

Here's the same thing again on the Python REPL, assigning leaf values as A=1, B=2, C=3 and D=4. We construct the root of the tree starting from the leaves and descending through its levels until reaching the root, H(H(A+B)+H(C+D)). Note that all the leaf values are padded to 32-bytes and are little-endian (as per their SSZ serialisation).

```
>>> from eth2spec.utils.ssz.ssz_typing import uint256
>>> from eth2spec.utils.hash_function import hash
>>> a = uint256(1).to_bytes(length = 32, byteorder='little')
>>> b = uint256(2).to_bytes(length = 32, byteorder='little')
>>> c = uint256(3).to_bytes(length = 32, byteorder='little')
>>> d = uint256(4).to_bytes(length = 32, byteorder='little')
>>> ab = hash(a + b)
>>> cd = hash(c + d)
>>> abcd = hash(ab + cd)
>>> abcd.hex()
'bfe3c665d2e561f13b30606c580cb703b2041287e212ade110f0bfd8563e21bb'
```

Merkle tree constructions are a fairly common way to calculate a digest of a bunch of data, such as a blockchain state. Ethereum 1 uses a more sophisticated version of this called a hexary Merkle-Patricia trie (in Eth1 it's a "trie" not a "tree" for complicated reasons), though there are proposals to simplify that.

An extremely useful feature of Merkle trees is that it is quite efficient to construct inclusion proofs using them. This is critical functionality for light clients, and we will discuss it in depth when we look at Merkle proofs.

Merkleization

The normal way to implement a Merkle tree is to store the entire tree structure in memory or on disk, including all the intermediate levels between the leaves and the root. As leaves are updated the affected nodes in the tree are updated: changing A means updating H(A+B) and then the root, everything else is unchanged.

The difference with Merkleization is that the Merkle tree is computed on-the-fly from the given leaves. We can pick up where we left off from the last REPL session as follows.

```
>>> from eth2spec.utils.merkle_minimal import merkleize_chunks
>>> merkleize_chunks([a, b, c, d]).hex()
'bfe3c665d2e561f13b30606c580cb703b2041287e212ade110f0bfd8563e21bb'
```

The Merkleization function (called merkleize() in the SSZ spec, and merkleize_chunks() in the executable spec) takes a list of 32-byte chunks and returns the root of the tree for which those chunks are the leaves.

The list of chunks passed to merkleize_chunks() can be any length, but will be padded with zero chunks so that the total number of chunks is rounded up to the next whole power of two, such that we conceptually have a full binary tree. Thus, a list of three chunks gets implicitly padded with an extra zero chunk:

```
>>> z = bytearray(32)
>>> merkleize_chunks([a, b, c]).hex()
'66c419026fee8793be7fd0011b9db46b98a79f9c9b640e25317865c358f442db'
>>> merkleize_chunks([a, b, c, z]).hex()
'66c419026fee8793be7fd0011b9db46b98a79f9c9b640e25317865c358f442db'
```

A larger tree width can be provided as a parameter to merkleize_chunks(), and the list will be padded with zero chunks accordingly. This capability is used when dealing with lists and bitlists.

An implementation can do this zero padding "virtually", and can optimise further by pre-computing the various levels of hashes of zero chunks: H(0+0), H(H(0+0)+H(0+0)), and so on. In this way we don't always need to build the whole tree to find the Merkle root.

Note that the Merkleization of a single chunk is always just the chunk itself. This reduces the overall amount of hashing needed.

The Hash Tree Root

The hash tree root is a generalisation of Merkleization that we can apply to the kind of complex, compound data structures we have in the beacon state. Calculating hash tree roots is tightly connected to the type-scheme of Simple Serialize.

Calculating the hash tree root of an SSZ object is recursive. Given a composite SSZ object, we iteratively move through the layers of its structure until we reach a basic type or collection of basic types that we can pack into chunks and Merkleize directly. Then we move back through the structure using the calculated hash tree roots as chunks themselves.

The process of calculating a hash tree root is defined in the Simple Serialize specification, and that's the place to go for the full details. However, in simplified form (once again ignoring the SSZ union type) there are basically two paths to choose from when finding an object's hash tree root.

- For basic types or collections of basic types (lists and vectors), we just pack and Merkleize directly.
- For containers and collections of composite types, we recursively find the hash tree roots of the contents.

The following two rules are a simplified summary of the first six rules listed in the specification.

- If X is an SSZ basic object, a list or vector of basic objects, or a bitlist or bitvector, then hash_tree_root(X) = merkleize_chunks(pack(X)). The pack() function returns a list of chunks that can be Merkleized directly.
- 2. If X is an SSZ container, or a vector or list of composite objects, then the hash tree root is calculated recursively, $hash_tree_root(X) = merkleize_chunks([hash_tree_root(x) for x in X])$. The list comprehension is a list of hash tree roots, which is equivalent to a list of chunks.

We'll see plenty of concrete applications of these two rules in the worked example below.

Packing and Chunking

Merkleization operates on lists of "chunks" which are 32-byte blobs of data. Lists generated by means of step 2 above are already in this form. However, step 1 involves basic objects that require a "packing and chunking" operation prior to Merkleization.

The spec gives the precise rules, but it basically looks like this:

- The object (a basic type, a list/vector of basic types, or a bitlist/bitvector) is serialised via SSZ. The sentinel bit is omitted from the serialisation of bitlist types.
- The serialisation is right-padded with zero bytes up to the next full chunk (32 byte boundary).
- The result is split into a list of 32 byte chunks.
- If necessary, further (virtual) zero chunks will be appended to reach the following total lengths (only lists and bitlists might actually need extra padding):
 - All basic types give a single chunk; no basic type has a serialisation longer than 32 bytes.
 - Bitlist[N] and Bitvector[N]: (N + 255) // 256 (dividing by chunk size in bits and rounding up)
 - List[B, N] and Vector[B, N], where B is a basic type: $(N * size_of(B) + 31) // 32$ (dividing by chunk size in bytes and rounding up)

Containers and composite objects that result from rule 2 will have the following numbers of chunks, including zero-chunk padding where required for lists.

- List[C, N] and Vector[C, N], where C is a composite type: N, since the Merkleization comprises N hash tree roots.
- Containers: len(fields), since there is one hash tree root per field in the container.

It is not immediately obvious why lists and bitlists are padded with zero chunks up to their full maximum lengths, even if these are "virtual" chunks. However, this enables the use of generalised indices which provide a consistent way of creating Merkle proofs against hash tree roots, the topic of our next section.

Recall that, in addition to any padding added here, the Merkleization process will further pad the list with zero chunks to make it up to a power-of-two in length.

Mixing in the length

We want objects that have the same type but different contents to have different hash tree roots. This presents a problem for lists. Consider the list **a** of three elements, and the list **b** which is the same three elements plus a fourth zero element on the end. These are different lists of the same type, but both Merkleize to the same value.

```
>>> from eth2spec.utils.ssz.ssz_typing import uint256, List
>>> from eth2spec.utils.merkle_minimal import merkleize_chunks
>>> a = List[uint256, 4](1, 2, 3).encode_bytes()
>>> b = List[uint256, 4](1, 2, 3, 0).encode_bytes()
>>> merkleize_chunks([a[0:32], a[32:64], a[64:96]])
0x66c419026fee8793be7fd0011b9db46b98a79f9c9b640e25317865c358f442db
>>> merkleize_chunks([b[0:32], b[32:64], b[64:96], b[96:128]])
0x66c419026fee8793be7fd0011b9db46b98a79f9c9b640e25317865c358f442db
```

We need to ensure that a list ending with a zero value has a different hash tree root from the same list without the zero value. To do this, we put lists (and bitlists) through an extra mix_in_length() process that involves hashing a concatenation of the Merkle root of the list and the length of the list. This is equivalent to the Merkleization of two chunks, the first being the Merkle root of the list, the second being its length.

See the diagram for attesting_indices below for an illustration of this in practice.

Bitlists require a similar treatment since we remove the sentinel bit before Merkleizing.

Summaries and Expansions

The SSZ spec describes features of Merkleization called summaries and expansions. These are not explicit functions of Merkleization, but implicitly arise as consequences of the design.

Simply put, anywhere in the process, an entire SSZ object can be replaced with its hash tree root without affecting the final result.

We make use of this in a number of ways. First and foremost is the ability to cache the hash tree roots of any unchanged parts of the state, which makes it practical to recalculate the hash tree root of the whole state when required. For example, if a validator record is unchanged we do not need to recalculate its hash tree root when finding the root of the validator registry. If the validator registry is unchanged, we do not need to recalculate its hash tree root when calculating the full state root.

As another example, consider the BeaconBlock and the BeaconBlockHeader types.

```
class BeaconBlock(Container):
    slot: Slot
    proposer_index: ValidatorIndex
    parent_root: Root
    state_root: Root
    body: BeaconBlockBody

class BeaconBlockHeader(Container):
    slot: Slot
    proposer_index: ValidatorIndex
    parent_root: Root
    state_root: Root
    body_root: Root
```

These differ only in their last fields, body and body_root respectively. If body_root is the hash tree root of the BeaconBlockBody, body, then these two objects will have exactly the same hash tree root. BeaconBlock is the expansion type of BeaconBlockHeader; BeaconBlockHeader is a summary type of BeaconBlock. Proposer slashing reports make use of this fact to save space by stripping out the block bodies and replacing them with their hash tree roots.

The Flashbots MEV-Boost design also makes use of this capability. In the MEV-Boost system validators are required to sign "blinded blocks". That is, blocks for which they do not have the bodies. Since the header is a summary of the block (in the sense we are using the word summary here) the same signature will be valid both for the BeaconBlockHeader and the corresponding full BeaconBlock. This simplifies the protocol design.

Worked example

For this section's worked example we shall revisit our friend, the IndexedAttestation. This gives us nice instances of Merkleizing composite type, list types, and vector types, as well as demonstrating summaries and expansions.

Recall that the IndexedAttestation type is defined as follows,

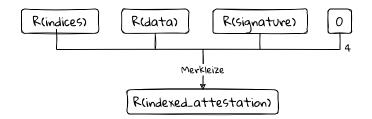
```
class IndexedAttestation(Container):
   attesting_indices: List[ValidatorIndex, MAX_VALIDATORS_PER_COMMITTEE]
   data: AttestationData
   signature: BLSSignature
```

We will create an instance of this just as we did previously, only for brevity I shall call it a, rather than attestation. We want to calculate the hash tree root of this IndexedAttestation, a.

A container's hash tree root is the Merkleization of the list of hash tree roots of the objects it contains (by rule 2). Diagrammatically we are building the following tree and finding its root.

Alternatively, in code, we have the following.

The merkleize_chunks() function is provided by the merkle_minimal.py library. We can apply this function directly as the hash tree roots in the list already constitute chunks. (We could also use the



Calculating the hash tree root of an IndexedAttestation. In this and the following diagrams, R(X) is the Merkleization of X, S(X) is the SSZ serialisation of X. Each box is a 32 byte chunk, and the small digits are the number of leaves in the Merkleization operation.

get_merkle_root() function, but then we'd have to specify a pad_to value of 4 to get a tree of the correct
depth.)

The $attesting_indices$ root

Working down the members of the list, we need the hash tree root of the attesting_indices object, which has type List[ValidatorIndex, MAX_VALIDATORS_PER_COMMITTEE]. This is a list of basic types, namely uint64 since that's the type of ValidatorIndex, and rule 1 applies.

Our attesting_indices list has three elements, [33652, 59750, 92360], which we need to chunk and pad. First we serialise the list as usual with SSZ, then we pad it up to 32 bytes:

This gives us our first chunk. However, the full number of chunks we need is 2048 // 4 = 512 (MAX_VALIDATORS_PER_COMMITTEE divided by uint64s per chunk), so we must add 511 zero chunks. In practice this padding is done "virtually". The merkleize_chunks() function allows us to specify the full number of chunks and takes care of adding the extras. Behind the scenes, it is creating a ten-layer deep Merkle tree with our 512 chunks as leaves and returning the tree's root.

```
>>> merkleize_chunks([serialize(a.attesting_indices) + bytearray(8)], 512).hex()
'04e3bf0951474a6b06dd506648fdf8e84866542614e1c14fa832cd4bebfda0e3'
```

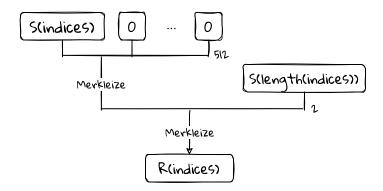
If this were a vector then our work would be done. However, when working with lists, there is a little further wrinkle: as a final step we need to concatenate the root that we have with the actual length of the list and hash them together. This is the mix_in_length() function described above which we implement here by Merkleizing the list's Merkle root with the list's length.

In diagram form the hash tree root calculation for the list looks like this.

The data root

The data field of the IndexedAttestation is another container, an AttestationData object, defined as,

```
class AttestationData(Container):
    slot: Slot
    index: CommitteeIndex
    beacon_block_root: Root
```



Calculating the hash tree root of the attesting_indices. This is a List[uint256, 2048] type, and our example list has three elements, comprising a single chunk. Note the extra mix_in_length() step that's applied to lists.

```
source: Checkpoint
target: Checkpoint
```

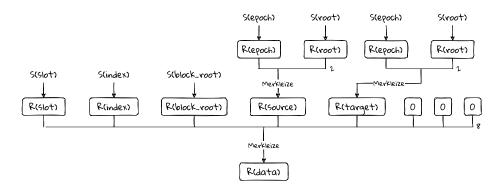
As before, to find the hash tree root of a container, by rule 2 we need the root of the roots it contains. That is,

The Slot and the CommitteeIndex are just basic uint64 types. Their hash tree roots are their little-endian 256-bit representations.

The Root is Bytes32 type, which is equivalent to a Vector[unit8, 32]. Handily, the hash tree root is just the Root value itself since it is only a single chunk.

```
>>> a.data.beacon_block_root.hex()
'4f4250c05956f5c2b87129cf7372f14dd576fc152543bf7042e963196b843fe6'
>>> a.data.beacon_block_root.hash_tree_root().hex()
'4f4250c05956f5c2b87129cf7372f14dd576fc152543bf7042e963196b843fe6'
```

The source and target are once again containers, both having type Checkpoint. The Checkpoint type is simple to Merkleize with the knowledge we have. So, putting everything together, we can find the hash tree root of the data field by hand as follows.

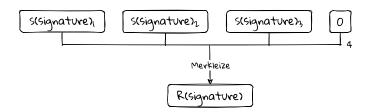


Calculating the hash tree root of an AttestationData container. It contains in turn two Checkpoint containers, source and target.

The signature root

The final part of the IndexedAttestation we need to deal with is the signature field. This is of type Signature, which is a Vector[uint8, 96] and rule 1 applies. This is simple to Merkleize as it is exactly three chunks when packed. The merkleize_chunks() function takes care of adding a single virtual zero chunk to make a power-of-two number of leaves.

```
assert(a.signature.hash_tree_root() ==
    merkleize_chunks([a.signature[0:32], a.signature[32:64], a.signature[64:96]]))
```



Calculating the hash tree root of a Signature, which is really a Bytes96, or Vector[uint8, 96] type.

Putting it all together

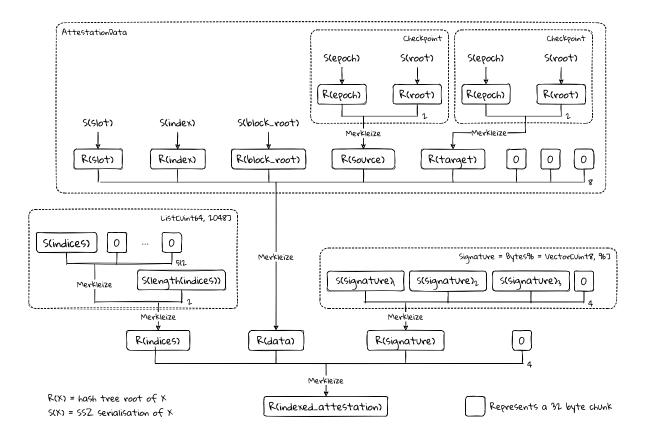
Assembling all these parts we can illustrate in both diagram form and code form how the hash tree root of the IndexedAttestation is calculated from the serialisation of the underlying basic types via repeated applications of Merkleization.

The full picture

The full code

The following code illustrates all the points from the worked example. You can run it by setting up the executable spec as described in the Appendix. If everything goes well the only thing it should print is Success!.

```
from eth2spec.capella import mainnet
from eth2spec.capella.mainnet import *
from eth2spec.utils.ssz.ssz_typing import *
from eth2spec.utils.merkle_minimal import merkleize_chunks
# Initialise an IndexedAttestation type
a = IndexedAttestation(
```



Illustrating the steps required to calculate the hash tree root of an IndexedAttestation. The small digits are the number of leaves in each Merkleization operation.

```
attesting_indices = [33652, 59750, 92360],
    data = AttestationData(
       slot = 3080829,
        index = 9,
        beacon_block_root = '0x4f4250c05956f5c2b87129cf7372f14dd576fc152543bf7042e963196b843fe6',
        source = Checkpoint (
            epoch = 96274,
            root = '0xd24639f2e661bcladcbe7157280776cf76670fff0fee0691f146ab827f4flade'
       ),
        target = Checkpoint(
           epoch = 96275,
            root = '0x9bcd31881817ddeab686f878c8619d664e8bfa4f8948707cba5bc25c8d74915d'
        )
    ),
    signature = '0xaaf504503ff15ae86723c906b4b6bac91ad728e4431aea3be2e8e3acc888d8af'
                + '5dffbbcf53b234ea8e3fde67fbb09120027335ec63cf23f0213cc439e8d1b856'
                + 'c2ddfc1a78ed3326fb9b4fe333af4ad3702159dbf9caeb1a4633b752991ac437'
)
# A container's root is the merkleization of the roots of its fields.
# This is IndexedAttestation.
assert(a.hash_tree_root() == merkleize_chunks(
   ſ
        a.attesting indices.hash tree root(),
        a.data.hash_tree_root(),
        a.signature.hash_tree_root()
    ]))
# A list is serialised then (virtually) padded to its full number of chunks before Merkleization.
# Finally its actual length is mixed in via a further hash/merkleization.
assert(a.attesting_indices.hash_tree_root() ==
       merkleize_chunks(
           Γ
               merkleize chunks([a.attesting indices.encode bytes() + bytearray(8)], 512),
               a.attesting_indices.length().to_bytes(32, 'little')
           ]))
# A container's root is the merkleization of the roots of its fields.
# This is AttestationData.
assert(a.data.hash_tree_root() == merkleize_chunks(
   [
        a.data.slot.hash_tree_root(),
        a.data.index.hash_tree_root(),
        a.data.beacon_block_root.hash_tree_root(),
        a.data.source.hash_tree_root(),
        a.data.target.hash_tree_root()
    ]))
# Expanding the above AttestationData roots by "manually" calculating the roots of its fields.
assert(a.data.hash_tree_root() == merkleize_chunks(
   [
        a.data.slot.to_bytes(32, 'little'),
        a.data.index.to_bytes(32, 'little'),
        a.data.beacon_block_root,
        merkleize chunks([a.data.source.epoch.to bytes(32, 'little'), a.data.source.root]),
        merkleize_chunks([a.data.target.epoch.to_bytes(32, 'little'), a.data.target.root]),
    ]))
# The Signature type has a simple Merkleization.
assert(a.signature.hash_tree_root() ==
       merkleize_chunks([a.signature[0:32], a.signature[32:64], a.signature[64:96]]))
# Putting everything together, we have a "by-hand" Merkleization of the IndexedAttestation.
```

```
assert(a.hash_tree_root() == merkleize_chunks(
    Γ
        # a.attesting indices.hash tree root()
        merkleize_chunks(
            [
                merkleize_chunks([a.attesting_indices.encode_bytes() + bytearray(8)], 512),
                a.attesting_indices.length().to_bytes(32, 'little')
            ]),
        # a.data.hash_tree_root()
        merkleize_chunks(
            [
                a.data.slot.to_bytes(32, 'little'),
                a.data.index.to_bytes(32, 'little'),
                a.data.beacon block root,
                merkleize_chunks([a.data.source.epoch.to_bytes(32, 'little'), a.data.source.root]),
                merkleize_chunks([a.data.target.epoch.to_bytes(32, 'little'), a.data.target.root]),
            ]),
        # a.signature.hash_tree_root()
        merkleize_chunks([a.signature[0:32], a.signature[32:64], a.signature[64:96]])
    ]))
print("Success!")
```

See also

What is a Merkle Tree? by Alin Tomescu is the best primer I have found on Merkle trees, and a great starting point if you are unsure about their construction and properties.

The SSZ specification is the authoritative source for Merkleization as well as serialisation. Many SSZ implementations also include Merkleization.

A formal verification of Merkleization has been performed: Notes and Code.

The Remerkleable library is a Python implementation that introduces some more advanced tools such as backing trees for the data structures. Ztyp is a further exploration of backing trees. Backing trees are a useful approach to representing and maintaining the beacon state within client implementations.

Given the limited type of hashing that's done during Merkleization (always hashing the concatenation of two 32 byte strings), it's worth looking into whether specific performance optimisations are available. Potuz has produced an optimised library, Hashtree, for Merkle tree computation that takes advantage of this.

Generalised indices and Merkle proofs

TODO

Sync Committees

TODO

Networking

Introduction

TODO

Discovery

TODO

 ${\bf Gossip}$

TODO

RPC

TODO

Syncing

TODO

Message Types

TODO

Implementation

Introduction

TODO

Protoarray

TODO

SSZ backing tree

TODO

Batch signature verification

TODO

Slashing protection

TODO

Checkpoint sync

TODO

Part 3: Annotated Specification

Introduction

The beacon chain specification is the guts of the machine. Like the guts of a computer, all the components are showing and the wires are hanging out: everything is on display. In the course of the next sections I will be dissecting the entire core beacon chain specification line by line. My aim is not only to explain how things work, but also to give some historical context: some of the reasoning behind how we ended up where we are today.

Early versions of the specs were written with much more narrative and explanation than today's. Over time, they were coded up in Python for better precision and the benefits of being executable. However, in that process, most of the explanation and intuition was removed.⁹⁵ Vitalik has created his own annotated specifications that covers many of the key insights. It's hard to compete with Vitalik, but my intention here is to go one level deeper in thoroughness and detail. And perhaps to give an independent perspective.

As and when other parts of the book get written I will add links to the specific chapters on each topic (for example on Simple Serialize, consensus, networking).

Note that the online annotated specification is available in two forms:

- divided into chapters in Part 3 of the main book, and
- as a standalone single page that's useful for searching.

The contents of each are identical.

Version information

This edition of Upgrading Ethereum is based on the Capella version of the beacon chain specification, and corresponds to Release v1.3.0, made on the 18th of April, 2023.

There is no single specification document that covers Capella. Rather, we have the Phase 0 specification, the Altair specification changes, the Bellatrix specification changes, and the Capella specification changes. Each builds on top of the previous version in a kind of text-based diff. In addition, these documents are not stable between upgrades. For example, the Phase 0 specs were updated as part of the Capella release. This can all be rather confusing and difficult to track.

To make the whole thing easier to follow in this chapter, I have consolidated all of the specifications to date, (mostly) omitting parts that have been superseded⁹⁶. In general, I have tried to reflect the existing structure of the documents to make them easier to read side-by-side with the original specs. However, I have included the separate BLS document into the flow of this one.

See also

In addition to the spec documents referenced above, a few other current and historical documents exist.

- Vitalik's annotated specifications, covering Phase 0, Altair, The Merge, and beyond.
- Serenity Design Rationale
- Phase 0 for Humans [v0.10.0]
- Phase 0 design notes (Justin Drake)
- My own Phase 0 annotated specification remains available for historical interest.

Hsiao-Wei Wang gave a Lightning Talk on the consensus Pyspec at Devcon VI that briefly describes its structure and how it can be executed.

 $^{^{95}\}mathrm{A}$ process called "Justinification". Iykyk ;-)

⁹⁶You can still find old versions, as described in the Preface.

Types, Constants, Presets, and Configuration

Preamble

For some, a chapter on constants, presets and parameters will seem drier than the Namib Desert, but I've long found these to be a rich and fertile way in to the ideas and mechanisms we'll be unpacking in detail in later chapters. Far from being a desert, this part of the spec bustles with life.

The foundation is laid with a set of custom data types. The beacon chain specification is executable in Python; the data types defined at the top of the spec represent the fundamental quantities that will reappear frequently.

Then – with constants, presets, and parameters – we will examine the numbers that define and constrain the behaviour of the chain. Each of these quantities tells a story. Each parameter encapsulates an insight, or a mechanism, or a compromise. Why is it here? How has it changed over time? Where does its value come from?

Custom Types

The specification defines the following Python custom types, "for type hinting and readability": the data types defined here appear frequently throughout the spec; they are the building blocks for everything else.

Each type has a name, an "SSZ equivalent", and a description. SSZ is the encoding method used to pass data between clients, among other things. Here it can be thought of as just a primitive data type.

Throughout the spec, (almost) all integers are unsigned 64-bit numbers, uint64, but this hasn't always been the case.

Regarding "unsigned", there was much discussion around whether Eth2 should use signed or unsigned integers, and eventually unsigned was chosen. As a result, it is critical to preserve the order of operations in some places to avoid inadvertently causing underflows since negative numbers are forbidden.

And regarding "64-bit", early versions of the spec used other bit lengths than 64 (a "premature optimisation"), but arithmetic integers are now standardised at 64 bits throughout the spec, the only exception being ParticipationFlags, introduced in the Altair upgrade, which has type uint8, and is really a byte type.

Name	SSZ equivalent	Description
Slot	uint64	a slot number
Epoch	uint64	an epoch number
CommitteeIndex	uint64	a committee index at a slot
ValidatorIndex	uint64	a validator registry index
Gwei	uint64	an amount in Gwei
Root	Bytes32	a Merkle root
Hash32	Bytes32	a 256-bit hash
Version	Bytes4	a fork version number
DomainType	Bytes4	a domain type
ForkDigest	Bytes4	a digest of the current fork data
Domain	Bytes32	a signature domain
BLSPubkey	Bytes48	a BLS12-381 public key
BLSSignature	Bytes96	a BLS12-381 signature
ParticipationFlags	uint8	a succinct representation of 8 boolean participation flags
Transaction	<pre>ByteList[MAX_BYTES_PER_ TRANSACTION]</pre>	either a typed transaction envelope or a legacy transaction
ExecutionAddress	Bytes20	Address of account on the execution layer
WithdrawalIndex	uint64	an index of a Withdrawal

me SSZ equivalent Description

Slot

Time is divided into fixed length slots. Within each slot, exactly one validator is randomly selected to propose a beacon chain block. The progress of slots is the fundamental heartbeat of the beacon chain.

Epoch

Sequences of slots are combined into fixed-length epochs.

Epoch boundaries are the points at which the chain can be justified and finalised (by the Casper FFG mechanism). They are also the points at which validator balances are updated, validator committees get shuffled, and validator exits, entries, and slashings are processed. That is, the main state-transition work is performed per epoch, not per slot.

Epochs have always felt like a slightly uncomfortable overlay on top of the slot-by-slot progress of the beacon chain, but necessitated by Casper FFG finality. There have been proposals to move away from epochs, and there are possible future developments that could allow us to do away with epochs entirely. But, for the time being, they remain.

Fun fact: Epochs were originally called Cycles.

CommitteeIndex

Validators are organised into committees that collectively vote (make attestations) on blocks. Each committee is active at exactly one slot per epoch, but several committees are active at each slot. The CommitteeIndex type is an index into the list of committees active at a slot.

The beacon chain's committee-based design is a large part of what makes it practical to implement while maintaining security. If all validators were active all the time, there would be an overwhelming number of messages to deal with. The random shuffling of committees make them very hard to subvert by an attacker without a supermajority of stake.

ValidatorIndex

Each validator making a successful deposit is consecutively assigned a unique validator index number that is permanent, remaining even after the validator exits. It is permanent because the validator's balance is associated with its index, so the data needs to be preserved when the validator exits, at least until the balance is withdrawn at an unknown future time.

Gwei

All Ether amounts on the consensus layer are specified in units of Gwei (10^9 Wei, 10^{-9} Ether). This is basically a hack to avoid having to use integers wider than 64 bits to store validator balances and while doing calculations, since 2^{64} Wei is only 18 Ether. Even so, in some places care needs to be taken to avoid arithmetic overflow when dealing with Ether calculations.

Root

Merkle roots are ubiquitous in the Eth2 protocol. They are a very succinct and tamper-proof way of representing a lot of data, an example of a cryptographic accumulator. Blocks are summarised by their Merkle roots; state is summarised by its Merkle root; the list of Eth1 deposits is summarised by its Merkle root; the digital signature of a message is calculated from the Merkle root of the data structure contained within the message.

Hash32

Merkle roots are constructed with cryptographic hash functions. In the spec, a Hash32 type is used to represent Eth1 block roots (which are also Merkle roots).

I don't know why only the Eth1 block hash has been awarded the Hash32 type: other hashes in the spec remain Bytes32. In early versions of the spec Hash32 was used for all cryptographic has quantities, but this was changed to Bytes32.

Anyway, it's worth taking a moment in appreciation of the humble cryptographic hash function. The hash function is arguably the single most important algorithmic innovation underpinning blockchain technology, and in fact most of our online lives. Easily taken for granted, but utterly critical in enabling our modern world.

Version

Unlike Ethereum 1⁹⁷, the beacon chain has an in-protocol concept of a version number. It is expected that the protocol will be updated/upgraded from time to time, a process commonly known as a "hardfork". For example, the upgrade from Phase 0 to Altair took place on the 27th of October 2021, and was assigned its own fork version. Similarly, the upgrade from Altair to Bellatrix was assigned a different fork version.

Version is used when computing the ForkDigest.

DomainType

DomainType is just a cryptographic nicety: messages intended for different purposes are tagged with different domains before being hashed and possibly signed. It's a kind of name-spacing to avoid clashes; probably unnecessary, but considered a best-practice. Eleven domain types are defined in Capella.

ForkDigest

ForkDigest is the unique chain identifier, generated by combining information gathered at genesis with the current chain Version identifier.

The ForkDigest serves two purposes.

- 1. Within the consensus protocol to prevent, for example, attestations from validators on one fork (that maybe haven't upgraded yet) being counted on a different fork.
- 2. Within the networking protocol to help to distinguish between useful peers that on the same chain, and useless peers that are on a different chain. This usage is described in the Ethereum 2.0 networking specification, where ForkDigest appears frequently.

Specifically, ForkDigest is the first four bytes of the hash tree root of the ForkData object containing the current chain Version and the genesis_validators_root which was created at beacon chain initialisation. It is computed in compute_fork_digest().

Domain

Domain is used when verifying protocol messages validators. To be valid, a message must have been combined with both the correct domain and the correct fork version. It calculated as the concatenation of the four byte DomainType and the first 28 bytes of the fork data root.

BLSPubkey

BLS (Boneh-Lynn-Shacham) is the digital signature scheme used by Eth2. It has some very nice properties, in particular the ability to aggregate signatures. This means that many validators can sign the same message (for example, that they support block X), and these signatures can all be efficiently aggregated into a single signature for verification. The ability to do this efficiently makes Eth2 practical as a protocol. Several other protocols have adopted or will adopt BLS, such as Zcash, Chia, Dfinity and Algorand. We are using the BLS signature scheme based on the BLS12-381 (Barreto-Lynn-Scott) elliptic curve

The BLSPubkey type holds a validator's public key, or the aggregation of several validators' public keys. This is used to verify messages that are claimed to have come from that validator or group of validators.

⁹⁷Ethereum 1.0 introduced a fork identifier as defined in EIP-2124 which is similar to Version, but the Eth1 fork ID is not part of the consensus protocol and is used only in the networking protocol.

In Ethereum 2.0, BLS public keys are elliptic curve points from the BLS12-381 G_1 group, thus are 48 bytes long when compressed.

See the section on BLS signatures in part 2 for a more in-depth look at these things.

BLSSignature

As above, we are using BLS signatures over the BLS12-381 elliptic curve in order to sign messages between participants. As with all digital signature schemes, this guarantees both the identity of the sender and the integrity of the contents of any message.

In Ethereum 2.0, BLS signatures are elliptic curve points from the BLS12-381 G_2 group, thus are 96 bytes long when compressed.

ParticipationFlags

The ParticipationFlags type was introduced in the Altair upgrade as part of the accounting reforms.

Prior to Altair, all attestations seen in blocks were stored in state for two epochs. At the end of an epoch, finality calculations, and reward and penalty calculations for each active validator, would be done by processing all the attestations for the previous epoch as a batch. This created a spike in processing at epoch boundaries, and led to a noticeable increase in late blocks and attestations during the first slots of epochs. With Altair, participation flags are now used to continuously track validators' attestations, reducing the processing load at the end of epochs.

Three of the eight bits are currently used; five are reserved for future use.

As an aside, it might have been more intuitive if ParticipationFlags were a Bytes1 type, rather than introducing a weird uint8 into the spec. After all, it is not used as an arithmetic integer. However, Bytes1 is a composite type in SSZ, really an alias for Vector[uint8, 1], whereas uint8 is a basic type. When computing the hash tree root of a List type, multiple basic types can be packed into a single leaf, while composite types take a leaf each. This would result in 32 times as many hashing operations for a list of Bytes1. For similar reasons the type of ParticipationFlags was changed from bitlist to uint8.

Transaction

The Transaction type was introduced in the Bellatrix pre-Merge upgrade to allow for Ethereum transactions to be included in beacon blocks. It appears in ExecutionPayload objects.

Transactions are completely opaque to the beacon chain and are exclusively handled in the execution layer. A note reflecting this is included in the Bellatrix specification:

Note: The Transaction type is a stub which is not final.

The maximum size of a transaction is MAX_BYTES_PER_TRANSACTION which looks huge, but since the underlying type is an SSZ ByteList (which is a List), a Transaction object will only occupy as much space as necessary.

ExecutionAddress

The ExecutionAddress type was introduced in the Bellatrix pre-Merge upgrade to represent the fee recipient on the execution chain for beacon blocks that contain transactions. It is a normal, 20-byte, Ethereum address, and is used in the ExecutionPayload class.

WithdrawalIndex

The WithdrawalIndex keeps track of the total number of withdrawal transactions made from the consensus layer to the execution layer. All nodes store this number in their state, so a block containing withdrawal transactions that have unexpected withdrawal indices is invalid.

At the maximum rate of 16 withdrawals per slot, a uint64 will take 438 billion years to overflow. This ought to be enough.

References

- A primer on Merkle roots.
 - See also Wikipedia on Merkle Trees.
- I have written an intro to the BLS12-381 elliptic curve elsewhere.

Constants

The distinction between "constants", "presets", and "configuration values" is not always clear, and things have moved back and forth between the sections at times⁹⁸. In essence, "constants" are things that are expected never to change for the beacon chain, no matter what fork or test network it is running.

Miscellaneous

Name	Value
GENESIS_SLOT	Slot(0)
GENESIS_EPOCH	Epoch(0)
FAR_FUTURE_EPOCH	Epoch(2**64 - 1)
DEPOSIT_CONTRACT_TREE_DEPTH	uint64(2**5) $(=32)$
JUSTIFICATION_BITS_LENGTH	uint64(4)
PARTICIPATION_FLAG_WEIGHTS	<pre>[TIMELY_SOURCE_WEIGHT, TIMELY_TARGET_WEIGHT, TIMELY_HEAD_WEIGHT]</pre>
ENDIANNESS	'little'

GENESIS_SLOT

The very first slot number for the beacon chain is zero.

Perhaps this seems uncontroversial, but it actually featured heavily in the Great Signedness Wars mentioned previously. The issue was that calculations on unsigned integers might have negative intermediate values, which would cause problems. A proposed work-around for this was to start the chain at a non-zero slot number. It was initially set to 2^19, then 2^63, then 2^32, and finally back to zero. In my humble opinion, this madness only confirms that we should have been using signed integers all along.

GENESIS_EPOCH

As above. When the chain starts, it starts at epoch zero.

FAR_FUTURE_EPOCH

A candidate for the dullest constant. It's used as a default initialiser for validators' activation and exit times before they are properly set. No epoch number will ever be bigger than this one.

DEPOSIT_CONTRACT_TREE_DEPTH

DEPOSIT_CONTRACT_TREE_DEPTH specifies the size of the (sparse) Merkle tree used by the Eth1 deposit contract to store deposits made. With a value of 32, this allows for $2^{32} = 4.3$ billion deposits. Given that the minimum deposit it 1 Ether, that number is clearly enough.

Since deposit receipts contain Merkle proofs, their size depends on the value of this constant.

⁹⁸See Issue 2390 for discussion and a rationale for the current categorisation into constants, presets, and configuration variables.

JUSTIFICATION BITS LENGTH

As an optimisation to Casper FFG – the process by which finality is conferred on epochs – the beacon chain uses a "k-finality" rule. We will describe this more fully when we look at processing justification and finalisation. For now, this constant is just the number of bits we need to store in state to implement k-finality. With k = 2, we track the justification status of the last four epochs.

PARTICIPATION_FLAG_WEIGHTS

This array is just a convenient way to access the various weights given to different validator achievements when calculating rewards. The three weights are defined under incentivization weights, and each weight corresponds to a flag stored in state and defined under participation flag indices.

ENDIANNESS

Endianness refers to the order of bytes in the binary representation of a number: most-significant byte first is big-endian; least-significant byte first is little-endian. For the most part, these details are hidden by compilers, and we don't need to worry about endianness. But endianness matters when converting between integers and bytes, which is relevant to shuffling and proposer selection, the RANDAO, and when serialising with SSZ.

The spec began life as big-endian, but the Nimbus team from Status successfully lobbied for it to be changed to little-endian in order to better match processor hardware implementations, and the endianness of WASM. SSZ was changed first, and then the rest of the spec followed.

Participation flag indices

Name	Value
TIMELY_SOURCE_FLAG_INDEX	0
TIMELY_TARGET_FLAG_INDEX	1
TIMELY_HEAD_FLAG_INDEX	2

Validators making attestations that get included on-chain are rewarded for three things:

- getting attestations included with the correct source checkpoint within 5 slots (integer_squareroot(SLOTS_PER_EPOCH));
- getting attestations included with the correct target checkpoint within 32 slots (SLOTS_PER_EPOCH); and,
- getting attestations included with the correct head within 1 slot (MIN_ATTESTATION_INCLUSION_DELAY), basically immediately.

These flags are temporarily recorded in the BeaconState when attestations are processed, then used at the ends of epochs to update finality and to calculate validator rewards for making attestations.

The mechanism for rewarding timely inclusion of attestations (thus penalising late attestations) differs between Altair and Phase 0. In Phase 0, attestations included within 32 slots would receive the full reward for the votes they got correct (source, target, head), plus a declining reward based on the delay in inclusion: $\frac{1}{2}$ for a two slot delay, $\frac{1}{3}$ for a three slot delay, and so on. With Altair, for each vote, we now have a cliff before which the validator receives the full reward and after which a penalty. The cliffs differ in duration, which is intended to more accurately target incentives at behaviours that genuinely help the chain (there is little value in rewarding a correct head vote made 30 slots late, for example). See get_attestation_participation_flag_indices() for how this is implemented in code.

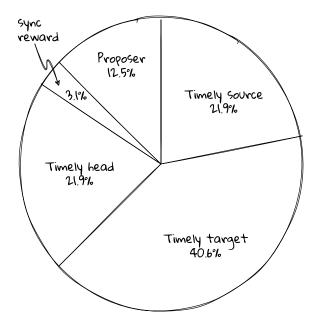
Incentivization weights

Name	Value
TIMELY_SOURCE_WEIGHT	uint64(14)
TIMELY_TARGET_WEIGHT	uint64(26)
TIMELY_HEAD_WEIGHT	uint64(14)
SYNC_REWARD_WEIGHT	uint64(2)
PROPOSER_WEIGHT	uint64(8)
WEIGHT_DENOMINATOR	uint64(64)

These weights are used to calculate the reward earned by a validator for performing its duties. There are five duties in total. Three relate to making attestations: attesting to the source epoch, attesting to the target epoch, and attesting to the head block. There are also rewards for proposing blocks, and for participating in sync committees. Note that the sum of the five weights is equal to WEIGHT_DENOMINATOR.

On a long-term average, a validator can expect to earn a total amount of get_base_reward() per epoch, with these weights being the relative portions for each of the duties comprising that total. Proposing blocks and participating in sync committees do not happen in every epoch, but are randomly assigned, so over small periods of time validator earnings may differ from get_base_reward().

The apportioning of rewards was overhauled in the Altair upgrade to better reflect the importance of each activity within the protocol. The total reward amount remains the same, but sync committee rewards were added, and the relative weights were adjusted. Previously, the weights corresponded to 16 for correct source, 16 for correct target, 16 for correct head, 14 for inclusion (equivalent to correct source), and 2 for block proposals. The factor of four increase in the proposer reward addressed a long-standing spec bug.



The proportion of the total reward derived from each of the micro-rewards.

Withdrawal Prefixes

Name	Value
BLS_WITHDRAWAL_PREFIX	Bytes1('0x00')
ETH1_ADDRESS_WITHDRAWAL_PREFIX	Bytes1('0x01')

Withdrawal prefixes relate to the withdrawal credentials provided when deposits are made for validators.

Two ways to specify the withdrawal credentials are currently available, versioned with these prefixes, with others such as 0×02 and 0×03 under discussion.

When processing deposits onto the consensus layer, the withdrawal_credential of the deposit is not checked in any way. It's up to the depositor to ensure that they are using the correct prefix and contents to be able to receive their rewards and retrieve their stake back after exiting the consensus layer. This also means that we can potentially introduce new types of withdrawal credentials at any time, enabling them later with a hard fork, just as we did with 0×01 credentials ahead of the Capella upgrade that began using them.

BLS WITHDRAWAL PREFIX

The beacon chain launched with only BLS-style withdrawal credentials available, so all early stakers used this.

It was not at all clear in the early days what accounts on Ethereum 2.0 would look like, and what addressing scheme they might use. The 0×00 credential created a placeholder or commitment to a future withdrawal credential change.

With this type of credential, in addition to a BLS signing key, stakers have a second BLS "withdrawal" key. Since the Capella upgrade, stakers have been able to use their withdrawal key to sign a message instructing the consensus layer to change its withdrawal credential from type 0x00 to type 0x01.

The credential registered in the deposit data is the 32 byte SHA256 hash of the validator's withdrawal public key, with the first byte set to 0x00 (BLS WITHDRAWAL PREFIX).

ETH1_ADDRESS_WITHDRAWAL_PREFIX

Eth1 withdrawal credentials are much simpler, and were adopted once it became clear that Ethereum 2.0 would not be using a BLS-based address scheme for accounts at any time soon. The Capella upgrade enables automatic partial and full withdrawals of validators' balances from the beacon chain to normal Ethereum accounts and wallets.

An Eth1 withdrawal credential looks like the byte 0x01 (ETH1_ADDRESS_WITHDRAWAL_PREFIX), followed by eleven 0x00 bytes, followed by the 20-byte Ethereum address of the destination account.

In addition to enabling withdrawal transactions for validators having 0x01 Eth1 credentials, the Capella upgrade gives validators with old 0x00 BLS style credentials the opportunity to make a one-time change from BLS to Eth1 withdrawal credentials⁹⁹.

Domain types

Name	Value
DOMAIN_BEACON_PROPOSER	DomainType('0x00000000')
DOMAIN_BEACON_ATTESTER	DomainType('0x01000000')
DOMAIN_RANDAO	DomainType('0x02000000')
DOMAIN_DEPOSIT	DomainType('0x03000000')
DOMAIN_VOLUNTARY_EXIT	DomainType('0x04000000')
DOMAIN_SELECTION_PROOF	DomainType('0x05000000')
DOMAIN_AGGREGATE_AND_PROOF	DomainType('0x06000000')
DOMAIN_SYNC_COMMITTEE	DomainType('0x07000000')
DOMAIN_SYNC_COMMITTEE_SELECTION_PROOF	DomainType('0x08000000')
DOMAIN_CONTRIBUTION_AND_PROOF	DomainType('0x09000000')
DOMAIN_BLS_TO_EXECUTION_CHANGE	<pre>DomainType('0x0A000000')</pre>

These domain types are used in three ways: for seeds, for signatures, and for selecting aggregators.

⁹⁹Fun fact: at the point of the Capella upgrade, out of 567,144 total validators, 322,491 (56.9%) had 0x00 BLS withdrawal credentials and 244,653 (43.1%) had 0x01 Eth1 withdrawal credentials.

As seeds

When random numbers are required in-protocol, one way they are generated is by hashing the RANDAO mix with other quantities, one of them being a domain type (see get_seed()). The original motivation was to avoid occasional collisions between Phase 0 committees and Phase 1 persistent committees, back when they were a thing. So, when computing the beacon block proposer, DOMAIN_BEACON_PROPOSER is hashed into the seed, when computing attestation committees, DOMAIN_BEACON_ATTESTER is hashed in, and when computing sync committees, DOMAIN_SYNC_COMMITTEE is hashed in.

See the Randomness chapter for more information.

As signatures

In addition, as a cryptographic nicety, each of the protocol's signature types is augmented with the appropriate domain before being signed:

- Signed block proposals incorporate DOMAIN BEACON PROPOSER
- Signed attestations incorporate DOMAIN_BEACON_ATTESTER
- RANDAO reveals are BLS signatures, and use DOMAIN RANDAO
- Deposit data messages incorporate DOMAIN_DEPOSIT
- Validator voluntary exit messages incorporate DOMAIN VOLUNTARY EXIT
- $\bullet \ \ {\rm Sync\ committee\ signatures\ incorporate\ DOMAIN_SYNC_COMMITTEE}$
- BLS withdrawal credential change messages incorporate DOMAIN_BLS_TO_EXECUTION_CHANGE

For most of these, the fork version is also incorporated before signing. This allows validators to participate, if they wish, in two independent forks of the beacon chain without fear of being slashed.

However, the user-signed messages for deposits (DOMAIN_DEPOSIT) and for BLS withdrawal credential changes (DOMAIN_BLS_TO_EXECUTION_CHANGE) do not incorporate the fork version when signed. This makes them valid across all forks, which is a usability enhancement.

Voluntary exit messages (DOMAIN_VOLUNTARY_EXIT) are a bit of an anomaly in that they are user signed but also incorporate the fork version, meaning that they expire after two upgrades (voluntary exit messages signed in Phase 0 or Altair are no longer valid in Capella). There is some discussion about making voluntary exits non-expiring in future.

See the BLS signatures chapter for more information.

Aggregator selection

The remaining four types, suffixed _PROOF are not used directly in the beacon chain specification. They were introduced to implement attestation subnet validations for denial of service resistance. The technique was extended to sync committees with the Altair upgrade.

Briefly, at each slot, validators are selected to aggregate attestations from their committees. The selection is done based on the validator's signature over the slot number, mixing in <code>DOMAIN_SELECTION_PROOF</code>. The validator then signs the whole aggregated attestation, including the previous signature as proof that it was selected to be a validator, using <code>DOMAIN_AGGREGATE_AND_PROOF</code>. And similarly for sync committees. In this way, everything is verifiable and attributable, making it hard to flood the network with fake messages.

These four are not part of the consensus-critical state-transition, but are nonetheless important to the healthy functioning of the chain.

This mechanism is described in the Phase 0 honest validator spec for attestation aggregation, and in the Altair honest validator spec for sync committee aggregation.

See the Aggregator Selection chapter for more information.

Crypto

Name	Value		
G2_POINT_AT_INFINITY	BLSSignature(b'\xc0' + b'\x00' * 95)		

This is the compressed serialisation of the "point at infinity", the identity point, of the G2 group of the BLS12-381 curve that we are using for signatures. Note that it is in big-endian format (unlike all other constants in the spec).

It was introduced as a convenience when verifying aggregate signatures that contain no public keys in eth_fast_aggregate_verify(). The underlying FastAggregateVerify function from the BLS signature standard would reject these.

G2_POINT_AT_INFINITY is described in the separate BLS Extensions document, but included here for convenience.

Preset

The "presets" are consistent collections of configuration variables that are bundled together. The specs repo currently defines two sets of presets, mainnet and minimal. The mainnet configuration is running in production on the beacon chain; minimal is often used for testing. Other configurations are possible. For example, Teku uses a swift configuration for acceptance testing.

All the values discussed below are from the mainnet configuration.

You'll notice that most of these values are powers of two. There's no huge significance to this. Computer scientists think it's neat, and it ensures that things cleanly divide other things in general. There is a view that this practice helps to minimise bike-shedding (endless arguments over trivial matters).

Some of the configuration parameters below are quite technical and perhaps obscure. I'll take the opportunity here to introduce some concepts, and give more detailed explanations when they appear in later chapters.

Misc

Name	Value
MAX_COMMITTEES_PER_SLOT	uint64(2**6) (= 64)
TARGET_COMMITTEE_SIZE	uint64(2**7) $(= 128)$
MAX_VALIDATORS_PER_COMMITTEE	uint64(2**11) $(=2,048)$
SHUFFLE_ROUND_COUNT	uint64(90)

MAX COMMITTEES PER SLOT

Validators are organised into committees to do their work. At any one time, each validator is a member of exactly one beacon chain committee, and is called on to make an attestation exactly once per epoch. An attestation is a vote for, or a statement of, the validator's view of the chain at that point in time.

On the beacon chain, up to 64 committees are active in a slot and effectively act as a single committee as far as the fork-choice rule is concerned. They all vote on the proposed block for the slot, and their votes/attestations are pooled. In a similar way, all committees active during an epoch (that is, the whole active validator set) act effectively as a single committee as far as justification and finalisation are concerned.

The number 64 was intended to map to one committee per shard once data shards were deployed in the now abandoned Phase 1 of the Ethereum 2.0 roadmap. The plan was for each committee to also vote on one shard crosslink, for a total of 64 shards. We are no longer going down that path, but the committees remain at each slot.

All the above is discussed further in the section on Committees.

Note that sync committees are a different thing: there is only one sync committee active at any time.

TARGET COMMITTEE SIZE

To achieve a desirable level of security, committees need to be larger than a certain size. This makes it infeasible for an attacker to randomly end up with a super-majority in a committee even if they control a significant number of validators. The target here is a kind of lower-bound on committee size. If there are not enough validators for all committees to have at least 128 members, then, as a first measure, the number of committees per slot is reduced to maintain this minimum. Only if there are fewer than SLOTS_PER_EPOCH * TARGET_COMMITTEE_SIZE = 4096 validators in total will the committee size be reduced below TARGET_COMMITTEE_SIZE. With so few validators, the system would be insecure in any case.

For further discussion and an explanation of how the value of TARGET_COMMITTEE_SIZE was set, see the section on committees.

MAX_VALIDATORS_PER_COMMITTEE

This is just used for sizing some data structures, and is not particularly interesting. Reaching this limit would imply over 4 million active validators, staked with a total of 128 million Ether, which exceeds the total supply today.

SHUFFLE_ROUND_COUNT

The beacon chain implements a rather interesting way of shuffling validators in order to select committees, called the "swap-or-not shuffle". This shuffle proceeds in rounds, and the degree of shuffling is determined by the number of rounds, SHUFFLE_ROUND_COUNT. The time taken to shuffle is linear in the number of rounds, so for light-weight, non-mainnet configurations, the number of rounds can be reduced.

The value 90 was introduced in Vitalik's initial commit without explanation. The original paper describing the shuffling technique seems to suggest that a cryptographically safe number of rounds is $6 \log N$. With 90 rounds, then, we should be good for shuffling 3.3 million validators, which is close to the maximum number possible (given the Ether supply).

Hysteresis parameters

Name	Value
HYSTERESIS_QUOTIENT	uint64(4)
HYSTERESIS_DOWNWARD_MULTIPLIER	uint64(1)
HYSTERESIS_UPWARD_MULTIPLIER	uint64(5)

The parameters prefixed HYSTERESIS_ control the way that effective balance is changed (see EFFECTIVE_BALANCE_INCREMENT). As described there, the effective balance of a validator follows changes to the actual balance in a step-wise way, with hysteresis applied. This ensures that the effective balance does not change often.

The original hysteresis design had an unintended effect that might have encouraged stakers to over-deposit or make multiple deposits in order to maintain a balance above 32 Ether at all times. If a validator's balance were to drop below 32 Ether soon after depositing, however briefly, the effective balance would have immediately dropped to 31 Ether and taken a long time to recover. This would have resulted in a 3% reduction in rewards for a period.

This problem was addressed by making the hysteresis configurable via these parameters. Specifically, these settings mean:

- 1. if a validators' balance falls 0.25 Ether below its effective balance, then its effective balance is reduced by 1 Ether
- 2. if a validator's balance rises 1.25 Ether above its effective balance, then its effective balance is increased by 1 Ether

These calculations are done in process_effective_balance_updates() during end of epoch processing.

Gwei values

Name	Value
MIN_DEPOSIT_AMOUNT	Gwei(2**0 * 10**9) $(=1,000,000,000)$
MAX_EFFECTIVE_BALANCE	Gwei(2**5 * 10**9) $(=32,\!000,\!000,\!000)$
EFFECTIVE_BALANCE_INCREMENT	$\texttt{Gwei(2**0 * 10**9)} \ (= 1,\!000,\!000,\!000)$

MIN_DEPOSIT_AMOUNT

MIN_DEPOSIT_AMOUNT is not actually used anywhere within the beacon chain specification document. Rather, it is enforced in the deposit contract that was deployed to the Ethereum 1 chain. Any amount less than this value sent to the deposit contract is reverted.

Allowing stakers to make deposits smaller than a full stake is useful for topping-up a validator's balance if its effective balance has dropped below 32 Ether in order to maintain full productivity. However, this actually led to a vulnerability for some staking pools, involving the front-running of deposits. In some circumstances, a front-running attacker could change a genuine depositor's withdrawal credentials to their own.

MAX EFFECTIVE BALANCE

There is a concept of "effective balance" for validators: whatever a validator's total balance, its voting power is weighted by its effective balance, even if its actual balance is higher. Effective balance is also the amount on which all rewards, penalties, and slashings are calculated - it's used a lot in the protocol

The MAX_EFFECTIVE_BALANCE is the highest effective balance that a validator can have: 32 Ether. Any balance above this is ignored. Note that this means that staking rewards don't compound in the usual case (unless a validator's effective balance somehow falls below 32 Ether, in which case rewards kind of compound).

There is a discussion in the Design Rationale of why 32 Ether was chosen as the staking amount. In short, we want enough validators to keep the chain both alive and secure under attack, but not so many that the message overhead on the network becomes too high.

EFFECTIVE_BALANCE_INCREMENT

Throughout the protocol, a quantity called "effective balance" is used instead of the validators' actual balances. Effective balance tracks the actual balance, with two differences: (1) effective balance is capped at MAX_EFFECTIVE_BALANCE no matter how high the actual balance of a validator is, and (2) effective balance is much more granular - it changes only in steps of EFFECTIVE_BALANCE_INCREMENT rather than Gwei.

This discretisation of effective balance is intended to reduce the amount of hashing required when making state updates. The goal is to avoid having to re-calculate the hash tree root of validator records too often. Validators' actual balances, which change frequently, are stored as a contiguous list in BeaconState, outside validators' records. Effective balances are stored inside validators' individual records, which are more costly to update (more hashing required). So we try to update effective balances relatively infrequently.

Effective balance is changed according to a process with hysteresis to avoid situations where it might change frequently. See HYSTERESIS QUOTIENT.

You can read more about effective balance in the Design Rationale and in this article.

Time parameters

Name	Value	Unit	Duration
MIN_ATTESTATION_INCLUSION_DELAY	uint64(2**0) (= 1)	slots	12 seconds
SLOTS_PER_EPOCH	uint64(2**5) $(=32)$	slots	6.4 minutes

Name	Value	Unit	Duration
MIN_SEED_LOOKAHEAD	uint64(2**0) $(=1)$	epochs	6.4 minutes
MAX_SEED_LOOKAHEAD	uint64(2**2) $(=4)$	epochs	25.6 minutes
MIN_EPOCHS_TO_INACTIVITY_PENALTY	uint64(2**2) $(=4)$	epochs	25.6 minutes
EPOCHS_PER_ETH1_VOTING_PERIOD	uint64(2**6) $(=64)$	epochs	$\sim 6.8 \text{ hours}$
SLOTS_PER_HISTORICAL_ROOT	uint64(2**13) $(=8,192)$	slots	$\sim 27 \text{ hours}$

MIN ATTESTATION INCLUSION DELAY

A design goal of Ethereum 2.0 is not to heavily disadvantage validators that are running on lower-spec systems, or, conversely, to reduce any advantage gained by running on high-spec systems.

One aspect of performance is network bandwidth. When a validator becomes the block proposer, it needs to gather attestations from the rest of its committee. On a low-bandwidth link, this takes longer, and could result in the proposer not being able to include as many past attestations as other better-connected validators might, thus receiving lower rewards.

MIN_ATTESTATION_INCLUSION_DELAY was an attempt to "level the playing field" by setting a minimum number of slots before an attestation can be included in a beacon block. It was originally set at 4, with a 6-second slot time, allowing 24 seconds for attestations to propagate around the network.

It was later set to one – attestations are included as early as possible – and MIN_ATTESTATION_INCLUSION_ DELAY exists today as a relic of the earlier design. The current slot time of 12 seconds is assumed to allow sufficient time for attestations to propagate and be aggregated sufficiently within one slot.

SLOTS PER EPOCH

We currently have 12-second slots and 32-slot epochs. In earlier designs, slots were 6 seconds and there were 64 slots per epoch. So the time between epoch boundaries was unchanged when slots were lengthened.

The choice of 32 slots per epoch is a trade-off between time to finality (we need two epochs to finalise, so we prefer to keep them as short as we can) and being as certain as possible that at least one honest proposer per epoch will make a block to update the RANDAO (for which we prefer longer epochs).

In addition, epoch boundaries are where the heaviest part of the beacon chain state-transition calculation occurs, so that's another reason for not having them too close together.

Since every validator attests one every epoch, there is an interplay between the number of slots per epoch, the number of committees per slot, committee sizes, and the total number of validators.

MIN SEED LOOKAHEAD

A random seed is used to select all the committees and proposers for an epoch. During each epoch, the beacon chain accumulates randomness from proposers via the RANDAO and stores it. The seed for the current epoch is based on the RANDAO output from the epoch MIN_SEED_LOOKAHEAD + 1 ago. With MIN_SEED_LOOKAHEAD set to one, the effect is that we can know the seed for the current epoch and the next epoch, but not beyond, since the next-but-one epoch depends on randomness from the current epoch that hasn't been accumulated yet.

This mechanism is designed to allow sufficient time for members of newly formed committees to find each other on the peer-to-peer network, while preventing committee makeup being known too far ahead limits the opportunity for coordinated collusion between validators.

MAX SEED LOOKAHEAD

The above notwithstanding, if an attacker has a large proportion of the stake, or is, for example, able to DoS block proposers for a while, then it might be possible for the attacker to predict the output of the RANDAO further ahead than MIN_SEED_LOOKAHEAD would normally allow. This might enable the attacker to manipulate committee memberships to their advantage by performing well-timed exits and activations of their validators.

To prevent this, we assume a maximum feasible lookahead that an attacker might achieve (MAX_SEED_LOOKAHEAD) and delay all activations and exits by this amount, which allows new randomness to come in via block proposals from honest validators. With MAX_SEED_LOOKAHEAD set to 4, if only 10% of validators are online and honest, then the chance that an attacker can succeed in forecasting the seed beyond (MAX_SEED_LOOKAHEAD - MIN_SEED_LOOKAHEAD) = 3 epochs is $0.9^{3\times32}$, which is about 1 in 25,000.

MIN_EPOCHS_TO_INACTIVITY_PENALTY

The inactivity penalty is discussed below. This parameter sets the length of time until it kicks in. If the last finalised epoch is longer ago than MIN_EPOCHS_TO_INACTIVITY_PENALTY, then the beacon chain starts operating in "leak" mode. In this mode, participating validators no longer get rewarded, and validators that are not participating get penalised.

EPOCHS_PER_ETH1_VOTING_PERIOD

In order to safely onboard new validators, the beacon chain needs to take a view on what the Eth1 chain looks like. This is done by collecting votes from beacon block proposers - they are expected to consult an available Eth1 client in order to construct their vote.

EPOCHS_PER_ETH1_VOTING_PERIOD * SLOTS_PER_EPOCH is the total number of votes for Eth1 blocks that are collected. As soon as half of this number of votes are for the same Eth1 block, that block is adopted by the beacon chain and deposit processing can continue. This processing is done in process_eth1_data().

Rules for how validators select the right block to vote for are set out in the validator guide. ETH1_FOLLOW_DISTANCE is the (approximate) minimum depth of block that can be considered.

This parameter was increased from 32 to 64 epochs for the beacon chain mainnet. This increase is intended to allow devs more time to respond if there is any trouble on the Eth1 chain, in addition to the eight hours grace provided by ETH1_FOLLOW_DISTANCE.

For a detailed analysis of these parameters, see this article.

SLOTS_PER_HISTORICAL_ROOT

There have been several redesigns of the way the beacon chain stores its past history. The current design is a double batched accumulator. The block root and state root for every slot are stored in the state for SLOTS_PER_HISTORICAL_ROOT slots. When those lists are full, each list is Merkleized separately, and their roots are added to the ever-growing state.historical_summaries list within an HistoricalSummary container.

State list lengths

The following parameters set the sizes of some lists in the beacon chain state. Some lists have natural sizes, others such as the validator registry need an explicit maximum size to guide SSZ serialisation.

Name	Value	Unit	Duration
EPOCHS_PER_HISTORICAL_VECTOR	uint64(2**16) $(=65,536)$	epochs	~0.8 years
EPOCHS_PER_SLASHINGS_VECTOR	uint64(2**13) $(=8,192)$	epochs	$\sim 36 \text{ days}$
HISTORICAL_ROOTS_LIMIT	uint64(2**24) $(=16,777,216)$	historical roots	\sim 52,262 years
VALIDATOR_REGISTRY_LIMIT	uint64(2**40) $(=1,099,511,627,776)$	validators	-

EPOCHS PER HISTORICAL VECTOR

This is the number of epochs of previous RANDAO mixes that are stored (one per epoch). Having access to past randao mixes allows historical shufflings to be recalculated. Since Validator records keep track of the activation and exit epochs of all past validators, we can reconstitute past committees as far back as we have the RANDAO values. This information can be used for slashing long-past attestations, for example. It is not clear how the value of this parameter was decided.

EPOCHS_PER_SLASHINGS_VECTOR

In the epoch in which a misbehaving validator is slashed, its effective balance is added to an accumulator in the state. In this way, the state.slashings list tracks the total effective balance of all validators slashed during the last EPOCHS_PER_SLASHINGS_VECTOR epochs.

At a time EPOCHS_PER_SLASHINGS_VECTOR // 2 after being slashed, a further penalty is applied to the slashed validator, based on the total amount of value slashed during the 4096 epochs before and the 4096 epochs after it was originally slashed.

The idea of this is to disproportionately punish coordinated attacks, in which many validators break the slashing conditions around the same time, while only lightly penalising validators that get slashed by making a mistake. Early designs for Eth2 would always slash a validator's entire deposit.

See also PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX.

HISTORICAL ROOTS LIMIT

Every SLOTS_PER_HISTORICAL_ROOT slots, the list of block roots and the list of state roots in the beacon state are Merkleized and added to state.historical_roots list. Although state.historical_roots is in principle unbounded, all SSZ lists must have maximum sizes specified. The size HISTORICAL_ROOTS_LIMIT will be fine for the next few millennia, after which it will be somebody else's problem. The list grows at less than 10 KB per year.

Storing past roots like this allows Merkle proofs to be constructed about anything in the beacon chain's history if required.

VALIDATOR REGISTRY LIMIT

Every time the Eth1 deposit contract processes a deposit from a new validator (as identified by its public key), a new entry is appended to the state.validators list.

In the current design, validators are never removed from this list, even after exiting from being a validator. This is largely because there is nowhere yet to send a validator's remaining deposit and staking rewards, so they continue to need to be tracked in the beacon chain.

The maximum length of this list is VALIDATOR_REGISTRY_LIMIT, which is one trillion, so we ought to be OK for a while, especially given that the minimum deposit amount is 1 Ether.

Rewards and penalties

Name	Value
BASE_REWARD_FACTOR	uint64(2**6) $(=64)$
WHISTLEBLOWER_REWARD_QUOTIENT	uint64(2**9) $(=512)$
PROPOSER_REWARD_QUOTIENT	uint64(2**3) (= 8)
INACTIVITY_PENALTY_QUOTIENT	${\tt uint64(2**26)}\ (=67{,}108{,}864)$
MIN_SLASHING_PENALTY_QUOTIENT	uint64(2**7) $(=128)$
PROPORTIONAL_SLASHING_MULTIPLIER	uint64(1)
INACTIVITY_PENALTY_QUOTIENT_ALTAIR	uint64(3 * 2**24) (= 50,331,648)
MIN_SLASHING_PENALTY_QUOTIENT_ALTAIR	${\tt uint64(2**6)}\ (=64)$
PROPORTIONAL_SLASHING_MULTIPLIER_ALTAIR	uint64(2)
INACTIVITY_PENALTY_QUOTIENT_BELLATRIX	${\tt uint64(2**24)}\ (=16{,}777{,}216)$
MIN_SLASHING_PENALTY_QUOTIENT_BELLATRIX	uint64(2**5) $(=32)$
PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX	uint64(3)

Note that there are similar constants with different values here.

• The original beacon chain Phase 0 constants have no suffix.

- Constants updated in the Altair upgrade have the suffix ALTAIR.
- Constants updated in the Bellatrix upgrade have the suffix BELLATRIX.

This is explained in the specs repo as follows:

Variables are not replaced but extended with forks. This is to support syncing from one state to another over a fork boundary, without hot-swapping a config. Instead, for forks that introduce changes in a variable, the variable name is suffixed with the fork name.

BASE REWARD FACTOR

This is the big knob to turn to change the issuance rate of Eth2. Almost all validator rewards are calculated in terms of a "base reward per increment" which is formulated as,

```
EFFECTIVE_BALANCE_INCREMENT * BASE_REWARD_FACTOR // integer_squareroot(get_total_active_balance(state))
```

Thus, the total validator rewards per epoch (the Eth2 issuance rate) could be tuned by increasing or decreasing BASE_REWARD_FACTOR.

The exception is proposer rewards for including slashing reports in blocks. However, these are more than offset by the amount of stake burnt, so do not increase the overall issuance rate.

WHISTLEBLOWER REWARD QUOTIENT

One reward that is not tied to the base reward is the whistleblower reward. This is an amount awarded to the proposer of a block containing one or more proofs that a proposer or attester has violated a slashing condition. The whistleblower reward is set at $\frac{1}{512}$ of the effective balance of the slashed validator.

The whistleblower reward comes from new issuance of Ether on the beacon chain, but is more than offset by the Ether burned due to slashing penalties.

PROPOSER REWARD QUOTIENT

PROPOSER_REWARD_QUOTIENT was removed in the Altair upgrade in favour of PROPOSER_WEIGHT. It was used to apportion rewards between attesters and proposers when including attestations in blocks.

INACTIVITY PENALTY QUOTIENT BELLATRIX

This value supersedes INACTIVITY_PENALTY_QUOTIENT and INACTIVITY_PENALTY_QUOTIENT_ALTAIR.

If the beacon chain hasn't finalised a checkpoint for longer than MIN_EPOCHS_TO_INACTIVITY_PENALTY epochs, then it enters "leak" mode. In this mode, any validator that does not vote (or votes for an incorrect target) is penalised an amount each epoch of (effective_balance * inactivity_score) // (INACTIVITY_SCORE_BIAS * INACTIVITY_PENALTY_QUOTIENT_BELLATRIX).

Since the Altair upgrade, inactivity_score has become a per-validator quantity, whereas previously validators were penalised by a globally calculated amount when they missed a duty during a leak. See inactivity penalties for more on the rationale for this and how this score is calculated per validator.

During a leak, no validators receive rewards, and they continue to accrue the normal penalties when they fail to fulfil duties. In addition, for epochs in which validators do not make a correct, timely target vote, they receive a leak penalty.

To examine the effect of the leak on a single validator's balance, assume that during a period of inactivity leak (non-finalisation) the validator is completely offline. At each epoch, the offline validator will be penalised an extra amount nB/α , where n is the number of epochs since the leak started, B is the validator's effective balance, and α is the prevailing inactivity penalty quotient (currently INACTIVITY_PENALTY QUOTIENT BELLATRIX).

The effective balance B will remain constant for a while, by design, during which time the total amount of the penalty after n epochs would be $n(n+1)B/2\alpha$. This is sometimes called the "quadratic leak" since it grows as n^2 to first order. If B were continuously variable, the penalty would satisfy $\frac{dB}{dt} = -\frac{Bt}{\alpha}$, which can be solved to give $B(t) = B_0 e^{-t^2/2\alpha}$. The actual behaviour is somewhere between these two (piecewise

quadratic) since the effective balance is neither constant nor continuously variable but decreases in a step-wise fashion.

In the continuous approximation, the inactivity penalty quotient, α , is the square of the time it takes to reduce the balance of a non-participating validator to $1/\sqrt{e}$, or around 60.7% of its initial value. With the value of INACTIVITY_PENALTY_QUOTIENT_BELLATRIX at 2**24, this equates to 4096 epochs, or 18.2 days.

The idea for the inactivity leak (aka the quadratic leak) was proposed in the original Casper FFG paper. The problem it addresses is that, if a large fraction of the validator set were to go offline at the same time, it would not be possible to continue finalising checkpoints, since a majority vote from validators representing 2/3 of the total stake is required for finalisation.

In order to recover, the inactivity leak gradually reduces the stakes of validators who are not making attestations until, eventually, the participating validators control 2/3 of the remaining stake. They can then begin to finalise checkpoints once again.

This inactivity penalty mechanism is designed to protect the chain long-term in the face of catastrophic events (sometimes referred to as the ability to survive World War III). The result might be that the beacon chain could permanently split into two independent chains either side of a network partition, and this is assumed to be a reasonable outcome for any problem that can't be fixed in a few weeks. In this sense, the beacon chain formally prioritises availability over consistency. (You can't have both.)

The value of INACTIVITY_PENALTY_QUOTIENT was increased by a factor of four from 2**24 to 2**26 for the beacon chain launch, with the intention of penalising validators less severely in case of non-finalisation due to implementation problems in the early days. As it happens, there were no instances of non-finalisation during the eleven months of Phase 0 of the beacon chain.

The value was decreased by one quarter in the Altair upgrade from 2**26 (INACTIVITY_PENALTY_QUOTIENT) to 3 * 2**24 (INACTIVITY_PENALTY_QUOTIENT_ALTAIR), and to its final value of 2**24 (INACTIVITY_PENALTY_QUOTIENT_BELLATRIX) in the Bellatrix upgrade. Decreasing the inactivity penalty quotient speeds up recovery of finalisation in the event of an inactivity leak.

MIN SLASHING PENALTY QUOTIENT BELLATRIX

When a validator is first convicted of a slashable offence, an initial penalty is applied. This is calculated as, validator.effective balance // MIN SLASHING PENALTY QUOTIENT BELLATRIX.

Thus, the initial slashing penalty is between 0.5 ETH and 1 ETH depending on the validator's effective balance (which is between 16 and 32 Ether; note that effective balance is denominated in Gwei).

A further slashing penalty is applied later based on the total amount of balance slashed during a period of EPOCHS_PER_SLASHINGS_VECTOR.

The value of MIN_SLASHING_PENALTY_QUOTIENT was increased by a factor of four from 2**5 to 2**7 for the beacon chain launch, anticipating that unfamiliarity with the rules of Ethereum 2.0 staking was likely to result in some unwary users getting slashed. In the event, a total of 157 validators were slashed during Phase 0, all as a result of user error or misconfiguration as far as can be determined.

The value of this parameter was halved in the Altair upgrade from 2**7 (MIN_SLASHING_PENALTY_QUOTIENT) to 2**6 (MIN_SLASHING_PENALTY_QUOTIENT_ALTAIR), and set to its final value of 2**5 (MIN_SLASHING_PENALTY_QUOTIENT_BELLATRIX) in the Bellatrix upgrade.

PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX

When a validator has been slashed, a further penalty is later applied to the validator based on how many other validators were slashed during a window of size EPOCHS_PER_SLASHINGS_VECTOR epochs centred on that slashing event (approximately 18 days before and after).

The proportion of the validator's remaining effective balance that will be subtracted is calculated as, PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX multiplied by the sum of the effective balances of the slashed validators in the window, divided by the total effective balance of all validators. The idea of this mechanism is to punish accidents lightly (in which only a small number of validators were slashed) and attacks heavily (where many validators coordinated to double vote).

To finalise conflicting checkpoints, at least a third of the balance must have voted for both. That's why the "natural" setting of PROPORTIONAL_SLASHING_MULTIPLIER is three: in the event of an attack that finalises conflicting checkpoints, the attackers lose their entire stake. This provides "the maximal minimum accountable safety margin".

However, for the initial stage of the beacon chain, Phase 0, PROPORTIONAL_SLASHING_MULTIPLIER was set to one. It was increased to two at the Altair upgrade, and to its final value of three at the Bellatrix upgrade. The lower values provided some insurance against client bugs that might have caused mass slashings in the early days.

Max operations per block

Name	Value
MAX_PROPOSER_SLASHINGS	2**4 (= 16)
MAX_ATTESTER_SLASHINGS	2**1 (= 2)
MAX_ATTESTATIONS	2**7 (= 128)
MAX_DEPOSITS	2**4 (= 16)
MAX_VOLUNTARY_EXITS	2**4 (= 16)
MAX_BLS_TO_EXECUTION_CHANGES	2**4 (= 16)

These parameters are used to size lists in the beacon block bodies for the purposes of SSZ serialisation, as well as constraining the maximum size of beacon blocks so that they can propagate efficiently, and avoid DoS attacks.

Some comments on the chosen values:

- I have suggested elsewhere reducing MAX_DEPOSITS from sixteen to one to ensure that more validators must process deposits, which encourages them to run Eth1 clients.
- At first sight, there looks to be a disparity between the number of proposer slashings and the number of attester slashings that may be included in a block. But note that an attester slashing (a) can be much larger than a proposer slashing, and (b) can result in many more validators getting slashed than a proposer slashing.
- MAX_ATTESTATIONS is double the value of MAX_COMMITTEES_PER_SLOT. This allows there to be an empty slot (with no block proposal), yet still include all the attestations for the empty slot in the next slot. Since, ideally, each committee produces a single aggregate attestation, a block can hold two slots' worth of aggregate attestations.

Sync committee

Name	Value	Unit	Duration
SYNC_COMMITTEE_SIZE EPOCHS_PER_SYNC_ COMMITTEE_PERIOD	uint64(2**9) $(=512)$ uint64(2**8) $(=256)$	Validators epochs	~27 hours

Sync committees were introduced by the Altair upgrade to allow light clients to quickly and trustlessly determine the head of the beacon chain.

Why did we need a new committee type? Couldn't this be built on top of existing committees, say committees 0 to 3 at a slot? After all, voting for the head of the chain is already one of their duties. The reason is that it is important for reducing the load on light clients that sync committees do not change very often. Standard committees change every slot; we need something much longer lived here.

Only a single sync committee is active at any one time, and contains a randomly selected subset of size SYNC_COMMITTEE_SIZE of the total validator set.

A sync committee does its duties (and receives rewards for doing so) for only EPOCHS_PER_SYNC_COMMITTEE_PERIOD epochs until the next committee takes over.

With 500,000 validators, the expected time between being selected for sync committee duty is around 37 months. The probability of being in the current sync committee would be $\frac{512}{500,000}$ per validator.

SYNC_COMMITTEE_SIZE is a trade-off between security (ensuring that enough honest validators are always present) and efficiency for light clients (ensuring that they do not have to handle too much computation). The value 512 is conservative in terms of safety. It would be catastrophic for trustless bridges to other protocols, for example, if a sync committee voted in an invalid block.

EPOCHS_PER_SYNC_COMMITTEE_PERIOD is around a day, and again is a trade-off between security (short enough that it's hard for an attacker to find and corrupt committee members) and efficiency (reducing the data load on light clients).

Execution

Value
uint64(2**30) (= $1,073,741,824$)
uint64(2**20) (= 1,048,576)
uint64(2**8) $(=256)$
2**5 (= 32)
uint64(2**4) $(=16)$

These first four of these constants were introduced at the Bellatrix pre-Merge upgrade and are used only to size some fields within the ExecutionPayload class.

The execution payload (formerly known as an Eth1 block) contains a list of up to MAX_TRANSACTIONS_PER_PAYLOAD normal Ethereum transactions. Each of these has size up to MAX_BYTES_PER_TRANSACTION. These constants are needed only because SSZ list types require a maximum size to be specified. They are set ludicrously large, but that's not a problem in practice.

BYTES_PER_LOGS_BLOOM and MAX_EXTRA_DATA_BYTES are a direct carry-over from Eth1 blocks as specified in the Yellow Paper, being the size of a block's Bloom filter and the size of a block's extra data field respectively. The execution payload's extra data is analogous to a beacon block's graffiti - the block builder can set it to any value they choose.

MAX_WITHDRAWALS_PER_PAYLOAD was introduced at the Capella upgrade. It is the maximum number of withdrawals that the consensus client will ask the execution client to include in an execution payload. As a consequence, the rate of withdrawals is limited to MAX_WITHDRAWALS_PER_PAYLOAD per slot.

Withdrawals processing

Name	Value
MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP	16384 (= 2**14)

This preset constant was introduced in the Capella upgrade to bound the amount of work each node wold need to do when processing withdrawals.

The number of withdrawal transactions per block is bounded at MAX_WITHDRAWALS_PER_PAYLOAD. But not all validators will be eligible for a withdrawal transaction, meaning that nodes might have to search indefinitely through the validator set to find enough withdrawals to include. Searching the validator set can be an expensive operation, therefore we bound the search, considering only MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP validators per block. If we find fewer withdrawable validators than MAX_WITHDRAWALS_PER_PAYLOAD then we make fewer withdrawal transactions.

The primary reason that a validator might not be withdrawable is that it still has an old 0x00 BLS withdrawal credential. At least in the early days of Capella this could have led to long stretches of the validator set that were not withdrawable, before many validators had updated their credentials.

Another reason might be having an effective balance lower than MAX_EFFECTIVE_BALANCE. In the event of an inactivity leak this could also lead to long stretches of validators being non-withdrawable.

Configuration

Genesis Settings

Beacon chain genesis is long behind us. Nevertheless, the ability to spin-up testnets is useful in all sorts of scenarios, so the spec retains genesis functionality, now called initialisation.

The following parameters refer to the actual mainnet beacon chain genesis, and I'll explain them in that context. When starting up new testnets, these will of course be changed. For example, see the configuration file for the Prater testnet.

Name	Value
MIN_GENESIS_ACTIVE_VALIDATOR_COUNT	uint64(2**14) $(=16,384)$
MIN_GENESIS_TIME	uint64(1606824000) (Dec $1, 2020, 12pm \ UTC$)
GENESIS_FORK_VERSION	Version('0x00000000')
GENESIS_DELAY	uint64(604800) (7 days)

MIN_GENESIS_ACTIVE_VALIDATOR_COUNT

MIN_GENESIS_ACTIVE_VALIDATOR_COUNT is the minimum number of full validator stakes that must have been deposited before the beacon chain can start producing blocks. The number is chosen to ensure a degree of security. It allows for four 128 member committees per slot, rather than the 64 committees per slot eventually desired to support the fully operational data shards that were on the roadmap at that time (but no longer). Fewer validators means higher rewards per validator, so it is designed to attract early participants to get things bootstrapped.

 $MIN_GENESIS_ACTIVE_VALIDATOR_COUNT$ used to be much higher (65,536 = 2 million Ether staked), but was reduced when $MIN_GENESIS_TIME$, below, was added.

In the actual event of beacon chain genesis, there were 21,063 participating validators, comfortably exceeding the minimum necessary count.

MIN_GENESIS_TIME

MIN_GENESIS_TIME is the earliest date that the beacon chain can start.

Having a MIN_GENESIS_TIME allows us to start the chain with fewer validators than was previously thought necessary. The previous plan was to start the chain as soon as there were MIN_GENESIS_ACTIVE_VALIDATOR_COUNT validators staked. But there were concerns that with a lowish initial validator count, a single entity could form the majority of them and then act to prevent other validators from entering (a "gatekeeper attack"). A minimum genesis time allows time for all those who wish to make deposits to do so before they could be excluded by a gatekeeper attack.

The beacon chain actually started at 12:00:23 UTC on the 1st of December 2020. The extra 23 seconds comes from the timestamp of the first Eth1 block to meet the genesis criteria, block 11320899. I like to think of this as a little remnant of proof of work forever embedded in the beacon chain's history.

GENESIS_FORK_VERSION

Unlike Ethereum 1.0, the beacon chain gives in-protocol versions to its forks. See the Version custom type for more explanation.

GENESIS_FORK_VERSION is the fork version the beacon chain starts with at its "genesis" event: the point at which the chain first starts producing blocks. Nowadays, this value is used only when computing the

cryptographic domain for deposit messages and BLS credential change messages, which are valid across all forks.

Fork versions and timings for the Altair, Bellatrix, and Capella upgrades are defined in their respective specifications as follows.

Name	Value
ALTAIR_FORK_VERSION	Version('0x01000000')
ALTAIR_FORK_EPOCH	Epoch(74240) (Oct 27, 2021, 10:56:23am UTC)
BELLATRIX_FORK_VERSION	Version('0x02000000')
BELLATRIX_FORK_EPOCH	Epoch(144896) (Sept 6, 2022, 11:34:47am UTC)
CAPELLA_FORK_VERSION	Version('0x03000000')
CAPELLA_FORK_EPOCH	Epoch(194048) (April 12, 2023, $10:27:35pm \ UTC$)

GENESIS_DELAY

The GENESIS_DELAY is a grace period to allow nodes and node operators time to prepare for the genesis event. The genesis event cannot occur before MIN_GENESIS_TIME. If MIN_GENESIS_ACTIVE_VALIDATOR_COUNT validators are not registered sufficiently in advance of MIN_GENESIS_TIME, then Genesis will occur GENESIS_DELAY seconds after enough validators have been registered.

Seven days' notice was regarded as sufficient to allow client dev teams time to make a release once the genesis parameters were known, and for node operators to upgrade to that release. And, of course, to organise some parties. It was increased from 2 days over time due to lessons learned on some of the pre-genesis testnets.

Time parameters

Name	Value	Unit	Duration
SECONDS_PER_SLOT	uint64(12)	seconds	12 seconds
SECONDS_PER_ETH1_BLOCK	uint64(14)	seconds	14 seconds
MIN_VALIDATOR_WITHDRAWABILITY_DELAY	uint64(2**8) $(=256)$	epochs	$\sim 27 \text{ hours}$
SHARD_COMMITTEE_PERIOD	uint64(2**8) $(=256)$	epochs	$\sim 27 \text{ hours}$
ETH1_FOLLOW_DISTANCE	uint64(2**11) $(=2,048)$	Eth1 blocks	$\sim 8 \text{ hours}$

SECONDS_PER_SLOT

This was originally six seconds, but is now twelve, and has been other values in between.

Network delays are the main limiting factor in shortening the slot length. Three communication activities need to be accomplished within a slot, and it is supposed that four seconds is enough for the vast majority of nodes to have participated in each:

- 1. Blocks are proposed at the start of a slot and should have propagated to most of the network within the first four seconds.
- 2. At four seconds into a slot, committee members create and broadcast attestations, including attesting to this slot's block. During the next four seconds, these attestations are collected by aggregators in each committee.
- 3. At eight seconds into the slot, the aggregators broadcast their aggregate attestations which then have four seconds to reach the validator who is proposing the next block.

There is a general intention to shorten the slot time in future, perhaps to 8 seconds, if it proves possible to do this in practice. Or perhaps to lengthen it to 16 seconds.

Post-Merge, the time taken by the execution client to validate the execution payload contents (that is, the normal Ethereum transactions) is now on the critical path for validators during step 1, the first

four seconds. In order for the validator to attest correctly, the beacon block must first be broadcast, propagated and received, then validated by the consensus client, and also validated by the execution client, all within that initial four-second window. In borderline cases, the extra time taken by execution validation can push the whole process beyond the four-second point at which attestations must be made. This can lead to voting incorrectly for an empty slot. See Adrian Sutton's article Understanding Attestation Misses for further explanation.

SECONDS PER ETH1 BLOCK

The assumed block interval on the Eth1 chain, used in conjunction with ETH1_FOLLOW_DISTANCE when considering blocks on the Eth1 chain, either at genesis, or when voting on the deposit contract state.

The average Eth1 block time since January 2020 has actually been nearer 13 seconds, but never mind. The net effect is that we will be going a little deeper back in the Eth1 chain than ETH1_FOLLOW_DISTANCE would suggest, which ought to be safer.

MIN VALIDATOR WITHDRAWABILITY DELAY

A validator can stop participating once it has made it through the exit queue. However, its stake remains locked for the duration of MIN_VALIDATOR_WITHDRAWABILITY_DELAY. This is to allow some time for any slashable behaviour to be detected and reported so that the validator can still be penalised (in which case the validator's withdrawable time is pushed EPOCHS PER SLASHINGS VECTOR into the future).

Once the MIN_VALIDATOR_WITHDRAWABILITY_DELAY period has passed, the validator becomes eligible for a full withdrawal of its stake and rewards on the next withdrawals sweep, as long as it has ETH1_ADDRESS_WITHDRAWAL_PREFIX (0x01) withdrawal credentials set. In any case, being in a "withdrawable" state means that a validator has now fully exited from the protocol.

SHARD_COMMITTEE_PERIOD

This really anticipates the implementation of data shards, which is no longer planned, at least in its originally envisaged form. The idea is that it's bad for the stability of longer-lived committees if validators can appear and disappear very rapidly. Therefore, a validator cannot initiate a voluntary exit until SHARD_COMMITTEE_PERIOD epochs after it has been activated. However, it could still be ejected by slashing before this time.

ETH1_FOLLOW_DISTANCE

This is used to calculate the minimum depth of block on the Ethereum 1 chain that can be considered by the Eth2 chain: it applies to the Genesis process and the processing of deposits by validators. The Eth1 chain depth is estimated by multiplying this value by the target average Eth1 block time, SECONDS_PER_ETH1_BLOCK.

The value of ETH1_FOLLOW_DISTANCE is not based on the expected depth of any reorgs of the Eth1 chain, which are rarely if ever more than 2-3 blocks deep. It is about providing time to respond to an incident on the Eth1 chain such as a consensus failure between clients.

This parameter was increased from 1024 to 2048 blocks for the beacon chain mainnet, to allow devs more time to respond if there were any trouble on the Eth1 chain.

The whole follow distance concept has been made redundant by the Merge and may be removed in a future upgrade, so that validators can make deposits and become active more-or-less instantly.

Validator Cycle

Name	Value
EJECTION_BALANCE	Gwei(2**4 * 10**9) $(=16,\!000,\!000,\!000)$
MIN_PER_EPOCH_CHURN_LIMIT	uint64(2**2) $(=4)$
CHURN_LIMIT_QUOTIENT	${\tt uint64(2**16)}\ (=65{,}536)$

EJECTION BALANCE

If a validator's effective balance falls to 16 Ether or below then it is exited from the system. This is most likely to happen as a result of the "inactivity leak", which gradually reduces the balances of inactive validators in order to maintain the liveness of the beacon chain.

This mechanism is intended to protect stakers who no longer have access to their keys. If a validator has been offline for long enough to lose half of its balance, it is unlikely to be coming back. To save the staker from losing everything, we choose to eject the validator before its balance reaches zero.

Note that the dependence on effective balance means that the validator is queued for ejection as soon as its actual balance falls to 16.75 Ether.

MIN PER EPOCH CHURN LIMIT

Validators are allowed to exit the system and cease validating, and new validators may apply to join at any time. For interesting reasons, a design decision was made to apply a rate-limit to entries (activations) and exits. Basically, it is important in proof of stake protocols that the validator set not change too quickly.

In the normal case, a validator is able to exit fairly swiftly: it just needs to wait MAX_SEED_LOOKAHEAD (currently four) epochs. However, if a large number of validators wishes to exit at the same time, a queue forms with a limited number of exits allowed per epoch. The minimum number of exits per epoch (the minimum "churn") is MIN_PER_EPOCH_CHURN_LIMIT, so that validators can always eventually exit. The actual allowed churn per epoch is calculated in conjunction with CHURN_LIMIT_QUOTIENT.

The same applies to new validator activations, once a validator has been marked as eligible for activation.

The rate at which validators can exit is strongly related to the concept of weak subjectivity, and the weak subjectivity period.

CHURN_LIMIT_QUOTIENT

This is used in conjunction with $MIN_PER_EPOCH_CHURN_LIMIT$ to calculate the actual number of validator exits and activations allowed per epoch. The number of exits allowed is $max(MIN_PER_EPOCH_CHURN_LIMIT$, n // $CHURN_LIMIT_QUOTIENT$), where n is the number of active validators. The same applies to activations.

Inactivity penalties

Name	Value	Description
INACTIVITY_SCORE_BIAS	uint64(2**2) $(=4)$	score points per inactive epoch
INACTIVITY_SCORE_RECOVERY_RATE	${\tt uint64(2**4)}\ (=16)$	score points per leak-free epoch

INACTIVITY_SCORE_BIAS

If the beacon chain hasn't finalised an epoch for longer than MIN_EPOCHS_TO_INACTIVITY_PENALTY epochs, then it enters "leak" mode. In this mode, any validator that does not vote (or votes for an incorrect target) is penalised an amount each epoch of (effective_balance * inactivity_score) // (INACTIVITY_SCORE_BIAS * INACTIVITY_PENALTY_QUOTIENT_BELLATRIX). See INACTIVITY_PENALTY_QUOTIENT_BELLATRIX for discussion of the inactivity leak itself.

The per-validator inactivity-score was introduced in the Altair upgrade. During Phase 0, inactivity penalties were an increasing global amount applied to all validators that did not participate in an epoch, regardless of their individual track records of participation. So a validator that was able to participate for a significant fraction of the time nevertheless could be quite severely penalised due to the growth of the per-epoch inactivity penalty. Vitalik gives a simplified example: "if fully [off]line validators get leaked and lose 40% of their balance, someone who has been trying hard to stay online and succeeds at 90% of their duties would still lose 4% of their balance. Arguably this is unfair."

In addition, if many validators are able to participate intermittently, it indicates that whatever event has befallen the chain is potentially recoverable (unlike a permanent network partition, or a super-majority

network fork, for example). The inactivity leak is intended to bring finality to irrecoverable situations, so prolonging the time to finality if it's not irrecoverable is likely a good thing.

Each validator has an individual inactivity score in the beacon state which is updated by process_inactivity updates() as follows.

- Every epoch, irrespective of the inactivity leak,
 - decrease the score by one when the validator makes a correct timely target vote, and
 - increase the score by INACTIVITY SCORE BIAS otherwise.
- When *not* in an inactivity leak
 - decrease every validator's score by INACTIVITY SCORE RECOVERY RATE.

There is a floor of zero on the score. So, outside a leak, validators' scores will rapidly return to zero and stay there, since INACTIVITY SCORE RECOVERY RATE is greater than INACTIVITY SCORE BIAS.

When in a leak, if p is the participation rate between 0 and 1, and λ is INACTIVITY_SCORE_BIAS, then the expected score after N epochs is $\max(0, N((1-p)\lambda-p))$. For $\lambda=4$ this is $\max(0, N(4-5p))$. So a validator that is participating 80% of the time or more can maintain a score that is bounded near zero. With less than 80% average participation, its score will increase unboundedly.

INACTIVITY SCORE RECOVERY RATE

When not in an inactivity leak, validators' inactivity scores are reduced by INACTIVITY_SCORE_RECOVERY_RATE + 1 per epoch when they make a timely target vote, and by INACTIVITY_SCORE_RECOVERY_RATE - INACTIVITY_SCORE_BIAS when they don't. So, even for non-performing validators, scores decrease three times faster than they increase.

The new scoring system means that some validators will continue to be penalised due to the leak, even after finalisation starts again. This is intentional. When the leak causes the beacon chain to finalise, at that point we have just 2/3 of the stake online. If we immediately stop the leak (as we used to), then the amount of stake online would remain close to 2/3 and the chain would be vulnerable to flipping in and out of finality as small numbers of validators come and go. We saw this behaviour on some of the testnets prior to launch. Continuing the leak after finalisation serves to increase the balances of participating validators to greater than 2/3, providing a margin that should help to prevent such behaviour.

See the section on the Inactivity Leak for some more analysis of the inactivity score and some graphs of its effect.

Transition settings

Name	Value
TERMINAL_TOTAL_DIFFICULTY	587500000000000000000000
TERMINAL_BLOCK_HASH	Hash32()
TERMINAL_BLOCK_HASH_ACTIVATION_EPOCH	FAR_FUTURE_EPOCH

These values are not used in the main beacon chain specification, but are used in the Bellatrix fork choice and validator guide to determine the point of handover from proof of work to proof of stake for the execution chain.

All previous upgrades to the Ethereum proof of work chain took place at a pre-defined block height. That approach was deemed to be insecure for the Merge due to the irreversible dynamics of the switch to proof of stake. The rationale is given in the Security Considerations section of EIP-3675.

Using a pre-defined block number for the hardfork is unsafe in this context due to the PoS fork choice taking priority during the transition.

An attacker may use a minority of hash power to build a malicious chain fork that would satisfy the block height requirement. Then the first PoS block may be maliciously proposed on top of the PoW block from this adversarial fork, becoming the head and subverting the security of the transition.

To protect the network from this attack scenario, difficulty accumulated by the chain (total difficulty) is used to trigger the upgrade.

Thus, the Bellatrix upgrade defined a terminal total difficulty (TTD) at which the Merge would take place. Each block on the Ethereum proof of work chain has a "difficulty" associated with it, which corresponds to the expected number of hashes it would take to mine it. The total difficulty is the monotonically increasing accumulated difficulty of all the blocks so far.

The first block to exceed TERMINAL_TOTAL_DIFFICULTY was Ethereum block number 15537393. That block became the last canonical block to be produced under proof of work. The next execution payload was included in the beacon chain at slot 4700013, which was produced at 06:42:59 UTC on September the 15th, 2022.

TERMINAL_BLOCK_HASH and TERMINAL_BLOCK_HASH_ACTIVATION_EPOCH are present in case a need arose to manually select a particular proof of work fork to follow in case of trouble. TERMINAL_BLOCK_HASH would have been set in clients, by a manual override or a client update, to point to a specific proof of work block chosen by agreement to be the terminal block. In the event this functionality was not needed.

Containers

Preamble

We are about to see our first Python code in the executable spec. For specification purposes, these Container data structures are just Python data classes that are derived from the base SSZ Container class.

SSZ is the serialisation and Merkleization format used everywhere in Ethereum 2.0. It is not self-describing, so you need to know ahead of time what you are unpacking when describing. SSZ deals with basic types and composite types. Classes like the below are handled as SSZ containers, a composite type defined as an "ordered heterogeneous collection of values".

Client implementations in different languages will obviously use their own paradigms to represent these data structures.

Two notes directly from the spec:

- The definitions are ordered topologically to facilitate execution of the spec.
- Fields missing in container instantiations default to their zero value.

Misc dependencies

Fork

```
class Fork(Container):
    previous_version: Version
    current_version: Version
    epoch: Epoch # Epoch of latest fork
```

Fork data is stored in the BeaconState to indicate the current and previous fork versions. The fork version gets incorporated into the cryptographic domain in order to invalidate messages from validators on other forks. The previous fork version and the epoch of the change are stored so that pre-fork messages can still be validated (at least until the next fork). This ensures continuity of attestations across fork boundaries.

Note that this is all about planned protocol forks (upgrades), and nothing to do with the fork-choice rule, or inadvertent forks due to errors in the state transition.

ForkData

```
class ForkData(Container):
    current_version: Version
    genesis_validators_root: Root
```

ForkData is used only in compute_fork_data_root(). This is used when distinguishing between chains for the purpose of peer-to-peer gossip, and for domain separation. By including both the current fork version and the genesis validators root, we can cleanly distinguish between, say, mainnet and a testnet. Even if they have the same fork history, the genesis validators roots will differ.

Version is the datatype for a fork version number.

Checkpoint

```
class Checkpoint(Container):
    epoch: Epoch
    root: Root
```

Checkpoints are the points of justification and finalisation used by the Casper FFG protocol. Validators use them to create AttestationData votes, and the status of recent checkpoints is recorded in BeaconState.

As per the Casper paper, checkpoints contain a height, and a block root. In this implementation of Casper FFG, checkpoints occur whenever the slot number is a multiple of SLOTS_PER_EPOCH, thus they

correspond to epoch numbers. In particular, checkpoint N is the first slot of epoch N. The genesis block is checkpoint 0, and starts off both justified and finalised.

Thus, the root element here is the block root of the first block in the epoch. (This might be the block root of an earlier block if some slots have been skipped, that is, if there are no blocks for those slots.).

It is very common to talk about justifying and finalising epochs. This is not strictly correct: checkpoints are justified and finalised.

Once a checkpoint has been finalised, the slot it points to and all prior slots will never be reverted.

Validator

```
class Validator(Container):
   pubkey: BLSPubkey
   withdrawal_credentials: Bytes32 # Commitment to pubkey for withdrawals
   effective_balance: Gwei # Balance at stake
   slashed: boolean
   # Status epochs
   activation_eligibility_epoch: Epoch # When criteria for activation were met
   activation_epoch: Epoch
   exit_epoch: Epoch
   withdrawable_epoch: Epoch # When validator can withdraw funds
```

This is the data structure that stores most of the information about an individual validator, with only validators' balances and inactivity scores stored elsewhere.

Validators' actual balances are stored separately in the BeaconState structure, and only the slowly changing "effective balance" is stored here. This is because actual balances are liable to change quite frequently (at least every epoch, and sometimes more frequently): the Merkleization process used to calculate state roots means that only the parts that change need to be recalculated; the roots of unchanged parts can be cached. Separating out the validator balances potentially means that only 1/15th (8/121) as much data needs to be rehashed every epoch compared to storing them here, which is an important optimisation.

For similar reasons, validators' inactivity scores are stored outside validator records as well, as they are also updated every epoch.

A validator's record is created when its deposit is first processed. Sending multiple deposits does not create multiple validator records: deposits with the same public key are aggregated in one record. Validator records never expire; they are stored permanently, even after the validator has exited the system. Thus, there is a 1:1 mapping between a validator's index in the list and the identity of the validator (validator records are only ever appended to the list).

Also stored in Validator:

- pubkey serves as both the unique identity of the validator and the means of cryptographically verifying messages purporting to have been signed by it. The public key is stored raw, unlike in Eth1, where it is hashed to form the account address. This allows public keys to be aggregated for verifying aggregated attestations.
- Depending on its prefix, withdrawal_credentials might specify an Eth1 account to which withdrawal transactions will be made, or it might be an old-style BLS commitment that needs to be updated before withdrawals can occur for that validator. The withdrawal credentials included in a validator's deposit data are not checked in any way by the consensus layer.
- effective_balance is a topic of its own that we've touched upon already, and will discuss more fully when we look at effective balances updates.
- slashed indicates that a validator has been slashed, that is, punished for violating the slashing conditions. A validator can be slashed only once.
- The remaining values are the epochs in which the validator changed, or is due to change state.

A detailed explanation of the stages in a validator's lifecycle is here, and we'll be covering it in detail as we work through the beacon chain logic. But, in simplified form, progress is as follows:

- 1. A 32 ETH deposit has been made on the Ethereum 1 chain. No validator record exists yet.
- 2. The deposit is processed by the beacon chain at some slot. A validator record is created with all epoch fields set to FAR_FUTURE_EPOCH.
- 3. At the end of the current epoch, the activation_eligibility_epoch is set to the next epoch.
- 4. After the epoch activation_eligibility_epoch has been finalised, the validator is added to the activation queue by setting its activation_epoch appropriately, taking into account the per-epoch churn limit and MAX_SEED_LOOKAHEAD.
- 5. On reaching activation_epoch the validator becomes active, and should carry out its duties.
- 6. At any time after SHARD_COMMITTEE_PERIOD epochs have passed, a validator may request a voluntary exit. exit_epoch is set according to the validator's position in the exit queue and MAX_SEED_ LOOKAHEAD, and withdrawable epoch is set MIN VALIDATOR WITHDRAWABILITY DELAY epochs after that.
- 7. From exit_epoch onward the validator is no longer active. There is no mechanism for exited validators to rejoin: exiting is permanent.
- 8. After withdrawable_epoch, the validator's full stake can be withdrawn.

The above does not account for slashing or forced exits due to low balance.

AttestationData

class AttestationData(Container):

slot: Slot
index: CommitteeIndex
LMD GHOST vote
beacon block root: Root

FFG vote

source: Checkpoint
target: Checkpoint

The beacon chain relies on a combination of two different consensus mechanisms: LMD GHOST keeps the chain moving, and Casper FFG brings finalisation. These are documented in the Gasper paper. Attestations from (committees of) validators are used to provide votes simultaneously for each of these consensus mechanisms.

This container is the fundamental unit of attestation data. It provides the following elements.

- slot: each active validator should be making exactly one attestation per epoch. Validators have an assigned slot for their attestation, and it is recorded here for validation purposes.
- index: there can be several committees active in a single slot. This is the number of the committee that the validator belongs to in that slot. It can be used to reconstruct the committee to check that the attesting validator is a member. Ideally, all (or the majority at least) of the attestations in a slot from a single committee will be identical, and can therefore be aggregated into a single aggregate attestation.
- beacon_block_root is the validator's vote on the head block for that slot after locally running the LMD GHOST fork-choice rule. It may be the root of a block from a previous slot if the validator believes that the current slot is empty.
- source is the validator's opinion of the best currently justified checkpoint for the Casper FFG finalisation process.
- target is the validator's opinion of the block at the start of the current epoch, also for Casper FFG finalisation.

This AttestationData structure gets wrapped up into several other similar but distinct structures:

• Attestation is the form in which attestations normally make their way around the network. It is signed and aggregatable, and the list of validators making this attestation is compressed into a bitlist.

- IndexedAttestation is used primarily for attester slashing. It is signed and aggregated, with the list of attesting validators being an uncompressed list of indices.
- PendingAttestation. In Phase 0, after having their validity checked during block processing, PendingAttestations were stored in the beacon state pending processing at the end of the epoch. This was reworked in the Altair upgrade and PendingAttestations are no longer used.

IndexedAttestation

```
class IndexedAttestation(Container):
    attesting_indices: List[ValidatorIndex, MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    signature: BLSSignature
```

This is one of the forms in which aggregated attestations – combined identical attestations from multiple validators in the same committee – are handled.

Attestations and IndexedAttestations contain essentially the same information. The difference being that the list of attesting validators is stored uncompressed in IndexedAttestations. That is, each attesting validator is referenced by its global validator index, and non-attesting validators are not included. To be valid, the validator indices must be unique and sorted, and the signature must be an aggregate signature from exactly the listed set of validators.

IndexedAttestations are primarily used when reporting attester slashing. An Attestation can be converted to an IndexedAttestation using get_indexed_attestation().

PendingAttestation

```
class PendingAttestation(Container):
    aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    inclusion_delay: Slot
    proposer_index: ValidatorIndex
```

PendingAttestations were removed in the Altair upgrade and now appear only in the process for upgrading the state during the fork. The following is provided for historical reference.

Prior to Altair, Attestations received in blocks were verified then temporarily stored in beacon state in the form of PendingAttestations, pending further processing at the end of the epoch.

A PendingAttestation is an Attestation minus the signature, plus a couple of fields related to reward calculation:

- inclusion_delay is the number of slots between the attestation having been made and it being included in a beacon block by the block proposer. Validators are rewarded for getting their attestations included in blocks, but the reward used to decline in inverse proportion to the inclusion delay. This incentivised swift attesting and communicating by validators.
- proposer_index is the block proposer that included the attestation. The block proposer gets a micro reward for every validator's attestation it includes, not just for the aggregate attestation as a whole. This incentivises efficient finding and packing of aggregations, since the number of aggregate attestations per block is capped.

Taken together, these rewards are designed to incentivise the whole network to collaborate to do efficient attestation aggregation (proposers want to include only well-aggregated attestations; validators want to get their attestations included, so will ensure that they get well aggregated).

This whole mechanism was replaced in the Altair upgrade by ParticipationFlags.

Eth1Data

```
class Eth1Data(Container):
    deposit_root: Root
    deposit_count: uint64
    block_hash: Hash32
```

Proposers include their view of the Ethereum 1 chain in blocks, and this is how they do it. The beacon chain stores these votes up in the beacon state until there is a simple majority consensus, then the winner is committed to beacon state. This is to allow the processing of Eth1 deposits, and creates a simple "honest-majority" one-way bridge from Eth1 to Eth2. The 1/2 majority assumption for this (rather than 2/3 for committees) is considered safe as the number of validators voting each time is large: EPOCHS_PER_ETH1_VOTING_PERIOD * SLOTS_PER_EPOCH = 64 * 32 = 2048.

- deposit_root is the result of the get_deposit_root() method of the Eth1 deposit contract after executing the Eth1 block being voted on it's the root of the (incremental) Merkle tree of deposits.
- deposit_count is the number of deposits in the deposit contract at that point, the result of the get_deposit_count method on the contract. This will be equal to or greater than (if there are pending unprocessed deposits) the value of state.ethl_deposit_index.
- block_hash is the hash of the Eth1 block being voted for. This doesn't have any current use within the Eth2 protocol, but is "too potentially useful to not throw in there", to quote Danny Ryan.

HistoricalBatch

```
class HistoricalBatch(Container):
   block_roots: Vector[Root, SLOTS_PER_HISTORICAL_ROOT]
   state roots: Vector[Root, SLOTS PER HISTORICAL ROOT]
```

The HistoricalBatch container has been superseded by HistoricalSummary in the Capella upgrade. It remains in the spec since the historical_roots list remains in the BeaconState, albeit it now frozen forever.

HistoricalBatch is no longer used anywhere in the state transition. However, applications validating pre-Capella data against the historical_roots list will need to use it.

See process_historical_summaries_update() for more discussion of this change.

DepositMessage

```
class DepositMessage(Container):
   pubkey: BLSPubkey
   withdrawal_credentials: Bytes32
   amount: Gwei
```

The basic information necessary to either add a validator to the registry, or to top up an existing validator's stake.

pubkey is the unique public key of the validator. If it is already present in the registry (the list of validators in beacon state) then amount is added to its balance. Otherwise, a new Validator entry is appended to the list and credited with amount.

See the Validator container for more on withdrawal_credentials.

There are two protections that DepositMessages get at different points.

- 1. DepositData is included in beacon blocks as a Deposit, which adds a Merkle proof that the data has been registered with the Eth1 deposit contract.
- 2. When the containing beacon block is processed, deposit messages are stored, pending processing at the end of the epoch, in the beacon state as DepositData. This includes the pending validator's BLS signature so that the authenticity of the DepositMessage can be verified before a validator is added.

DepositData

```
class DepositData(Container):
   pubkey: BLSPubkey
   withdrawal_credentials: Bytes32
   amount: Gwei
   signature: BLSSignature # Signing over DepositMessage
```

A signed DepositMessage. The comment says that the signing is done over DepositMessage. What actually happens is that a DepositMessage is constructed from the first three fields; the root of that is combined with DOMAIN_DEPOSIT in a SigningData object; finally the root of this is signed and included in DepositData.

BeaconBlockHeader

```
class BeaconBlockHeader(Container):
    slot: Slot
    proposer_index: ValidatorIndex
    parent_root: Root
    state_root: Root
    body_root: Root
```

A standalone version of a beacon block header: BeaconBlocks contain their own header. It is identical to BeaconBlock, except that body is replaced by body_root. It is BeaconBlock-lite.

BeaconBlockHeader is stored in beacon state to record the last processed block header. This is used to ensure that we proceed along a continuous chain of blocks that always point to their predecessor 100. See process_block_header().

The signed version is used in proposer slashings.

SyncCommittee

```
class SyncCommittee(Container):
   pubkeys: Vector[BLSPubkey, SYNC_COMMITTEE_SIZE]
   aggregate_pubkey: BLSPubkey
```

Sync committees were introduced in the Altair upgrade to support light clients to the beacon chain protocol. The list of committee members for each of the current and next sync committees is stored in the beacon state. Members are updated every EPOCHS_PER_SYNC_COMMITTEE_PERIOD epochs by get_next_sync committee().

Including the aggregate_pubkey of the sync committee is an optimisation intended to save light clients some work when verifying the sync committee's signature. All the public keys of the committee members (including any duplicates) are aggregated into this single public key. If any signatures are missing from the SyncAggregate, the light client can "de-aggregate" them by performing elliptic curve subtraction. As long as more than half of the committee contributed to the signature, then this will be faster than constructing the aggregate of participating members from scratch. If less than half contributed to the signature, the light client can start instead with the identity public key and use elliptic curve addition to aggregate those public keys that are present.

See also SYNC_COMMITTEE_SIZE.

SigningData

```
class SigningData(Container):
   object_root: Root
   domain: Domain
```

This is just a convenience container, used only in compute_signing_root() to calculate the hash tree root of an object along with a domain. The resulting root is the message data that gets signed with a BLS signature. The SigningData object itself is never stored or transmitted.

Withdrawal

```
class Withdrawal(Container):
   index: WithdrawalIndex
  validator_index: ValidatorIndex
  address: ExecutionAddress
  amount: Gwei
```

¹⁰⁰It's a blockchain, yo!

A container for handling validator balance withdrawals from the consensus layer to the execution layer. The index is a simple count of the total number of withdrawal transactions made since withdrawals were enabled in the Capella upgrade.

As per the type definition of the amount field, the consensus layer denominates withdrawals in Gwei (as it does all Ether amounts), while the execution layer denominates withdrawals in Wei (as it does all Ether amounts). Care needs to be taken when dealing with withdrawal transactions not to end up a factor of 10^9 wrong.

HistoricalSummary

```
class HistoricalSummary(Container):
    """
    `HistoricalSummary` matches the components of the phase0 `HistoricalBatch`
    making the two hash_tree_root-compatible.
    """
    block_summary_root: Root
    state_summary_root: Root
```

This is part of the double batched accumulator mechanism implemented by process_historical_summaries_update(). It was introduced in the Capella upgrade and supersedes HistoricalBatch as the structure for storing roots of historical data.

The comment here is interesting. It reflects the invariant that the SSZ hash tree root of a container of objects is the same as the hash tree root of a container of the objects' hash tree roots - what I call the magic of Merkleization.

The following code demonstrates this equivalence between the pre- and post-Capella constructions. It should run with no errors.

```
from eth2spec.capella import mainnet
from eth2spec.capella.mainnet import *
from eth2spec.utils.ssz.ssz_typing import *
# Dummy data
roots = [Root('0x0123456789abcdef0123456789abcdef0123456789abcdef0123456789abcdef')] *
                                         \hookrightarrow SLOTS PER HISTORICAL ROOT
block_roots = state_roots = Vector[Root, SLOTS_PER_HISTORICAL_ROOT](*roots)
# Pre-Capella
historical_batch = HistoricalBatch(
    block_roots = block_roots,
    state_roots = state_roots)
# Post-Capella
historical summary = HistoricalSummary(
    block summary root = hash tree root(block roots),
    state_summary_root = hash_tree_root(state_roots))
assert(hash_tree_root(historical_batch) == hash_tree_root(historical_summary))
```

Beacon operations

The following are the various protocol messages that can be transmitted in a block on the beacon chain.

For most of these, the proposer is rewarded either explicitly or implicitly for including the object in a block.

The proposer receives explicit in-protocol rewards for including the following in blocks:

- ProposerSlashings,
- AttesterSlashings,
- Attestations, and

• SyncAggregates.

Including Deposit objects in blocks is only implicitly rewarded, in that, if there are pending deposits that the block proposer does not include then the block is invalid, so the proposer receives no reward.

There is no direct reward for including VoluntaryExit objects. However, for each validator exited, rewards for the remaining validators increase very slightly, so it's still beneficial for proposers not to ignore VoluntaryExits.

ProposerSlashing

```
class ProposerSlashing(Container):
    signed_header_1: SignedBeaconBlockHeader
    signed header 2: SignedBeaconBlockHeader
```

ProposerSlashings may be included in blocks to prove that a validator has broken the rules and ought to be slashed. Proposers receive a reward for correctly submitting these.

In this case, the rule is that a validator may not propose two different blocks at the same height, and the payload is the signed headers of the two blocks that evidence the crime. The signatures on the SignedBeaconBlockHeaders are checked to verify that they were both signed by the accused validator.

AttesterSlashing

```
class AttesterSlashing(Container):
   attestation_1: IndexedAttestation
   attestation 2: IndexedAttestation
```

AttesterSlashings may be included in blocks to prove that one or more validators in a committee has broken the rules and ought to be slashed. Proposers receive a reward for correctly submitting these.

The contents of the IndexedAttestations are checked against the attester slashing conditions in is_slashable_attestation_data(). If there is a violation, then any validator that attested to both attestation_1 and attestation_2 is slashed, see process_attester_slashing().

AttesterSlashings can be very large since they could in principle list the indices of all the validators in a committee. However, in contrast to proposer slashings, many validators can be slashed as a result of a single report.

Attestation

```
class Attestation(Container):
    aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    signature: BLSSignature
```

This is the form in which attestations make their way around the network. It is designed to be easily aggregatable: Attestations containing identical AttestationData can be combined into a single attestation by aggregating the signatures.

Attestations contain the same information as IndexedAttestations, but use knowledge of the validator committees at slots to compress the list of attesting validators down to a bitlist. Thus, Attestations are at least 5 times smaller than IndexedAttestations, and up to 35 times smaller (with 128 or 2048 validators per committee, respectively).

When a validator first broadcasts its attestation to the network, the aggregation_bits list will contain only a single bit set, and calling get_attesting_indices() on it will return a list containing only a single entry, the validator's own index.

Deposit

```
class Deposit(Container):
    proof: Vector[Bytes32, DEPOSIT_CONTRACT_TREE_DEPTH + 1] # Merkle path to deposit root
    data: DepositData
```

This container is used to include deposit data from prospective validators in beacon blocks so that they can be processed into beacon state.

The proof is a Merkle proof constructed by the block proposer that the DepositData corresponds to the previously agreed deposit root of the Eth1 contract's deposit tree. It is verified in process_deposit() by is_valid_merkle_branch().

VoluntaryExit

```
class VoluntaryExit(Container):
    epoch: Epoch # Earliest epoch when voluntary exit can be processed
    validator_index: ValidatorIndex
```

Voluntary exit messages are how a validator signals that it wants to cease being a validator. Blocks containing VoluntaryExit data for an epoch later than the current epoch are invalid, so nodes should buffer or ignore any future-dated exits they see.

VoluntaryExit objects are never used naked; they are always wrapped up into a SignedVoluntaryExit object.

SyncAggregate

```
class SyncAggregate(Container):
    sync_committee_bits: Bitvector[SYNC_COMMITTEE_SIZE]
    sync_committee_signature: BLSSignature
```

The prevailing sync committee is stored in the beacon state, so the SyncAggregates included in blocks need only use a bit vector to indicate which committee members signed off on the message.

The sync_committee_signature is the aggregate signature of all the validators referenced in the bit vector over the block root of the previous slot.

 ${\tt SyncAggregates} \ {\rm are} \ {\rm handled} \ {\rm by} \ {\tt process_sync_aggregate()}.$

BLSToExecutionChange

```
class BLSToExecutionChange(Container):
    validator_index: ValidatorIndex
    from_bls_pubkey: BLSPubkey
    to_execution_address: ExecutionAddress
```

The Capella upgrade gives validators that have old style BLS withdrawal credentials a one-time opportunity to update them to Eth1 withdrawal credentials.

To make this change, a staker needs to broadcast a signed message containing this information via a consensus node. It will eventually be included in a block at which point nodes will verify it and update their validator registries. The from_bls_pubkey is verified against the validator's existing withdrawal credential, and the message's signature is verified against the from_bls_pubkey.

Beacon blocks

BeaconBlockBody

```
class BeaconBlockBody(Container):
    randao_reveal: BLSSignature
    eth1_data: Eth1Data # Eth1 data vote
    graffiti: Bytes32 # Arbitrary data
    # Operations
    proposer_slashings: List[ProposerSlashing, MAX_PROPOSER_SLASHINGS]
    attester_slashings: List[AttesterSlashing, MAX_ATTESTER_SLASHINGS]
    attestations: List[Attestation, MAX_ATTESTATIONS]
    deposits: List[Deposit, MAX_DEPOSITS]
    voluntary_exits: List[SignedVoluntaryExit, MAX_VOLUNTARY_EXITS]
    sync_aggregate: SyncAggregate # [New in Altair]
```

The two fundamental data structures for nodes are the BeaconBlock and the BeaconState. The BeaconBlock is how the leader (the chosen proposer in a slot) communicates network updates to all the other validators, and those validators update their own BeaconState by applying BeaconBlocks. The idea is that (eventually) all validators on the network come to agree on the same BeaconState.

Validators are randomly selected to propose beacon blocks, and there ought to be exactly one beacon block per slot if things are running correctly. If a validator is offline, or misses its slot, or proposes an invalid block, or has its block orphaned, then a slot can be empty.

The following objects are always present in a valid beacon block.

- randao_reveal: the block is invalid if the RANDAO reveal does not verify correctly against the proposer's public key. This is the block proposer's contribution to the beacon chain's randomness. The proposer generates it by signing the current epoch number (combined with DOMAIN_RANDAO) with its private key. To the best of anyone's knowledge, the result is indistinguishable from random. This gets mixed into the beacon state RANDAO.
- See Eth1Data for eth1_data. In principle, this is mandatory, but it is not checked, and there is no penalty for making it up.
- graffiti is left free for the proposer to insert whatever data it wishes. It has no protocol level significance. It can be left as zero; most clients set the client name and version string as their own default graffiti value.
- sync_aggregate is a record of which validators in the current sync committee voted for the chain head in the previous slot.
- execution_payload is what was known as an Eth1 block pre-Merge. Ethereum transactions are now included within beacon blocks in the form of an ExecutionPayload structure.

Deposits are a special case. They are mandatory only if there are pending deposits to be processed. There is no explicit reward for including deposits, except that a block is invalid without any that ought to be there.

• deposits: if the block does not contain either all the outstanding Deposits, or MAX_DEPOSITS of them in deposit order, then it is invalid.

Including any of the remaining objects is optional. They are handled, if present, in the process_operations() function.

The proposer earns rewards for including any of the following. Rewards for attestations and sync aggregates are available every slot. Slashings, however, are very rare.

- proposer slashings: up to MAX PROPOSER SLASHINGS ProposerSlashing objects may be included.
- $\bullet \ \ \text{attester_slashings: up to MAX_ATTESTER_SLASHINGS AttesterSlashing objects may be included.}$
- attestations: up to MAX_ATTESTATIONS (aggregated) Attestation objects may be included. The
 block proposer is incentivised to include well-packed aggregate attestations, as it receives a micro
 reward for each unique attestation. In a perfect world, with perfectly aggregated attestations, MAX_
 ATTESTATIONS would be equal to MAX_COMMITTEES_PER_SLOT; in our configuration it is double. This
 provides capacity in blocks to catch up with attestations after skip slots, and also room to include
 some imperfectly aggregated attestations.

Including voluntary exits and BLS to execution changes is optional, and there are no explicit rewards for doing so.

- voluntary_exits: up to MAX_VOLUNTARY_EXITS SignedVoluntaryExit objects may be included.
- bls_to_execution_changes: up to MAX_BLS_TO_EXECUTION_CHANGES SignedBLSToExecutionChange objects may be included.

BeaconBlock

```
class BeaconBlock(Container):
    slot: Slot
    proposer_index: ValidatorIndex
    parent_root: Root
    state_root: Root
    body: BeaconBlockBody
```

BeaconBlock just adds some blockchain paraphernalia to BeaconBlockBody. It is identical to BeaconBlockHeader, except that the body_root is replaced by the actual block body.

slot is the slot the block is proposed for.

proposer_index was added to avoid a potential DoS vector, and to allow clients without full access to the state to still know useful things.

parent_root is used to make sure that this block is a direct child of the last block we processed.

In order to calculate state_root, the proposer is expected to run the state transition with the block before propagating it. After the beacon node has processed the block, the state roots are compared to ensure they match. This is the mechanism for tying the whole system together and making sure that all validators and beacon nodes are always working off the same version of state (in the absence of short-term forks).

If any of these is incorrect, then the block is invalid with respect to the current beacon state and will be ignored.

Beacon state

BeaconState

```
class BeaconState(Container):
         # Versioning
         genesis_time: uint64
          genesis validators root: Root
         slot: Slot
         fork: Fork
         # History
         latest block header: BeaconBlockHeader
         block roots: Vector[Root, SLOTS PER HISTORICAL ROOT]
         state roots: Vector[Root, SLOTS PER HISTORICAL ROOT]
         historical_roots: List[Root, HISTORICAL_ROOTS_LIMIT] # Frozen in Capella, replaced by
                                                                                                       \hookrightarrow historical summaries
         # Eth1
         eth1 data: Eth1Data
         eth1 data votes: List[Eth1Data, EPOCHS PER ETH1 VOTING PERIOD * SLOTS PER EPOCH]
         eth1_deposit_index: uint64
         # Registry
         validators: List[Validator, VALIDATOR REGISTRY LIMIT]
         balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
         # Randomness
         randao mixes: Vector[Bytes32, EPOCHS PER HISTORICAL VECTOR]
         # Slashings
         slashings: Vector[Gwei, EPOCHS PER SLASHINGS VECTOR] # Per-epoch sums of slashed effective balances
          # Participation
         previous\_epoch\_participation: \ List[ParticipationFlags, \ VALIDATOR\_REGISTRY\_LIMIT] \ \# \ [Modified in the context of the c

→ Altairl

         current_epoch_participation: List[ParticipationFlags, VALIDATOR_REGISTRY_LIMIT] # [Modified in
                                                                                                      \hookrightarrow Altair]
         # Finality
          justification_bits: Bitvector[JUSTIFICATION_BITS_LENGTH] # Bit set for every recent justified epoch
         previous justified checkpoint: Checkpoint
          current justified checkpoint: Checkpoint
          finalized checkpoint: Checkpoint
```

```
# Inactivity
inactivity_scores: List[uint64, VALIDATOR_REGISTRY_LIMIT] # [New in Altair]
# Sync
current_sync_committee: SyncCommittee # [New in Altair]
next_sync_committee: SyncCommittee # [New in Altair]
# Execution
latest_execution_payload_header: ExecutionPayloadHeader # [New in Bellatrix]
# Withdrawals
next_withdrawal_index: WithdrawalIndex # [New in Capella]
next_withdrawal_validator_index: ValidatorIndex # [New in Capella]
# Deep history valid from Capella onwards
historical_summaries: List[HistoricalSummary, HISTORICAL_ROOTS_LIMIT] # [New in Capella]
```

All roads lead to the BeaconState. Maintaining this data structure is the sole purpose of all the apparatus in all the spec documents. This state is the focus of consensus among the beacon nodes; it is what everybody, eventually, must agree on.

The beacon chain's state is monolithic: everything is bundled into a single state object (sometimes referred to as the "God object"). Some have argued for more granular approaches that might be more efficient, but at least the current approach is simple.

Let's break this thing down.

```
# Versioning
genesis_time: uint64
genesis_validators_root: Root
slot: Slot
fork: Fork
```

How do we know which chain we're on, and where we are on it? The information here ought to be sufficient. A continuous path back to the genesis block would also suffice.

genesis_validators_root is calculated at Genesis time (when the chain starts) and is fixed for the life of the chain. This, combined with the fork identifier, should serve to uniquely identify the chain that we are on.

genesis_time is used by the fork choice rule to work out what slot we're in, and (since The Merge) to validate execution payloads.

The values of these two fields is fixed for the life of the chain. For the mainnet beacon chain they have the following values:

genesis_time	1606824023	
genesis_validators_root	0x4b363db94e286120d76eb905340fdd4e54bfe9f0	
	6bf33ff6cf5ad27f511bfe95	

The fork object is manually updated as part of beacon chain upgrades, also called hard forks. This invalidates blocks and attestations from validators not following the new fork.

Since the Capella fork, the fork field has contained the following values:

```
\begin{array}{ccc} & & & \\ & \text{previous\_version} & & \text{0x020000000} \\ & \text{current\_version} & & \text{0x030000000} \\ & \text{epoch} & & & 194048 \\ \end{array}
```

Historical info on fork versions and upgrade timing is in the Upgrade History chapter.

```
# History
latest_block_header: BeaconBlockHeader
block_roots: Vector[Root, SLOTS_PER_HISTORICAL_ROOT]
state_roots: Vector[Root, SLOTS_PER_HISTORICAL_ROOT]
```

```
historical_roots: List[Root, HISTORICAL_ROOTS_LIMIT] # Frozen in Capella, replaced by \hookrightarrow historical summaries
```

latest_block_header is only used to make sure that the next block we process is a direct descendent of the previous block. It's a blockchain thing.

Past block_roots and state_roots are stored in the lists here until the lists are full. Before the Capella upgrade, once the lists were full, they were Merkleized together and the root appended to historical_roots. Since Capella, they are now Merkleized separately and appended to historical_summaries (see below). The historical_roots list is now frozen and continues to exist only to allow proofs to be made against pre-Capella blocks and states.

```
# Eth1
eth1_data: Eth1Data
eth1_data_votes: List[Eth1Data, EPOCHS_PER_ETH1_VOTING_PERIOD * SLOTS_PER_EPOCH]
eth1_deposit_index: uint64
```

ethl_data is the latest agreed upon state of the Ethl chain and deposit contract. ethl_data_votes accumulates EthlData from blocks until there is an overall majority in favour of one Ethl state. If a majority is not achieved by the time the list is full then it is cleared down and voting starts again from scratch. ethl_deposit_index is the total number of deposits that have been processed by the beacon chain (which is greater than or equal to the number of validators, as a deposit can top up the balance of an existing validator).

```
# Registry
validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
```

The registry of Validators and their balances. The balances list is separated out as it changes much more frequently than the validators list. Roughly speaking, balances of active validators are updated at least once per epoch, while the validators list has only minor updates per epoch. When combined with SSZ tree hashing, this results in a big saving in the amount of data to be rehashed on registry updates. See also validator inactivity scores under Inactivity which we treat similarly.

```
# Randomness
randao_mixes: Vector[Bytes32, EPOCHS_PER_HISTORICAL_VECTOR]
```

Past randao mixes are stored in a fixed-size circular list for EPOCHS_PER_HISTORICAL_VECTOR epochs (~290 days). These can be used to recalculate past committees, which allows slashing of historical attestations. See EPOCHS_PER_HISTORICAL_VECTOR for more information.

```
# Slashings
slashings: Vector[Gwei, EPOCHS_PER_SLASHINGS_VECTOR]
```

A fixed-size circular list of past slashed amounts. Each epoch, the total effective balance of all validators slashed in that epoch is stored as an entry in this list. When the final slashing penalty for a slashed validator is calculated, it is weighted with the sum of this list. This mechanism is designed to less heavily penalise one-off slashings that are most likely accidental, and more heavily penalise mass slashings during a window of time, which are more likely to be a coordinated attack.

These lists record which validators participated in attesting during the current and previous epochs by recording flags for timely votes for the correct source, the correct target and the correct head. We store two epochs' worth since Validators have up to 32 slots to include a correct target vote. The flags are used to calculate finality and to assign rewards at the end of epochs.

Previously, during Phase 0, we stored two epochs' worth of actual attestations in the state and processed them en masse at the end of epochs. This was slow, and was thought to be contributing to observed

late block production in the first slots of epochs. The change to the new scheme was implemented in the Altair upgrade under the title of Accounting Reforms.

```
# Finality
justification_bits: Bitvector[JUSTIFICATION_BITS_LENGTH]
previous_justified_checkpoint: Checkpoint
current_justified_checkpoint: Checkpoint
finalized_checkpoint: Checkpoint
```

Ethereum 2.0 uses the Casper FFG finality mechanism, with a k-finality optimisation, where k = 2. The above objects in the state are the data that need to be tracked in order to apply the finality rules.

- justification_bits is only four bits long. It tracks the justification status of the last four epochs: 1 if justified, 0 if not. This is used when calculating whether we can finalise an epoch.
- Outside the finality calculations, previous_justified_checkpoint and current_justified_checkpoint are used to filter attestations: valid blocks include only attestations with a source checkpoint that matches the justified checkpoint in the state for the attestation's epoch.
- finalized_checkpoint: the network has agreed that the beacon chain state at or before that epoch will never be reverted. So, for one thing, the fork choice rule doesn't need to go back any further than this. The Casper FFG mechanism is specifically constructed so that two conflicting finalized checkpoints cannot be created without at least one third of validators being slashed.

```
# Inactivity
inactivity_scores: List[uint64, VALIDATOR_REGISTRY_LIMIT] # [New in Altair]
```

This is logically part of "Registry", above, and would be better placed there. It is a per-validator record of inactivity scores that is updated every epoch. This list is stored outside the main list of Validator objects since it is updated very frequently. See the Registry for more explanation.

```
# Sync
current_sync_committee: SyncCommittee # [New in Altair]
next_sync_committee: SyncCommittee # [New in Altair]
```

Sync committees were introduced in the Altair upgrade. The next sync committee is calculated and stored so that participating validators can prepare in advance by subscribing to the required p2p subnets.

```
# Execution
latest execution payload header: ExecutionPayloadHeader # [New in Bellatrix]
```

Since the Merge, the header of the most recent execution payload is cached in the beacon state. This serves two functions for now, though possibly more in future. First, it allows the chain to check whether the Merge has been completed or not. See <code>is_merge_transition_complete()</code>. Second, it allows the beacon chain to check that the execution chain is unbroken when processing a new execution payload. See <code>process_execution_payload()</code>.

```
# Withdrawals
next_withdrawal_index: WithdrawalIndex # [New in Capella]
next_withdrawal_validator_index: ValidatorIndex # [New in Capella]
```

Automatic validator balance withdrawals were added in the Capella upgrade. The next_withdrawal_index maintains a count of the total number of withdrawal transactions performed so far, while next_withdrawal_validator_index cycles through the validator registry to keep track of which validator should be considered for a withdrawal next. Validators are considered for withdrawals consecutively in order of their validator indices, and the withdrawals sweep wraps round to zero after considering the highest-numbered validator. A maximum of MAX WITHDRAWALS PER PAYLOAD withdrawals may be made per block.

```
# Deep history valid from Capella onwards
historical_summaries: List[HistoricalSummary, HISTORICAL_ROOTS_LIMIT] # [New in Capella]
```

Hash tree roots of state.block_roots and state.state_roots are periodically added to historical_summaries every SLOTS_PER_HISTORICAL_ROOT slots as part of the protocol's double batched accumulator. The work is done by process_historical_summaries_update().

The state.historical_summaries list was introduced in the Capella upgrade and functionally replaces the state.historical_roots list that's now frozen (see above). It uses the HistoricalSummary container, which is twice as big as a Root type (64 bytes per item rather than 32). The list will effectively grow without bound (HISTORICAL_ROOTS_LIMIT is large), but at a rate of only 20 KB per year. Keeping this data is useful for light clients, and also allows Merkle proofs to be created against past states, for example historical deposit data.

Historical Note

There was a period during which beacon state was split into "crystallized state" and "active state". The active state was constantly changing; the crystallized state changed only once per epoch (or what passed for epochs back then). Separating out the fast-changing state from the slower-changing state was an attempt to avoid having to constantly rehash the whole state every slot. With the introduction of SSZ tree hashing, this was no longer necessary, as the roots of the slower changing parts could simply be cached, which was a nice simplification. There remains an echo of this approach, however, in the splitting out of validator balances and inactivity scores into different structures withing the beacon state.

Execution

ExecutionPayload

```
class ExecutionPayload(Container):
   # Execution block header fields
   parent_hash: Hash32
   fee_recipient: ExecutionAddress # 'beneficiary' in the yellow paper
   state_root: Bytes32
   receipts root: Bytes32
   logs bloom: ByteVector[BYTES PER LOGS BLOOM]
   prev_randao: Bytes32 # 'difficulty' in the yellow paper
   block_number: uint64 # 'number' in the yellow paper
   gas_limit: uint64
   gas_used: uint64
   timestamp: uint64
   extra_data: ByteList[MAX_EXTRA_DATA_BYTES]
   base_fee_per_gas: uint256
   # Extra payload fields
   block_hash: Hash32 # Hash of execution block
   transactions: List[Transaction, MAX TRANSACTIONS PER PAYLOAD]
   withdrawals: List[Withdrawal, MAX WITHDRAWALS PER PAYLOAD] # [New in Capella]
```

Since the Merge, blocks on the beacon chain contain Ethereum transaction data, formerly known as Eth1 blocks, and now called execution payloads.

This is a significant change, and is what led to the name "The Merge".

- Pre-Merge, there were two types of block in the Ethereum system:
 - Eth1 blocks contained users' transactions and were gossiped between Eth1 nodes;
 - Eth2 blocks (beacon blocks) contained only consensus information and were gossiped between Eth2 nodes.
- Post-Merge, there is only one kind of block, the merged beacon block:
 - Beacon blocks contain execution payloads that in turn contain users' transactions. These blocks are gossiped only between consensus (Eth2) nodes.

The ExecutionPayload is contained in the BeaconBlock structure.

The fields of ExecutionPayload mostly reflect the old structure of Eth1 blocks as described in Ethereum's Yellow Paper¹⁰¹, section 4.3. Differences from the Eth1 block structure are noted in the comments.

¹⁰¹This is intended to be a permalink to the Yellow Paper's "Berlin" edition, a pre-Merge version of the YP. At the time of writing, the YP has not been updated for the "London" upgrade and is therefore missing the EIP-1559 field base_fee_per_gas.

The execution payload differs from an old Eth1 block in the following respects:

- ommersHash (also known as uncle_hashes), difficulty, mixHash and nonce were not carried over from Eth1 blocks as they were specific to the proof of work mechanism.
- fee_recipient is the Ethereum account address that will receive the unburnt portion of the transaction fees (the priority fees). This has been called various things at various times: the original Yellow Paper calls it beneficiary; EIP-1559 calls it author. In any case, the proposer of the block sets the fee_recipient to specify where the appropriate transaction fees for the block are to be sent. Under proof of work this was the same address as the COINBASE address that received the block reward. Under proof of stake, the block reward is credited to the validator's beacon chain balance, and the transaction fees are credited to the fee_recipient Ethereum address.
- prev_randao replaces difficulty. The Eth1 chain did not have access to good quality randomness. Sometimes the block hash or difficulty of the block were used to seed randomness, but these were low quality. The prev_randao field gives the execution layer access to the beacon chain's randomness. This is better, but still not of cryptographic quality.
- block_number in the execution layer is the block height in that chain, picking up from the Eth1 block height at the Merge. It increments by one for every beacon block produced. The beacon chain itself does not track block height, only slot number, which can differ from block height due to empty slots.
- The execution payload block_hash is included. The consensus layer does not know how to calculate the root hashes of execution blocks, but needs access to them when checking that the execution chain is unbroken during execution payload processing.
- Despite being flagged in the comments as an "extra payload field", a list of transactions was always part of Eth1 blocks. However, the list of ommers/uncles is no longer present.

Individual transactions are represented by the Transaction custom type. There can be up to MAX_TRANSACTIONS_PER_PAYLOAD of them in a single execution payload. The values of MAX_BYTES_PER_TRANSACTION and MAX_TRANSACTIONS_PER_PAYLOAD are huge, and suggest that an execution payload could be up to a petabyte in size. These sizes are specified only because SSZ List types require them. They will occupy only the minimum necessary space in practice.

The withdrawals field was added in the Capella upgrade. Withdrawal transactions are unusual in that they affect state on both the consensus side and the execution side. Uniquely, withdrawal transactions are the only data that's generated by the consensus layer but only communicated between nodes in execution payloads.

ExecutionPayloadHeader

```
class ExecutionPayloadHeader(Container):
   # Execution block header fields
   parent_hash: Hash32
    fee_recipient: ExecutionAddress
   state_root: Bytes32
    receipts_root: Bytes32
    logs_bloom: ByteVector[BYTES_PER_LOGS_BLOOM]
   prev_randao: Bytes32
   block_number: uint64
   gas_limit: uint64
    gas_used: uint64
    timestamp: uint64
    extra_data: ByteList[MAX_EXTRA_DATA_BYTES]
   base_fee_per_gas: uint256
    # Extra payload fields
   block_hash: Hash32 # Hash of execution block
    transactions_root: Root
   withdrawals_root: Root # [New in Capella]
```

The same as ExecutionPayload but with the transactions represented only by their root. By the magic of Merkleization, the hash tree root of an ExecutionPayloadHeader will be the same as the hash tree root

of its corresponding ExecutionPayload.

The most recent ExecutionPayloadHeader is stored in the beacon state.

Signed envelopes

The following are just wrappers for more basic types, with an added signature.

SignedVoluntaryExit

```
class SignedVoluntaryExit(Container):
    message: VoluntaryExit
    signature: BLSSignature
```

A voluntary exit is currently signed with the validator's online signing key.

There has been some discussion about changing this to also allow signing of a voluntary exit with the validator's offline withdrawal key. The introduction of multiple types of withdrawal credential makes this more complex, however, and it is no longer likely to be practical.

SignedBeaconBlock

```
class SignedBeaconBlock(Container):
    message: BeaconBlock
    signature: BLSSignature
```

BeaconBlocks are signed by the block proposer and unwrapped for block processing.

This signature is what makes proposing a block "accountable". If two correctly signed conflicting blocks turn up, the signatures guarantee that the same proposer produced them both, and is therefore subject to being slashed. This is also why stakers need to closely guard their signing keys.

SignedBeaconBlockHeader

```
class SignedBeaconBlockHeader(Container):
    message: BeaconBlockHeader
    signature: BLSSignature
```

This is used only when reporting proposer slashing, within a ProposerSlashing object.

Through the magic of SSZ hash tree roots, a valid signature for a SignedBeaconBlock is also a valid signature for a SignedBeaconBlockHeader. Proposer slashing makes use of this to save space in slashing reports.

SignedBLSToExecutionChange

```
class SignedBLSToExecutionChange(Container):
    message: BLSToExecutionChange
    signature: BLSSignature
```

A message requesting a change from BLS withdrawal credentials to Eth1 withdrawal credentials.

Uniquely, this message is signed with the validator's withdrawal key rather than its usual signing key. Only validators that made deposits with 0x00 BLS credentials have a withdrawal key, and it will usually be different from the signing key (although it may be derived from the same mnemonic).

Helper Functions

Preamble

Note: The definitions below are for specification purposes and are not necessarily optimal implementations.

This note in the spec is super important for implementers! There are many, many optimisations of the below routines that are being used in practice; a naive implementation would be impractically slow for mainnet configurations. As long as the optimised code produces identical results to the code here, then all is fine.

Math

integer squareroot

```
def integer_squareroot(n: uint64) -> uint64:
    """
    Return the largest integer ``x`` such that ``x**2 <= n``.
    """
    x = n
    y = (x + 1) // 2
    while y < x:
        x = y
        y = (x + n // x) // 2
    return x</pre>
```

Validator rewards scale with the reciprocal of the square root of the total active balance of all validators. This is calculated in get_base_reward_per_increment().

In principle integer_squareroot is also used in get_attestation_participation_flag_indices(), to specify the maximum delay for source votes to receive a reward. But this is just the constant, integer_squareroot(SLOTS_PER_EPOCH), which is 5.

Newton's method is used which has pretty good convergence properties, but implementations may use any method that gives identical results.

```
Used\ by \\ \\ get\_base\_reward\_per\_increment(),\ get\_attestation\_participation\_flag\_indices() \\
```

xor

```
def xor(bytes_1: Bytes32, bytes_2: Bytes32) -> Bytes32:
    """
    Return the exclusive-or of two 32-byte strings.
    """
    return Bytes32(a ^ b for a, b in zip(bytes_1, bytes_2))
```

The bitwise xor of two 32-byte quantities is defined here in Python terms.

This is used only in process_randao() when mixing in the new randao reveal.

Fun fact: if you xor two byte types in Java, the result is a 32 bit (signed) integer. This is one reason we need to define the "obvious" here. But mainly, because the spec is executable, we need to tell Python what it doesn't already know.

```
Used by process_randao()
```

def uint_to_bytes(n: uint) -> bytes is a function for serializing the uint type object to bytes in ENDIANNESS-endian. The expected length of the output is the byte-length of the uint type.

For the most part, integers are integers and bytes are bytes, and they don't mix much. But there are a few places where we need to convert from integers to bytes:

- several times in the compute_shuffled_index() algorithm;
- in compute proposer index() for selecting a proposer weighted by stake;
- in get_seed() to mix the epoch number into the randao mix;
- in get_beacon_proposer_index() to mix the slot number into the per-epoch randao seed; and
- in get_next_sync_committee_indices().

You'll note that in every case, the purpose of the conversion is for the integer to form part of a byte string that is hashed to create (pseudo-)randomness.

The result of this conversion is dependent on our arbitrary choice of endianness, that is, how we choose to represent integers as strings of bytes. For Eth2, we have chosen little-endian: see the discussion of ENDIANNESS for more background.

The uint_to_bytes() function is not given an explicit implementation in the specification, which is unusual. This to avoid exposing the innards of the Python SSZ implementation (of uint) to the rest of the spec. When running the spec as an executable, it uses the definition in the SSZ utilities.

```
Used by compute_shuffled_index(), compute_proposer_index(), get_seed(), get_beacon_proposer_index(), get_next_sync_committee_indices()

See also ENDIANNESS, SSZ utilities
```

bytes to uint64

```
def bytes_to_uint64(data: bytes) -> uint64:
    """
    Return the integer deserialization of ``data`` interpreted as ``ENDIANNESS``-endian.
    """
    return uint64(int.from_bytes(data, ENDIANNESS))
```

bytes_to_uint64() is the inverse of uint_to_bytes(), and is used by the shuffling algorithm to create a random index from the output of a hash.

It is also used in the validator specification when selecting validators to aggregate attestations, and sync committee messages.

int.from_bytes is a built-in Python 3 method. The uint64 cast is provided by the spec's SSZ implementation.

```
Used by compute_shuffled_index
See also attestation aggregator selection, sync committee aggregator selection
```

Crypto

hash

```
def hash(data: bytes) -> Bytes32 is SHA256.
```

SHA256 was chosen as the protocol's base hash algorithm for easier cross-chain interoperability: many other chains use SHA256, and Eth1 has a SHA256 precompile.

There was a lot of discussion about this choice early in the design process. The original plan had been to use the BLAKE2b-512 hash function – that being a modern hash function that's faster than SHA3 –

and to move to a STARK/SNARK friendly hash function at some point (such as MiMC). However, to keep interoperability with Eth1, in particular for the implementation of the deposit contract, the hash function was changed to Keccak256. Finally, we settled on SHA256 as having even broader compatibility.

The hash function serves two purposes within the protocol. The main use, computationally, is in Merkleization, the computation of hash tree roots, which is ubiquitous in the protocol. Its other use is to harden the randomness used in various places.

hash_tree_root

def hash_tree_root(object: SSZSerializable) -> Root is a function for hashing objects into a single root by utilizing a hash tree structure, as defined in the SSZ spec.

The development of the tree hashing process was transformational for the Ethereum 2.0 specification, and it is now used everywhere.

The naive way to create a digest of a data structure is to serialise it and then just run a hash function over the result. In tree hashing, the basic idea is to treat each element of an ordered, compound data structure as the leaf of a Merkle tree, recursively if necessary until a primitive type is reached, and to return the Merkle root of the resulting tree.

At first sight, this all looks quite inefficient. Twice as much data needs to be hashed when tree hashing, and actual speeds are 4-6 times slower compared with the linear hash. However, it is good for supporting light clients, because it allows Merkle proofs to be constructed easily for subsets of the full state.

The breakthrough insight was realising that much of the re-hashing work can be cached: if part of the state data structure has not changed, that part does not need to be re-hashed: the whole subtree can be replaced with its cached hash. This turns out to be a huge efficiency boost, allowing the previous design, with cumbersome separate crystallised and active state, to be simplified into a single state object.

Merkleization, the process of calculating the hash_tree_root() of an object, is defined in the SSZ specification, and explained further in the section on SSZ.

BLS signatures

See the main write-up on BLS Signatures for a more in-depth exploration of this topic.

The IETF BLS signature draft standard v4 with ciphersuite BLS_SIG_BLS12381G2_XMD:SHA-256_SSWU_RO_POP_ defines the following functions:

- def Sign(privkey: int, message: Bytes) -> BLSSignature
- def Verify(pubkey: BLSPubkey, message: Bytes, signature: BLSSignature) -> bool
- def Aggregate(signatures: Sequence[BLSSignature]) -> BLSSignature
- def FastAggregateVerify(pubkeys: Sequence[BLSPubkey], message: Bytes, signature: BLSSignature) -> bool
- def AggregateVerify(pubkeys: Sequence[BLSPubkey], messages: Sequence[Bytes], signature: BLSSignature) -> bool
- def KeyValidate(pubkey: BLSPubkey) -> bool

The above functions are accessed through the bls module, e.g. bls.Verify.

The detailed specification of the cryptographic functions underlying Ethereum 2.0's BLS signing scheme is delegated to the draft IRTF standard¹⁰² as described in the spec. This includes specifying the elliptic curve BLS12-381 as our domain of choice.

¹⁰²This document does not have the full force of an IETF standard. For one thing, it remains a draft (that is now expired), for another it is an IRTF document, meaning that it is from a research group rather than being on the IETF standards

Our intention in conforming to the in-progress standard is to provide for maximal interoperability with other chains, applications, and cryptographic libraries. Ethereum Foundation researchers and Eth2 developers had input to the development of the standard. Nevertheless, there were some challenges involved in trying to keep up as the standard evolved. For example, the Hashing to Elliptic Curves standard was still changing rather late in the beacon chain testing phase. In the end, everything worked out fine.

The following two functions are described in the separate BLS Extensions document, but included here for convenience.

eth aggregate pubkeys

```
def eth_aggregate_pubkeys(pubkeys: Sequence[BLSPubkey]) -> BLSPubkey:
    """
    Return the aggregate public key for the public keys in ``pubkeys``.

NOTE: the ``+`` operation should be interpreted as elliptic curve point addition, which takes as input elliptic curve points that must be decoded from the input ``BLSPubkey``s.
    This implementation is for demonstrative purposes only and ignores encoding/decoding concerns.
    Refer to the BLS signature draft standard for more information.
    """
    assert len(pubkeys) > 0
# Ensure that the given inputs are valid pubkeys
    assert all(bls.KeyValidate(pubkey) for pubkey in pubkeys)

result = copy(pubkeys[0])
for pubkey in pubkeys[1:]:
    result += pubkey
return result
```

Stand-alone aggregation of public keys is not defined by the BLS signature standard. In the standard, public keys are aggregated only in the context of performing an aggregate signature verification via AggregateVerify() or FastAggregateVerify().

The eth_aggregate_pubkeys() function was added in the Altair upgrade to implement an optimisation for light clients when verifying the signatures on SyncAggregates.

```
Used by get_next_sync_committee()
Uses bls.KeyValidate()
```

eth_fast_aggregate_verify

The specification of FastAggregateVerify() in the BLS signature standard returns INVALID if there are zero public keys given.

This function was introduced in Altair to handle SyncAggregates that no sync committee member had signed off on, in which case the G2_POINT_AT_INFINITY can be considered a "correct" signature (in our case, but not according to the standard).

track. Some context from Brian Carpenter, former IETF chair, > I gather that you are referring to an issue in draft-irtf-cfrg-bls-signature-04. That is not even an IETF draft; it's an IRTF draft, apparently being discussed in an IRTF Research Group. So it is not even remotely under consideration to become an IETF standard...

The networking and validator specs were later clarified to require that SyncAggregates have at least one signature. But this requirement is not enforced in the consensus layer (in process_sync_aggregate()), so we need to retain this eth_fast_aggregate_verify() wrapper to allow the empty signature to be valid.

```
Used by process_sync_aggregate()
Uses FastAggregateVerify()
See also G2_POINT_AT_INFINITY
```

Predicates

is_active_validator

```
def is_active_validator(validator: Validator, epoch: Epoch) -> bool:
    """
    Check if ``validator`` is active.
    """
    return validator.activation_epoch <= epoch < validator.exit_epoch</pre>
```

Validators don't explicitly track their own state (eligible for activation, active, exited, withdrawable - the sole exception being whether they have been slashed or not). Instead, a validator's state is calculated by looking at the fields in the Validator record that store the epoch numbers of state transitions.

In this case, if the validator was activated in the past and has not yet exited, then it is active.

This is used a few times in the spec, most notably in get_active_validator_indices() which returns a list of all active validators at an epoch.

```
Used by get_active_validator_indices(), get_eligible_validator_indices(), process_registry_updates(), process_voluntary_exit()

See also Validator
```

is_eligible_for_activation_queue

```
def is_eligible_for_activation_queue(validator: Validator) -> bool:
    """
    Check if ``validator`` is eligible to be placed into the activation queue.
    """
    return (
        validator.activation_eligibility_epoch == FAR_FUTURE_EPOCH
        and validator.effective_balance == MAX_EFFECTIVE_BALANCE
    )
```

When a deposit is processed with a previously unseen public key, a new Validator record is created with all the state-transition fields set to the default value of FAR FUTURE EPOCH.

It is possible to deposit any amount over MIN_DEPOSIT_AMOUNT (currently 1 Ether) into the deposit contract. However, validators do not become eligible for activation until their effective balance is equal to MAX_EFFECTIVE_BALANCE, which corresponds to an actual balance of 32 Ether or more.

This predicate is used during epoch processing to find validators that have acquired the minimum necessary balance, but have not yet been added to the queue for activation. These validators are then marked as eligible for activation by setting the validator.activation_eligibility_epoch to the next epoch.

```
Used by process_registry_updates()
See also Validator, FAR_FUTURE_EPOCH, MAX_EFFECTIVE_BALANCE
```

is_eligible_for_activation

```
def is_eligible_for_activation(state: BeaconState, validator: Validator) -> bool:
    """
    Check if ``validator`` is eligible for activation.
    """
    return (
        # Placement in queue is finalized
        validator.activation_eligibility_epoch <= state.finalized_checkpoint.epoch
        # Has not yet been activated
        and validator.activation_epoch == FAR_FUTURE_EPOCH
    )</pre>
```

A validator that is_eligible_for_activation() has had its activation_eligibility_epoch set, but its activation_epoch is not yet set.

To avoid any ambiguity or confusion on the validator side about its state, we wait until its eligibility activation epoch has been finalised before adding it to the activation queue by setting its activation_epoch. Otherwise, it might at one point become active, and then the beacon chain could flip to a fork in which it is not active. This could happen if the latter fork had fewer blocks and had thus processed fewer deposits.

Note that state.finalized_checkpoint.epoch does not mean that all of the slots in that epoch are finalised. We finalise checkpoints, not epochs, so only the first slot (the checkpoint) of that epoch is finalised. This is accounted for in process_registry_updates() by adding one to the current epoch when setting the validator.activation_eligibility_epoch, so that we can be sure that the block containing the deposit has been finalised. 103

```
Used by process_registry_updates()
See also Validator, FAR_FUTURE_EPOCH
```

is_slashable_validator

Validators can be slashed only once: the flag validator.slashed is set when the first correct slashing report for the validator is processed.

An unslashed validator remains eligible to be slashed from when it becomes active right up until it becomes withdrawable. This is MIN_VALIDATOR_WITHDRAWABILITY_DELAY epochs (around 27 hours) after it has exited from being a validator and ceased validation duties.

```
Used by process_proposer_slashing(), process_attester_slashing()
See also Validator
```

is slashable attestation data

```
def is_slashable_attestation_data(data_1: AttestationData, data_2: AttestationData) -> bool:
    """
    Check if ``data_1`` and ``data_2`` are slashable according to Casper FFG rules.
    """
    return (
```

 $^{^{103}\}mathrm{I'd}$ have preferred not adding the one there, and using <, here. But it is what it is.

```
# Double vote
  (data_1 != data_2 and data_1.target.epoch == data_2.target.epoch) or
  # Surround vote
   (data_1.source.epoch < data_2.source.epoch and data_2.target.epoch < data_1.target.epoch)</pre>
```

This predicate is used by process_attester_slashing() to check that the two sets of alleged conflicting attestation data in an AttesterSlashing do in fact qualify as slashable.

There are two ways for validators to get slashed under Casper FFG:

- 1. A double vote: voting more than once for the same target epoch, or
- 2. A surround vote: the source—target interval of one attestation entirely contains the source—target interval of a second attestation from the same validator or validators. The reporting block proposer needs to take care to order the IndexedAttestations within the AttesterSlashing object so that the first set of votes surrounds the second. (The opposite ordering also describes a slashable offence, but is not checked for here, so the order of the arguments matters.)

It is far from obvious, but this predicate also enforces LMD GHOST slashing for attestation equivocation. The AttestationData objects contain the LMD GHOST head vote (beacon_block_root) as well as the Casper FFG votes. So, the Casper FFG checkpoint votes might be identical and non-slashable, but if the LMD GHOST vote differs between the two attestations then it will be deemed slashable.

```
Used by process_attester_slashing()
See also AttestationData, AttesterSlashing
```

is_valid_indexed_attestation

is valid indexed attestation() is used in attestation processing and attester slashing.

IndexedAttestations differ from Attestations in that the latter record the contributing validators in a bitlist and the former explicitly list the global indices of the contributing validators.

An IndexedAttestation passes this validity test only if all the following apply.

- 1. There is at least one validator index present.
- 2. The list of validators contains no duplicates (the Python set function performs deduplication).
- 3. The indices of the validators are sorted. (It is not clear to me why this is required. It's used in the duplicate check here, but that could just be replaced by checking the set size.)
- 4. Its aggregated signature verifies against the aggregated public keys of the listed validators.

Verifying the signature uses the magic of aggregated BLS signatures. The indexed attestation contains a BLS signature that is supposed to be the combined individual signatures of each of the validators listed in the attestation. This is verified by passing it to bls.FastAggregateVerify() along with the list of public keys from the same validators. The verification succeeds only if exactly the same set of validators

signed the message (signing_root) as appear in the list of public keys. Note that get_domain() mixes in the fork version, so that attestations are not valid across forks.

No check is done here that the attesting_indices (which are the global validator indices) are all members of the correct committee for this attestation. In process_attestation() they must be, by construction. In process_attester_slashing() it doesn't matter: any validator signing conflicting attestations is liable to be slashed.

```
Used by process_attester_slashing(), process_attestation()
Uses get_domain(), compute_signing_root(), bls.FastAggregateVerify()
See also IndexedAttestation, Attestation
```

is valid merkle branch

This is the classic algorithm for verifying a Merkle branch (also called a Merkle proof). Nodes are iteratively hashed as the tree is traversed from leaves to root. The bits of index select whether we are the right or left child of our parent at each level. The result should match the given root of the tree.

In this way we prove that we know that leaf is the value at position index in the list of leaves, and that we know the whole structure of the rest of the tree, as summarised in branch.

We use this function in process_deposit() to check whether the deposit data we've received is correct or not. Based on the deposit data they have seen, Eth2 clients build a replica of the Merkle tree of deposits in the deposit contract. The proposer of the block that includes the deposit constructs the Merkle proof using its view of the deposit contract, and all other nodes use <code>is_valid_merkle_branch()</code> to check that their view matches the proposer's. If any deposit fails Merkle branch verification then the entire block is invalid.

```
Used by process_deposit()
```

is_merge_transition_complete

```
def is_merge_transition_complete(state: BeaconState) -> bool:
    return state.latest_execution_payload_header != ExecutionPayloadHeader()
```

A simple test for whether the given beacon state is pre- or post-Merge. If the latest_execution_payload_header in the state is the default ExecutionPayloadHeader then the chain is pre-Merge, otherwise it is post-Merge. Upgrades normally occur at a predetermined block height (or epoch number on the beacon chain), and that's the usual way to test for them. The block height of the Merge, however, was unknown ahead of time, so a different kind of test was required.

Although the mainnet beacon chain is decidedly post-Merge now, this remains useful for syncing nodes from pre-Merge starting points.

This function was added in the Bellatrix pre-Merge upgrade.

Used by	<pre>process_execution_payload(), is_merge_transition_block(), is_execution_enabled()</pre>
See also	ExecutionPayloadHeader

is_merge_transition_block

```
def is_merge_transition_block(state: BeaconState, body: BeaconBlockBody) -> bool:
    return not is_merge_transition_complete(state) and body.execution_payload != ExecutionPayload()
```

If the Merge transition is not complete (meaning that the beacon state still has the default execution payload header in it), yet our block has a non-default execution payload, then this must be the first block we've seen with an execution payload. It is therefore the Merge transition block.

This function was added in the Bellatrix pre-Merge upgrade.

```
Uses is_merge_transition_complete()
Used by is_execution_enabled(), on_block() (Bellatrix version)
See also ExecutionPayload
```

is_execution_enabled

```
def is_execution_enabled(state: BeaconState, body: BeaconBlockBody) -> bool:
    return is_merge_transition_block(state, body) or is_merge_transition_complete(state)
```

If the block that we have is the first block with an execution payload (the Merge transition block), or we know from the state that we have previously seen a block with an execution payload then execution is enabled, the execution and consensus chains have Merged.

This function was added in the Bellatrix pre-Merge upgrade.

has eth1 withdrawal credential

```
def has_eth1_withdrawal_credential(validator: Validator) -> bool:
    """
    Check if ``validator`` has an 0x01 prefixed "eth1" withdrawal credential.
    """
    return validator.withdrawal_credentials[:1] == ETH1_ADDRESS_WITHDRAWAL_PREFIX
```

Only validators that have Eth1 withdrawal credentials are eligible for balance withdrawals of any sort.

```
Used by is_fully_withdrawable_validator(), is_partially_withdrawable_validator()
See also ETH1_ADDRESS_WITHDRAWAL_PREFIX
```

is_fully_withdrawable_validator

```
def is_fully_withdrawable_validator(validator: Validator, balance: Gwei, epoch: Epoch) -> bool:
    """
    Check if ``validator`` is fully withdrawable.
    """
    return (
        has_ethl_withdrawal_credential(validator)
        and validator.withdrawable_epoch <= epoch
        and balance > 0
    )
```

A validator is fully withdrawable only when (a) it has an Eth1 withdrawal credential to make the withdrawal to, (b) it has become withdrawable, meaning that its exit has been processed and it has passed through its MIN_VALIDATOR_WITHDRAWABILITY_DELAY period, and (c) it has a nonzero balance.

```
Uses has_eth1_withdrawal_credential()
Used by get_expected_withdrawals()
```

is_partially_withdrawable_validator

```
def is_partially_withdrawable_validator(validator: Validator, balance: Gwei) -> bool:
    """
    Check if ``validator`` is partially withdrawable.
    """
    has_max_effective_balance = validator.effective_balance == MAX_EFFECTIVE_BALANCE
    has_excess_balance = balance > MAX_EFFECTIVE_BALANCE
    return has eth1 withdrawal credential(validator) and has max effective balance and has excess balance
```

A partial withdrawal is the withdrawal of excess Ether from an active (non-exited) validator.

A validator has excess Ether only when (a) it's effective balance is at MAX_EFFECTIVE_BALANCE, (b) its actual balance is greater than MAX_EFFECTIVE_BALANCE, and (c) it has an Eth1 withdrawal credential to make the withdrawal to.

The first of these conditions is related to the hysteresis in the effective balance. If a validator has previously suffered a drop in its balance, it's effective balance might be 31 Ether even while its actual balance is greater than 32 Ether. If we were to start skimming withdrawals in this situation, the validator's balance would never reach the 32.25 Ether necessary to bring its effective balance up to 32 Ether, and it would be forever stuck at 31 ETH. Therefore, only validators with the full effective balance are eligible for the excess to be withdrawn.

```
Used by get_expected_withdrawals()
Uses has_eth1_withdrawal_credential()
See also MAX_EFFECTIVE_BALANCE, hysteresis
```

Misc

compute_shuffled_index

```
def compute_shuffled_index(index: uint64, index_count: uint64, seed: Bytes32) -> uint64:
   Return the shuffled index corresponding to ``seed`` (and ``index count``).
   assert index < index count
   # Swap or not (https://link.springer.com/content/pdf/10.1007%2F978-3-642-32009-5_1.pdf)
    # See the 'generalized domain' algorithm on page 3
    for current_round in range(SHUFFLE_ROUND_COUNT):
        pivot = bytes_to_uint64(hash(seed + uint_to_bytes(uint8(current_round)))[0:8]) % index_count
        flip = (pivot + index_count - index) % index_count
        position = max(index, flip)
        source = hash(
            seed
            + uint to bytes(uint8(current round))
            + uint to bytes(uint32(position // 256))
        byte = uint8(source[(position % 256) // 8])
        bit = (byte >> (position % 8)) % 2
        index = flip if bit else index
    return index
```

Selecting random, distinct committees of validators is a big part of Ethereum 2.0; it is foundational for both its scalability and security. This selection is done by shuffling.

Shuffling a list of objects is a well understood problem in computer science. Notice, however, that this routine manages to shuffle a *single index* to a new location, knowing only the total length of the list. To use the technical term for this, it is *oblivious*. To shuffle the whole list, this routine needs to be called once per validator index in the list. By construction, each input index maps to a distinct output index. Thus, when applied to all indices in the list, it results in a permutation, also called a shuffling.

Why do this rather than a simpler, more efficient, conventional shuffle? It's all about light clients. Beacon nodes will generally need to know the whole shuffling, but light clients will often be interested only in a small number of committees. Using this technique allows the composition of a single committee to be calculated without having to shuffle the entire set: potentially a big saving on time and memory.

As stated in the code comments, this is an implementation of the "swap-or-not" shuffle, described in the cited paper. Vitalik kicked off a search for a shuffle with these properties in late 2018. With the help of Professor Dan Boneh of Stanford University, the swap-or-not was identified as a candidate a couple of months later, and adopted into the spec.

The algorithm breaks down as follows. For each iteration (each round), we start with a current index.

- 1. Pseudo-randomly select a pivot. This is a 64-bit integer based on the seed and current round number. This domain is large enough that any non-uniformity caused by taking the modulus in the next step is entirely negligible.
- 2. Use pivot to find another index in the list of validators, flip, which is pivot index accounting for wrap-around in the list.
- 3. Calculate a single pseudo-random bit based on the seed, the current round number, and some bytes from either index or flip depending on which is greater.
- 4. If our bit is zero, we keep index unchanged; if it is one, we set index to flip.

We are effectively swapping cards in a deck based on a deterministic algorithm.

The way that **position** is broken down is worth noting:

- Bits 0-2 (3 bits) are used to select a single bit from the eight bits of byte.
- Bits 3-7 (5 bits) are used to select a single byte from the thirty-two bytes of source.
- Bits 8-39 (32 bits) are used in generating source. Note that the upper two bytes of this will always be zero in practice, due to limits on the number of active validators.

SHUFFLE_ROUND_COUNT is, and always has been, 90 in the mainnet configuration, as explained there.

See the section on Shuffling for a more structured exposition and analysis of this algorithm (with diagrams!).

In practice, full beacon node implementations will run this once per epoch using an optimised version that shuffles the whole list, and cache the result of that for the epoch.

```
Used by compute_committee(), compute_proposer_index(), get_next_sync_committee_indices()
Uses bytes_to_uint64()
See also SHUFFLE_ROUND_COUNT
```

compute_proposer_index

```
total = uint64(len(indices))
while True:
    candidate_index = indices[compute_shuffled_index(i % total, total, seed)]
    random_byte = hash(seed + uint_to_bytes(uint64(i // 32)))[i % 32]
    effective_balance = state.validators[candidate_index].effective_balance
    if effective_balance * MAX_RANDOM_BYTE >= MAX_EFFECTIVE_BALANCE * random_byte:
        return candidate_index
    i += 1
```

There is exactly one beacon block proposer per slot, selected randomly from among all the active validators. The seed parameter is set in get_beacon_proposer_index based on the epoch and slot. Note that there is a small but finite probability of the same validator being called on to propose a block more than once in an epoch.

A validator's chance of being the proposer is weighted by its effective balance: a validator with a 32 Ether effective balance is twice as likely to be chosen as a validator with a 16 Ether effective balance.

To account for the need to weight by effective balance, this function implements as a try-and-increment algorithm. A counter i starts at zero. This counter does double duty:

- First i is used to uniformly select a candidate proposer with probability 1/N where, N is the number of active validators. This is done by using the compute_shuffled_index routine to shuffle index i to a new location, which is then the candidate index.
- Then i is used to generate a pseudo-random byte using the hash function as a seeded PRNG with at least 256 bits of output. The lower 5 bits of i select a byte in the hash function, and the upper bits salt the seed. (An obvious optimisation is that the output of the hash changes only once every 32 iterations.)

The if test is where the weighting by effective balance is done. If the candidate has MAX_EFFECTIVE_BALANCE, it will always pass this test and be returned as the proposer. If the candidate has a fraction of MAX_EFFECTIVE_BALANCE then that fraction is the probability of being returned as proposer.

If the candidate is not chosen, then i is incremented, and we try again. Since the minimum effective balance is half of the maximum, then this ought to terminate fairly swiftly. In the worst case, all validators have 16 Ether effective balance, so the chance of having to do another iteration is 50%, in which case there is a one in a million chance of having to do 20 iterations.

Note that this dependence on the validators' effective balances, which are updated at the end of each epoch, means that proposer assignments are valid only in the current epoch. This is different from attestation committee assignments, which are valid with a one epoch look-ahead.

```
Used by get_beacon_proposer_index()
Uses compute_shuffled_index()
See also MAX_EFFECTIVE_BALANCE
```

compute_committee

compute_committee is used by get_beacon_committee() to find the specific members of one of the committees at a slot. Every epoch, a fresh set of committees is generated; during an epoch, the committees are stable.

Looking at the parameters in reverse order:

- count is the total number of committees in an epoch. This is SLOTS_PER_EPOCH times the output of get_committee_count_per_slot().
- index is the committee number within the epoch, running from 0 to count 1. It is calculated in get_beacon_committee() from the committee number in the slot index and the slot number as (slot % SLOTS_PER_EPOCH) * committees_per_slot + index.
- seed is the seed value for computing the pseudo-random shuffling, based on the epoch number and a domain parameter. (get_beacon_committee() uses DOMAIN_BEACON_ATTESTER.)
- indices is the list of validators eligible for inclusion in committees, namely the whole list of indices of active validators.

Random sampling among the validators is done by taking a contiguous slice of array indices from start to end and seeing where each one gets shuffled to by compute_shuffled_index(). Note that ValidatorIndex(i) is a type-cast in the above: it just turns i into a ValidatorIndex type for input into the shuffling. The output value of the shuffling is then used as an index into the indices list. There is much here that client implementations will optimise with caching and batch operations.

It may not be immediately obvious, but not all committees returned will be the same size (they can vary by one), and every validator in indices will be a member of exactly one committee. As we increment index from zero, clearly start for index == j + 1 is end for index == j, so there are no gaps. In addition, the highest index is count - 1, so every validator in indices finds its way into a committee. 104

This method of selecting committees is light client friendly. Light clients can compute only the committees that they are interested in without needing to deal with the entire validator set. See the section on Shuffling for explanation of how this works.

Sync committees are assigned by a different process that is more akin to repeatedly performing compute_proposer_index().

```
Used by get_beacon_committee
Uses compute_shuffled_index()
```

compute_epoch_at_slot

```
def compute_epoch_at_slot(slot: Slot) -> Epoch:
    """
    Return the epoch number at ``slot``.
    """
    return Epoch(slot // SLOTS_PER_EPOCH)
```

This is trivial enough that I won't explain it. But note that it does rely on GENESIS_SLOT and GENESIS_EPOCH being zero. The more pernickety among us might prefer it to read,

```
return GENESIS_EPOCH + Epoch((slot - GENESIS_SLOT) // SLOTS_PER_EPOCH)
```

compute_start_slot_at_epoch

```
def compute_start_slot_at_epoch(epoch: Epoch) -> Slot:
    """
    Return the start slot of ``epoch``.
    """
    return Slot(epoch * SLOTS_PER_EPOCH)
```

Maybe should read,

¹⁰⁴Also not immediately obvious is that there is a subtle issue with committee sizes that was discovered by formal verification, although, given the max supply of ETH it will never be triggered.

```
return GENESIS_SLOT + Slot((epoch - GENESIS_EPOCH) * SLOTS_PER_EPOCH))
```

```
Used by get_block_root(), compute_slots_since_epoch_start()
See also SLOTS_PER_EPOCH, GENESIS_SLOT, GENESIS_EPOCH
```

compute_activation_exit_epoch

```
def compute_activation_exit_epoch(epoch: Epoch) -> Epoch:
    """
    Return the epoch during which validator activations and exits initiated in ``epoch`` take effect.
    """
    return Epoch(epoch + 1 + MAX SEED LOOKAHEAD)
```

When queuing validators for activation or exit in process_registry_updates() and initiate_validator_exit() respectively, the activation or exit is delayed until the next epoch, plus MAX_SEED_LOOKAHEAD epochs, currently 4.

See MAX_SEED_LOOKAHEAD for the details, but in short it is designed to make it extremely hard for an attacker to manipulate the membership of committees via activations and exits.

```
Used by initiate_validator_exit(), process_registry_updates()
See also MAX_SEED_LOOKAHEAD
```

compute_fork_data_root

```
def compute_fork_data_root(current_version: Version, genesis_validators_root: Root) -> Root:
    """
    Return the 32-byte fork data root for the ``current_version`` and ``genesis_validators_root``.
    This is used primarily in signature domains to avoid collisions across forks/chains.
    """
    return hash_tree_root(ForkData(
        current_version=current_version,
        genesis_validators_root=genesis_validators_root,
    ))
```

The fork data root serves as a unique identifier for the chain that we are on. <code>genesis_validators_root</code> identifies our unique genesis event, and <code>current_version</code> our own hard fork subsequent to that genesis event. This is useful, for example, to differentiate between a testnet and mainnet: both might have the same fork versions, but will definitely have different genesis validator roots.

It is used by compute_fork_digest() and compute_domain().

```
Used by compute_fork_digest(), compute_domain()
Uses hash_tree_root()
See also ForkData
```

compute_fork_digest

```
def compute_fork_digest(current_version: Version, genesis_validators_root: Root) -> ForkDigest:
    """
    Return the 4-byte fork digest for the ``current_version`` and ``genesis_validators_root``.
    This is a digest primarily used for domain separation on the p2p layer.
    4-bytes suffices for practical separation of forks/chains.
    """
    return ForkDigest(compute_fork_data_root(current_version, genesis_validators_root)[:4])
```

Extracts the first four bytes of the fork data root as a ForkDigest type. It is primarily used for domain separation on the peer-to-peer networking layer.

compute_fork_digest() is used extensively in the Ethereum 2.0 networking specification to distinguish between independent beacon chain networks or forks: it is important that activity on one chain does not interfere with other chains.

```
Uses compute_fork_data_root()
See also ForkDigest
```

compute_domain

When dealing with signed messages, the signature "domains" are separated according to three independent factors:

- 1. All signatures include a DomainType relevant to the message's purpose, which is just some cryptographic hygiene in case the same message is to be signed for different purposes at any point.
- 2. All but signatures on deposit messages include the fork version. This ensures that messages across different forks of the chain become invalid, and that validators won't be slashed for signing attestations on two different chains (this is allowed).
- 3. And, now, the root hash of the validator Merkle tree at Genesis is included. Along with the fork version this gives a unique identifier for our chain.

This function is mainly used by get_domain(). It is also used in deposit processing, in which case fork_version and genesis_validators_root take their default values since deposits are valid across forks.

Fun fact: this function looks pretty simple, but I found a subtle bug in the way tests were generated in a previous implementation.

```
Used by get_domain(), process_deposit()
Uses compute_fork_data_root()
See also Domain, DomainType GENESIS_FORK_VERSION
```

compute_signing_root

```
def compute_signing_root(ssz_object: SSZObject, domain: Domain) -> Root:
    """
    Return the signing root for the corresponding signing data.
    """
    return hash_tree_root(SigningData(
        object_root=hash_tree_root(ssz_object),
         domain=domain,
    ))
```

This is a pre-processor for signing objects with BLS signatures:

1. calculate the hash tree root of the object;

- $2. \ combine \ the \ hash \ tree \ root \ with \ the \ {\tt Domain} \ inside \ a \ temporary \ {\tt SigningData} \ object;$
- 3. return the hash tree root of that, which is the data to be signed.

The domain is usually the output of get_domain(), which mixes in the cryptographic domain, the fork version, and the genesis validators root to the message hash. For deposits, it is the output of compute_domain(), ignoring the fork version and genesis validators root.

This is exactly equivalent to adding the domain to an object and taking the hash tree root of the whole thing. Indeed, this function used to be called <code>compute_domain_wrapper_root()</code>.

```
Used by Many places
Uses hash_tree_root()
See also SigningData, Domain
```

compute_timestamp_at_slot

Note: This function is unsafe with respect to overflows and underflows.

```
def compute_timestamp_at_slot(state: BeaconState, slot: Slot) -> uint64:
    slots_since_genesis = slot - GENESIS_SLOT
    return uint64(state.genesis_time + slots_since_genesis * SECONDS_PER_SLOT)
```

A simple utility for calculating the Unix timestamp at the start of the given slot. This is used when validating execution payloads.

This function was added in the Bellatrix pre-Merge upgrade.

```
Used by process_execution_payload()
```

Participation flags

These two simple utilities were added in the Altair upgrade.

add_flag

```
def add_flag(flags: ParticipationFlags, flag_index: int) -> ParticipationFlags:
    """
    Return a new ``ParticipationFlags`` adding ``flag_index`` to ``flags``.
    """
    flag = ParticipationFlags(2**flag_index)
    return flags | flag
```

This is simple and self-explanatory. The 2**flag_index is a bit Pythonic. In a C-like language it would use a bit-shift:

```
1 << flag_index
```

```
Used by process_attestation()
See also ParticipationFlags
```

has_flag

```
def has_flag(flags: ParticipationFlags, flag_index: int) -> bool:
    """
    Return whether ``flags`` has ``flag_index`` set.
    """
    flag = ParticipationFlags(2**flag_index)
    return flags & flag == flag
```

Move along now, nothing to see here.

Used by	<pre>get_unslashed_participating_indices(), process_attestation()</pre>
See also	ParticipationFlags

Beacon State Accessors

As the name suggests, these functions access the beacon state to calculate various useful things, without modifying it.

get_current_epoch

```
def get_current_epoch(state: BeaconState) -> Epoch:
    """
    Return the current epoch.
    """
    return compute_epoch_at_slot(state.slot)
```

A getter for the current epoch, as calculated by compute_epoch_at_slot().

```
Used by Everywhere
Uses compute_epoch_at_slot()
```

get_previous_epoch

```
def get_previous_epoch(state: BeaconState) -> Epoch:
    """"

Return the previous epoch (unless the current epoch is ``GENESIS_EPOCH``).
    """

current_epoch = get_current_epoch(state)
    return GENESIS EPOCH if current epoch == GENESIS EPOCH else Epoch(current epoch - 1)
```

Return the previous epoch number as an Epoch type. Returns GENESIS_EPOCH if we are in the GENESIS_EPOCH, since it has no prior, and we don't do negative numbers.

```
Used by Everywhere
Uses get_current_epoch()
See also GENESIS_EPOCH
```

get block root

```
def get_block_root(state: BeaconState, epoch: Epoch) -> Root:
    """
    Return the block root at the start of a recent ``epoch``.
    """
    return get_block_root_at_slot(state, compute_start_slot_at_epoch(epoch))
```

The Casper FFG part of consensus deals in Checkpoints that are the first slot of an epoch. <code>get_block_root</code> is a specialised version of <code>get_block_root_at_slot()</code> that returns the block root of the checkpoint, given only an epoch.

get_block_root_at_slot

```
def get_block_root_at_slot(state: BeaconState, slot: Slot) -> Root:
    """
    Return the block root at a recent ``slot``.
    """
    assert slot < state.slot <= slot + SLOTS_PER_HISTORICAL_ROOT
    return state.block_roots[slot % SLOTS_PER_HISTORICAL_ROOT]</pre>
```

Recent block roots are stored in a circular list in state, with a length of SLOTS_PER_HISTORICAL_ROOT (currently ~27 hours).

get_block_root_at_slot() is used by get_attestation_participation_flag_indices() to check whether
an attestation has voted for the correct chain head. It is also used in process_sync_aggregate() to find
the block that the sync committee is signing-off on.

```
Used by get_block_root(), get_attestation_participation_flag_indices(), process_sync_aggregate()

See also SLOTS_PER_HISTORICAL_ROOT, Root
```

get_randao_mix

```
def get_randao_mix(state: BeaconState, epoch: Epoch) -> Bytes32:
    """
    Return the randao mix at a recent ``epoch``.
    """
    return state.randao_mixes[epoch % EPOCHS_PER_HISTORICAL_VECTOR]
```

RANDAO mixes are stored in a circular list of length EPOCHS_PER_HISTORICAL_VECTOR. They are used when calculating the seed for assigning beacon proposers and committees.

The RANDAO mix for the current epoch is updated on a block-by-block basis as new RANDAO reveals come in. The mixes for previous epochs are the frozen RANDAO values at the end of the epoch.

```
Used by get_seed, process_randao_mixes_reset(), process_randao()
See also EPOCHS_PER_HISTORICAL_VECTOR
```

get_active_validator_indices

```
def get_active_validator_indices(state: BeaconState, epoch: Epoch) -> Sequence[ValidatorIndex]:
    """
    Return the sequence of active validator indices at ``epoch``.
    """
    return [ValidatorIndex(i) for i, v in enumerate(state.validators) if is active validator(v, epoch)]
```

Steps through the entire list of validators and returns the list of only the active ones. That is, the list of validators that have been activated but not exited as determined by is_active_validator().

This function is heavily used, and I'd expect it to be memoised in practice.

Used by	Many places
Uses	<pre>is_active_validator()</pre>

get_validator_churn_limit

```
def get_validator_churn_limit(state: BeaconState) -> uint64:
    """
    Return the validator churn limit for the current epoch.
    """
    active_validator_indices = get_active_validator_indices(state, get_current_epoch(state))
    return max(MIN_PER_EPOCH_CHURN_LIMIT, uint64(len(active_validator_indices)) // CHURN_LIMIT_QUOTIENT)
```

The "churn limit" applies when activating and exiting validators and acts as a rate-limit on changes to the validator set. The value returned by this function provides the number of validators that may become active in an epoch, and the number of validators that may exit in an epoch.

Some small amount of churn is always allowed, set by MIN_PER_EPOCH_CHURN_LIMIT, and the amount of perepoch churn allowed increases by one for every extra CHURN_LIMIT_QUOTIENT validators that are currently active (once the minimum has been exceeded).

In concrete terms, with 500,000 validators, this means that up to seven validators can enter or exit the active validator set each epoch (1,575 per day). At 524,288 active validators the limit will rise to eight per epoch (1,800 per day).

```
Used by initiate_validator_exit(), process_registry_updates()
Uses get_active_validator_indices()
See also MIN_PER_EPOCH_CHURN_LIMIT, CHURN_LIMIT_QUOTIENT
```

get_seed

Used in get_beacon_committee(), get_beacon_proposer_index(), and get_next_sync_committee_indices() to provide the randomness for computing proposers and committees. domain_type is DOMAIN_BEACON_ATTESTER, DOMAIN_BEACON_PROPOSER, and DOMAIN_SYNC_COMMITTEE respectively.

RANDAO mixes are stored in a circular list of length EPOCHS_PER_HISTORICAL_VECTOR. The seed for an epoch is based on the randao mix from MIN_SEED_LOOKAHEAD epochs ago. This is to limit the forward visibility of randomness: see the explanation there.

The seed returned is not based only on the domain and the randao mix, but the epoch number is also mixed in. This is to handle the pathological case of no blocks being seen for more than two epochs, in which case we run out of randao updates. That could lock in forever a non-participating set of block proposers. Mixing in the epoch number means that fresh committees and proposers can continue to be selected.

get_committee_count_per_slot

```
def get_committee_count_per_slot(state: BeaconState, epoch: Epoch) -> uint64:
    """
    Return the number of committees in each slot for the given ``epoch``.
    """
```

Every slot in a given epoch has the same number of beacon committees, as calculated by this function.

As far as the LMD GHOST consensus protocol is concerned, all the validators attesting in a slot effectively act as a single large committee. However, organising them into multiple committees gives two benefits.

- 1. Having multiple smaller committees reduces the load on the aggregators that collect and aggregate the attestations from committee members. This is important, as validating the signatures and aggregating them takes time. The downside is that blocks need to be larger, as, in the best case, there are up to 64 aggregate attestations to store per block rather than a single large aggregate signature over all attestations.
- 2. It maps well onto the future plans for data shards, when each committee will be responsible for committing to a block on one shard in addition to its current duties.

Since the original Phase 1 sharding design that required these committees has now been abandoned, the second of these points no longer applies.

There is always at least one committee per slot, and never more than MAX_COMMITTEES_PER_SLOT, currently 64.

Subject to these constraints, the actual number of committees per slot is N/4096, where N is the total number of active validators.

The intended behaviour looks like this:

- The ideal case is that there are MAX_COMMITTEES_PER_SLOT = 64 committees per slot. This maps to one committee per slot per shard once data sharding has been implemented. These committees will be responsible for voting on shard crosslinks. There must be at least 262,144 active validators to achieve this.
- If there are fewer active validators, then the number of committees per shard is reduced below 64 in order to maintain a minimum committee size of TARGET_COMMITTEE_SIZE = 128. In this case, not every shard will get crosslinked at every slot (once sharding is in place).
- Finally, only if the number of active validators falls below 4096 will the committee size be reduced to less than 128. With so few validators, the chain has no meaningful security in any case.

```
Used by get_beacon_committee(), process_attestation()
Uses get_active_validator_indices()
See also MAX_COMMITTEES_PER_SLOT, TARGET_COMMITTEE_SIZE
```

get_beacon_committee

Beacon committees vote on the beacon block at each slot via attestations. There are up to MAX_COMMITTEES_PER_SLOT beacon committees per slot, and each committee is active exactly once per epoch.

This function returns the list of committee members given a slot number and an index within that slot to select the desired committee, relying on compute committee() to do the heavy lifting.

Note that, since this uses get_seed(), we can obtain committees only up to EPOCHS_PER_HISTORICAL_VECTOR epochs into the past (minus MIN SEED LOOKAHEAD).

get_beacon_committee is used by get_attesting_indices() and process_attestation() when processing attestations coming from a committee, and by validators when checking their committee assignments and aggregation duties.

get_beacon_proposer_index

```
def get_beacon_proposer_index(state: BeaconState) -> ValidatorIndex:
    """
    Return the beacon proposer index at the current slot.
    """
    epoch = get_current_epoch(state)
    seed = hash(get_seed(state, epoch, DOMAIN_BEACON_PROPOSER) + uint_to_bytes(state.slot))
    indices = get_active_validator_indices(state, epoch)
    return compute_proposer_index(state, indices, seed)
```

Each slot, exactly one of the active validators is randomly chosen to be the proposer of the beacon block for that slot. The probability of being selected is weighted by the validator's effective balance in compute_proposer_index().

The chosen block proposer does not need to be a member of one of the beacon committees for that slot: it is chosen from the entire set of active validators for that epoch.

The RANDAO seed returned by get_seed() is updated once per epoch. The slot number is mixed into the seed using a hash to allow us to choose a different proposer at each slot. This also protects us in the case that there is an entire epoch of empty blocks. If that were to happen the RANDAO would not be updated, but we would still be able to select a different set of proposers for the next epoch via this slot number mix-in process.

There is a chance of the same proposer being selected in two consecutive slots, or more than once per epoch. If every validator has the same effective balance, then the probability of being selected in a particular slot is simply $\frac{1}{N}$ independent of any other slot, where N is the number of active validators in the epoch corresponding to the slot.

Currently, neither <code>get_beacon_proposer_index()</code> nor <code>compute_proposer_index()</code> filter out slashed validators. This could result in a slashed validator, prior to its exit, being selected to propose a block. Its block would, however, be invalid due to the check in <code>process_block_header()</code>. A fix for this has been proposed so as to avoid many missed slots (slots with invalid blocks) in the event of a mass slashing.

A simple utility that returns the total balance of all validators in the list, indices, passed in.

As an aside, there is an interesting example of some fragility in the spec lurking here. This function used to return a minimum of 1 Gwei to avoid a potential division by zero in the calculation of rewards and penalties. However, the rewards calculation was modified to avoid a possible integer overflow condition, without modifying this function, which re-introduced the possibility of a division by zero. This was later fixed by returning a minimum of EFFECTIVE_BALANCE_INCREMENT. The formal verification of the specification is helpful in avoiding issues like this.

```
Used by get_total_active_balance(), get_flag_index_deltas(), process_justification_and_finalization()

See also EFFECTIVE_BALANCE_INCREMENT
```

get_total_active_balance

Uses get_total_balance() to calculate the sum of the effective balances of all active validators in the current epoch.

This quantity is frequently used in the spec. For example, Casper FFG uses the total active balance to judge whether the 2/3 majority threshold of attestations has been reached in justification and finalisation. And it is a fundamental part of the calculation of rewards and penalties. The base reward is proportional to the reciprocal of the square root of the total active balance. Thus, validator rewards are higher when little balance is at stake (few active validators) and lower when much balance is at stake (many active validators).

Since it is calculated from effective balances, total active balance does not change during an epoch, so is a great candidate for being cached.

```
Used by get_flag_index_deltas(), process_justification_and_finalization(), get_base_reward_per_increment(), process_slashings(), process_sync_aggregate()

Uses get_total_balance(), get_active_validator_indices()
```

get domain

```
def get_domain(state: BeaconState, domain_type: DomainType, epoch: Epoch=None) -> Domain:
    """
    Return the signature domain (fork version concatenated with domain type) of a message.
    """
    epoch = get_current_epoch(state) if epoch is None else epoch
    fork_version = state.fork.previous_version if epoch < state.fork.epoch else state.fork.current_version
    return compute_domain(domain_type, fork_version, state.genesis_validators_root)</pre>
```

get_domain() pops up whenever signatures need to be verified, since a DomainType is always mixed in to
the signed data. For the science behind domains, see Domain types and compute_domain().

Except for DOMAIN_DEPOSIT, domains are always combined with the fork version before being used in signature generation. This is to distinguish messages from different chains, and ensure that validators don't get slashed if they choose to participate on two independent forks. (That is, deliberate forks, aka hard-forks. Participating on both branches of temporary consensus forks is punishable: that's basically the whole point of slashing.)

Note that a message signed under one fork version will be valid during the next fork version, but not thereafter. So, for example, voluntary exit messages signed during Altair will be valid after the Bellatrix beacon chain upgrade, but not after the Capella upgrade. Voluntary exit messages signed during Phase 0 are valid under Altair but were made invalid by the Bellatrix upgrade¹⁰⁵.

```
Used by is_valid_indexed_attestation(), verify_block_signature(), process_randao(), process_proposer_slashing(), process_voluntary_exit(), process_sync_aggregate()

Uses compute_domain()

See also DomainType, Domain types
```

get indexed attestation

```
def get_indexed_attestation(state: BeaconState, attestation: Attestation) -> IndexedAttestation:
    """
    Return the indexed attestation corresponding to ``attestation``.
    """
    attesting_indices = get_attesting_indices(state, attestation.data, attestation.aggregation_bits)

return IndexedAttestation(
    attesting_indices=sorted(attesting_indices),
    data=attestation.data,
    signature=attestation.signature,
)
```

Lists of validators within committees occur in two forms in the specification.

- They can be compressed into a bitlist, in which each bit represents the presence or absence of a validator from a particular committee. The committee is referenced by slot, and committee index within that slot. This is how sets of validators are represented in Attestations.
- Or they can be listed explicitly by their validator indices, as in IndexedAttestations. Note that the list of indices is sorted: an attestation is invalid if not.

get_indexed_attestation() converts from the former representation to the latter. The slot number and
the committee index are provided by the AttestationData and are used to reconstruct the committee
members via get_beacon_committee(). The supplied bitlist will have come from an Attestation.

Attestations are aggregatable, which means that attestations from multiple validators making the same vote can be rolled up into a single attestation through the magic of BLS signature aggregation. However, in order to be able to verify the signature later, a record needs to be kept of which validators actually contributed to the attestation. This is so that those validators' public keys can be aggregated to match the construction of the signature.

The conversion from the bit-list format to the list format is performed by get_attesting_indices(), below.

```
Used by process_attestation()
Uses get_attesting_indices()
```

¹⁰⁵There is some discussion around changing this to make voluntary exit messages fork-agnostic in future, but that has not yet been implemented.

See also Attestation, IndexedAttestation

get_attesting_indices

As described under <code>get_indexed_attestation()</code>, lists of validators come in two forms. This routine converts from the compressed form, in which validators are represented as a subset of a committee with their presence or absence indicated by a 1 bit or a 0 bit respectively, to an explicit list of <code>ValidatorIndex</code> types.

```
Used by get_indexed_attestation(), process_attestation()
Uses get_beacon_committee()
See also AttestationData, IndexedAttestation
```

get_next_sync_committee_indices

```
def get_next_sync_committee_indices(state: BeaconState) -> Sequence[ValidatorIndex]:
    Return the sync committee indices, with possible duplicates, for the next sync committee.
    epoch = Epoch(get_current_epoch(state) + 1)
    MAX RANDOM BYTE = 2**8 - 1
    active_validator_indices = get_active_validator_indices(state, epoch)
    active_validator_count = uint64(len(active_validator_indices))
    seed = get_seed(state, epoch, DOMAIN_SYNC_COMMITTEE)
    i = 0
    sync committee indices: List[ValidatorIndex] = []
    while len(sync committee indices) < SYNC COMMITTEE SIZE:</pre>
        shuffled_index = compute_shuffled_index(uint64(i % active_validator_count),
                                         \hookrightarrow active validator count, seed)
        candidate_index = active_validator_indices[shuffled_index]
        random_byte = hash(seed + uint_to_bytes(uint64(i // 32)))[i % 32]
        effective_balance = state.validators[candidate_index].effective_balance
        if effective_balance * MAX_RANDOM_BYTE >= MAX_EFFECTIVE_BALANCE * random_byte:
            sync_committee_indices.append(candidate_index)
        i += 1
    return sync_committee_indices
```

<code>get_next_sync_committee_indices()</code> is used to select the subset of validators that will make up a sync committee. The committee size is <code>SYNC_COMMITTEE_SIZE</code>, and the committee is allowed to contain duplicates, that is, the same validator more than once. This is to <code>handle gracefully</code> the situation of there being fewer active validators than <code>SYNC_COMMITTEE_SIZE</code>.

Similarly to being chosen to propose a block, the probability of any validator being selected for a sync committee is proportional to its effective balance. Thus, the algorithm is almost the same as that of compute_proposer_index(), except that this one exits only after finding SYNC_COMMITTEE_SIZE members, rather than exiting as soon as a candidate is found. Both routines use the try-and-increment method to weight the probability of selection with the validators' effective balances.

It's fairly clear why block proposers are selected with a probability proportional to their effective balances: block production is subject to slashing, and proposers with less at stake have less to slash, so we reduce

their influence accordingly. It is not so clear why the probability of being in a sync committee is also proportional to a validator's effective balance; sync committees are not subject to slashing. It has to do with keeping calculations for light clients simple. We don't want to burden light clients with summing up validators' balances to judge whether a 2/3 supermajority of stake in the committee has voted for a block. Ideally, they can just count the participation flags. To make this somewhat reliable, we weight the probability that a validator participates in proportion to its effective balance.

get_next_sync_committee

Note: The function <code>get_next_sync_committee</code> should only be called at sync committee period boundaries and when upgrading state to Altair.

The random seed that generates the sync committee is based on the number of the next epoch. <code>get_next_sync_committee_indices()</code> doesn't contain any check that the epoch corresponds to a sync-committee change boundary, which allowed the timing of the Altair upgrade to be more flexible. But a consequence is that you will get an incorrect committee if you call <code>get_next_sync_committee()</code> at the wrong time.

```
def get_next_sync_committee(state: BeaconState) -> SyncCommittee:
    """
    Return the next sync committee, with possible pubkey duplicates.
    """
    indices = get_next_sync_committee_indices(state)
    pubkeys = [state.validators[index].pubkey for index in indices]
    aggregate_pubkey = eth_aggregate_pubkeys(pubkeys)
    return SyncCommittee(pubkeys=pubkeys, aggregate_pubkey=aggregate_pubkey)
```

get_next_sync_committee() is a simple wrapper around get_next_sync_committee_indices() that
packages everything up into a nice SyncCommittee object.

See the SyncCommittee type for an explanation of how the aggregate_pubkey is intended to be used.

```
Used by process_sync_committee_updates(), initialize_beacon_state_from_eth1()
Uses get_next_sync_committee_indices(), eth_aggregate_pubkeys()
See also SyncCommittee
```

get_unslashed_participating_indices

get_unslashed_participating_indices() returns the list of validators that made a timely attestation with the type flag_index during the epoch in question.

It is used with the <code>TIMELY_TARGET_FLAG_INDEX</code> flag in <code>process_justification_and_finalization()</code> to calculate the proportion of stake that voted for the candidate checkpoint in the current and previous epochs.

It is also used with the TIMELY_TARGET_FLAG_INDEX for applying inactivity penalties in process_inactivity_updates() and get_inactivity_penalty_deltas(). If a validator misses a correct target vote during an inactivity leak then it is considered not to have participated at all (it is not contributing anything useful).

And it is used in get_flag_index_deltas() for calculating rewards due for each type of correct vote.

Slashed validators are ignored. Once slashed, validators no longer receive rewards or participate in consensus, although they are subject to penalties until they have finally been exited.

```
Used by get_flag_index_deltas(), process_justification_and_finalization(), process_inactivity_updates(), get_inactivity_penalty_deltas()

Uses get_active_validator_indices(), has_flag()

See also Participation flag indices
```

get_attestation_participation_flag_indices

```
def get_attestation_participation_flag_indices(state: BeaconState,
                                                data: AttestationData,
                                                inclusion_delay: uint64) -> Sequence[int]:
    Return the flag indices that are satisfied by an attestation.
    if data.target.epoch == get_current_epoch(state):
        justified_checkpoint = state.current_justified_checkpoint
    else:
        justified checkpoint = state.previous justified checkpoint
    # Matching roots
    is matching source = data.source == justified checkpoint
    is_matching_target = is_matching_source and data.target.root == get_block_root(state,

    data.target.epoch)
    is_matching_head = is_matching_target and data.beacon_block_root == get_block_root_at_slot(state,
                                         \hookrightarrow data.slot)
    assert is_matching_source
    participation flag indices = []
    if is matching source and inclusion delay <= integer squareroot(SLOTS PER EPOCH):
        participation flag indices.append(TIMELY SOURCE FLAG INDEX)
    if is matching target and inclusion delay <= SLOTS PER EPOCH:</pre>
        participation_flag_indices.append(TIMELY_TARGET_FLAG_INDEX)
    if is_matching_head and inclusion_delay == MIN_ATTESTATION_INCLUSION_DELAY:
        participation flag indices.append(TIMELY HEAD FLAG INDEX)
    return participation flag indices
```

This is called by process_attestation() during block processing, and is the heart of the mechanism for recording validators' votes as contained in their attestations. It filters the given attestation against the beacon state's current view of the chain, and returns participation flag indices only for the votes that are both correct and timely.

data is an AttestationData object that contains the source, target, and head votes of the validators that contributed to the attestation. The attestation may represent the votes of one or more validators.

inclusion_delay is the difference between the current slot on the beacon chain and the slot for which the
attestation was created. For the block containing the attestation to be valid, inclusion_delay must be

between MIN_ATTESTATION_INCLUSION_DELAY and SLOTS_PER_EPOCH inclusive. In other words, attestations must be included in the next block, or in any block up to 32 slots later, after which they are ignored.

Since the attestation may be up to 32 slots old, it might have been generated in the current epoch or the previous epoch, so the first thing we do is to check the attestation's target vote epoch to see which epoch we should be looking at in the beacon state.

Next, we check whether each of the votes in the attestation are correct:

- Does the attestation's source vote match what we believe to be the justified checkpoint in the epoch in question?
- If so, does the attestation's target vote match the head block at the epoch's checkpoint, that is, the first slot of the epoch?
- If so, does the attestation's head vote match what we believe to be the head block at the attestation's slot? Note that the slot may not contain a block it may be a skip slot in which case the last known block is considered to be the head.

These three build on each other, so that it is not possible to have a correct target vote without a correct source vote, and it is not possible to have a correct head vote without a correct target vote.

The assert statement is interesting. If an attestation does not have the correct source vote, the block containing it is invalid and is discarded. Having an incorrect source vote means that the block proposer disagrees with me about the last justified checkpoint, which is an irreconcilable difference.

After checking the validity of the votes, the timeliness of each vote is checked. Let's take them in reverse order.

- Correct head votes must be included immediately, that is, in the very next slot.
 - Head votes, used for LMD GHOST consensus, are not useful after one slot.
- Correct target votes must be included within 32 slots, one epoch.
 - Target votes are useful at any time, but it is simpler if they don't span more than a couple of epochs, so 32 slots is a reasonable limit. This check is actually redundant since attestations in blocks cannot be older than 32 slots.
- Correct source votes must be included within 5 slots (integer squareroot(32)).
 - This is the geometric mean of 1 (the timely head threshold) and 32 (the timely target threshold). This is an arbitrary choice. Vitalik's view¹⁰⁶ is that, with this setting, the cumulative timeliness rewards most closely match an exponentially decreasing curve, which "feels more logical".

The timely inclusion requirements are new in Altair. In Phase 0, all correct votes received a reward, and there was an additional reward for inclusion the was proportional to the reciprocal of the inclusion distance. This led to an oddity where it was always more profitable to vote for a correct head, even if that meant waiting longer and risking not being included in the next slot.

```
Used by process_attestation()
Uses get_block_root(), get_block_root_at_slot(), integer_squareroot()
See also Participation flag indices, AttestationData, MIN_ATTESTATION_INCLUSION_DELAY
```

get_flag_index_deltas

```
def get_flag_index_deltas(state: BeaconState, flag_index: int) -> Tuple[Sequence[Gwei], Sequence[Gwei]]:
    """
    Return the deltas for a given ``flag_index`` by scanning through the participation flags.
    """
    rewards = [Gwei(0)] * len(state.validators)
```

 $^{^{106}\}mathrm{From}$ a conversation on the Ethereum Research Discord server.

```
penalties = [Gwei(0)] * len(state.validators)
previous_epoch = get_previous_epoch(state)
unslashed participating indices = get unslashed participating indices(state, flag index,
                                     \hookrightarrow previous_epoch)
weight = PARTICIPATION_FLAG_WEIGHTS[flag_index]
unslashed_participating_balance = get_total_balance(state, unslashed_participating_indices)
unslashed\_participating\_increments = unslashed\_participating\_balance // \ EFFECTIVE\_BALANCE\_INCREMENT
active_increments = get_total_active_balance(state) // EFFECTIVE_BALANCE_INCREMENT
for index in get_eligible_validator_indices(state):
    base_reward = get_base_reward(state, index)
    if index in unslashed_participating_indices:
        if not is_in_inactivity_leak(state):
            reward numerator = base reward * weight * unslashed participating increments
            rewards[index] += Gwei(reward numerator // (active increments * WEIGHT DENOMINATOR))
    elif flag_index != TIMELY_HEAD_FLAG_INDEX:
        penalties[index] += Gwei(base_reward * weight // WEIGHT_DENOMINATOR)
return rewards, penalties
```

This function is used during epoch processing to assign rewards and penalties to individual validators based on their voting record in the previous epoch. Rewards for block proposers for including attestations are calculated during block processing. The "deltas" in the function name are the separate lists of rewards and penalties returned. Rewards and penalties are always treated separately to avoid negative numbers.

The function is called once for each of the flag types corresponding to correct attestation votes: timely source, timely target, timely head.

The list of validators returned by get_unslashed_participating_indices() contains the ones that will be rewarded for making this vote type in a timely and correct manner. That routine uses the flags set in state for each validator by process_attestation() during block processing and returns the validators for which the corresponding flag is set.

Every active validator is expected to make an attestation exactly once per epoch, so we then cycle through the entire set of active validators, rewarding them if they appear in unslashed_participating_indices, as long as we are not in an inactivity leak. If we are in a leak, no validator is rewarded for any of its votes, but penalties still apply to non-participating validators.

Notice that the reward is weighted with unslashed_participating_increments, which is proportional to the total stake of the validators that made a correct vote with this flag. This means that, if participation by other validators is lower, then my rewards are lower, even if I perform my duties perfectly. The reason for this is to do with discouragement attacks (see also this nice explainer¹⁰⁷). In short, with this mechanism, validators are incentivised to help each other out (e.g. by forwarding gossip messages, or aggregating attestations well) rather than to attack or censor one-another.

Validators that did not make a correct and timely vote are penalised with a full weighted base reward for each flag that they missed, except for missing the head vote. Head votes have only a single slot to get included, so a missing block in the next slot is sufficient to cause a miss, but is completely outside the attester's control. Thus, head votes are only rewarded, not penalised. This also allows perfectly performing validators to break even during an inactivity leak, when we expect at least a third of blocks to be missing: they receive no rewards, but ideally no penalties either.

Untangling the arithmetic, the maximum total issuance due to rewards for attesters in an epoch, I_A , comes out as follows, in the notation described later.

$$I_A = \frac{W_s + W_t + W_h}{W_{\Sigma}} NB$$

Used by process_rewards_and_penalties()

¹⁰⁷Unfortunately, the original page, https://hackingresear.ch/discouragement-attacks/ seems to be unavailable now. The link in the text is to archive.org, but their version is a bit broken.

<pre>get_unslashed_participating_indices(), get_total_balance(), get_total_active_balance(), get_eligible_validator_indices(), get_base_reward(), is in inactivity leak()</pre>
process attestation(), participation flag indices, rewards and penalties

Beacon State Mutators

increase balance

```
def increase_balance(state: BeaconState, index: ValidatorIndex, delta: Gwei) -> None:
    """
    Increase the validator balance at index ``index`` by ``delta``.
    """
    state.balances[index] += delta
```

After creating a validator with its deposit balance, this and decrease_balance() are the only places in the spec where validator balances are ever modified.

We need two separate functions to change validator balances, one to increase them and one to decrease them, since we are using only unsigned integers.

Fun fact: A typo around this led to Teku's one and only consensus failure at the initial client interop event. Unsigned integers induce bugs!

decrease_balance

```
def decrease_balance(state: BeaconState, index: ValidatorIndex, delta: Gwei) -> None:
    """
    Decrease the validator balance at index ``index`` by ``delta``, with underflow protection.
    """
    state.balances[index] = 0 if delta > state.balances[index] else state.balances[index] - delta
```

The counterpart to increase_balance(). This has a little extra work to do to check for unsigned int underflow since balances may not go negative.

initiate_validator_exit

```
def initiate_validator_exit(state: BeaconState, index: ValidatorIndex) -> None:
    """
    Initiate the exit of the validator with index ``index``.
    """
    # Return if validator already initiated exit
    validator = state.validators[index]
    if validator.exit_epoch != FAR_FUTURE_EPOCH:
        return

# Compute exit queue epoch
    exit_epochs = [v.exit_epoch for v in state.validators if v.exit_epoch != FAR_FUTURE_EPOCH]
    exit_queue_epoch = max(exit_epochs + [compute_activation_exit_epoch(get_current_epoch(state))])
```

Exits may be initiated voluntarily, as a result of being slashed, or by dropping to the EJECTION_BALANCE threshold.

In all cases, a dynamic "churn limit" caps the number of validators that may exit per epoch. This is calculated by get_validator_churn_limit(). The mechanism for enforcing this is the exit queue: the validator's exit_epoch is set such that it is at the end of the queue.

The exit queue is not maintained as a separate data structure, but is continually re-calculated from the exit epochs of all validators and allowing for a fixed number to exit per epoch. I expect there are some optimisations to be had around this in actual implementations.

An exiting validator is expected to continue with its proposing and attesting duties until its exit_epoch has passed, and will continue to receive rewards and penalties accordingly.

In addition, an exited validator remains eligible to be slashed until its withdrawable_epoch, which is set to MIN_VALIDATOR_WITHDRAWABILITY_DELAY epochs after its exit_epoch. This is to allow some extra time for any slashable offences by the validator to be detected and reported.

```
Used by slash_validator(), process_registry_updates(), process_voluntary_exit()
Uses compute_activation_exit_epoch(), get_validator_churn_limit()
See also Voluntary Exits, MIN_VALIDATOR_WITHDRAWABILITY_DELAY
```

slash_validator

```
def slash validator(state: BeaconState,
                    slashed index: ValidatorIndex,
                    whistleblower_index: ValidatorIndex=None) -> None:
    Slash the validator with index ``slashed_index``.
    epoch = get_current_epoch(state)
   initiate_validator_exit(state, slashed_index)
   validator = state.validators[slashed_index]
   validator.slashed = True
   validator.withdrawable_epoch = max(validator.withdrawable_epoch, Epoch(epoch +
                                        \hookrightarrow EPOCHS PER SLASHINGS VECTOR))
   state.slashings[epoch % EPOCHS PER SLASHINGS VECTOR] += validator.effective balance
   slashing penalty = validator.effective balance // MIN SLASHING PENALTY QUOTIENT BELLATRIX
   decrease balance(state, slashed index, slashing penalty)
   # Apply proposer and whistleblower rewards
   proposer_index = get_beacon_proposer_index(state)
    if whistleblower_index is None:
        whistleblower_index = proposer_index
   whistleblower_reward = Gwei(validator.effective_balance // WHISTLEBLOWER_REWARD QUOTIENT)
   proposer reward = Gwei(whistleblower reward * PROPOSER WEIGHT // WEIGHT DENOMINATOR)
    increase balance(state, proposer index, proposer reward)
    increase_balance(state, whistleblower_index, Gwei(whistleblower_reward - proposer_reward))
```

Both proposer slashings and attester slashings end up here when a report of a slashable offence has been verified during block processing.

When a validator is slashed, several things happen immediately:

• The validator is processed for exit via initiate_validator_exit(), so it joins the exit queue.

- The validator is marked as slashed. This information is used when calculating rewards and penalties: while being exited, whatever it does, a slashed validator receives penalties as if it had failed to propose or attest, including the inactivity leak if applicable.
- Normally, as part of the exit process, the withdrawable_epoch for a validator (the point at which a validator's stake is in principle unlocked) is set to MIN_VALIDATOR_WITHDRAWABILITY_DELAY epochs after it exits. When a validator is slashed, a much longer period of lock-up applies, namely EPOCHS_PER_SLASHINGS_VECTOR. This is to allow a further, potentially much greater, slashing penalty to be applied later once the chain knows how many validators have been slashed together around the same time. The postponement of the withdrawable epoch is twice as long as required to apply the extra penalty, which is applied half-way through the period. This simply means that slashed validators continue to accrue attestation penalties for some 18 days longer than necessary. Treating slashed validators fairly is not a big priority for the protocol.
- The effective balance of the validator is added to the accumulated effective balances of validators slashed this epoch, and stored in the circular list, state.slashings. This will later be used by the slashing penalty calculation mentioned in the previous point.
- An initial "slap on the wrist" slashing penalty of the validator's effective balance (in Gwei) divided by the MIN_SLASHING_PENALTY_QUOTIENT_BELLATRIX is applied. For a validator with a full Effective Balance of 32 ETH, this initial penalty is 1 ETH.
- The block proposer that included the slashing proof receives a reward.

In short, a slashed validator receives an initial minor penalty, can expect to receive a further penalty later, and is marked for exit.

Note that the whistleblower_index defaults to None in the parameter list. This is never used in Phase 0, with the result that the proposer that included the slashing gets the entire whistleblower reward; there is no separate whistleblower reward for the finder of proposer or attester slashings. One reason is simply that reports are too easy to steal: if I report a slashable event to a block proposer, there is nothing to prevent that proposer claiming the report as its own. We could introduce some fancy ZK protocol to make this trustless, but this is what we're going with for now. Later developments, such as the proof-of-custody game, may reward whistleblowers directly.

Used by	<pre>process_proposer_slashing(), process_attester_slashing()</pre>
Uses	<pre>initiate_validator_exit(), get_beacon_proposer_index(), decrease_balance(), increase_balance()</pre>
See also	<pre>EPOCHS_PER_SLASHINGS_VECTOR, MIN_SLASHING_PENALTY_QUOTIENT_BELLATRIX, process_slashings()</pre>

Beacon Chain State Transition Function

Preamble

State transitions

The state transition function is at the heart of what blockchains do. Each node on the network maintains a state that corresponds to its view of the state of the world.

Classically, the node's state is updated by applying blocks, in order, with a "state transition function". The state transition function is "pure" in that its output depends only on the input, and it has no side effects. This makes it deterministic: if every node starts with the same state (the Genesis state), and applies the same sequence of blocks, then all nodes must end up with the same resulting state. If for some reason they don't, then we have a consensus failure.

If S is a beacon state, and B a beacon block, then the state transition function f can be written

$$S' \equiv f(S, B)$$

In this equation we call S the pre-state (the state before applying the block B), and S' the post-state. The function f is then iterated as we receive new blocks to constantly update the state.

That's the essence of blockchain progress in its purest form, as it existed under proof of work; under proof of work, the state transition function is driven exclusively by processing blocks.

The beacon chain, however, is not block-driven. Rather, it is slot-driven. Updates to the state depends on the progress of slots, whether or not that slot has a block associated with it.

Thus, the beacon chain's state transition function comprises three elements.

- 1. A per-slot transition function, $S' \equiv f_s(S)$. (The state contains the slot number, so we do not need to supply it.)
- 2. A per-block transition function $S' \equiv f_b(S, B)$.
- 3. A per-epoch transition function $S' \equiv f_e(S)$.

Each of these state transition functions needs to be run at the appropriate point when updating the chain, and it is the role of this part of the beacon chain specification to define all of this precisely.

Validity conditions

The post-state corresponding to a pre-state state and a signed block signed_block is defined as state_transition(state, signed_block). State transitions that trigger an unhandled exception (e.g. a failed assert or an out-of-range list access) are considered invalid. State transitions that cause a uint64 overflow or underflow are also considered invalid.

This is a very important statement of how the spec deals with invalid conditions and errors. Basically, if any block is processed that would trigger any kind of exception in the Python code of the specification, then that block is invalid and must be rejected. That means having to undo any state modifications already made in the course of processing the block.

People who do formal verification of the specification don't much like this, as having assert statements in running code is an anti-pattern: it is better to ensure that your code can simply never fail.

Specification

Anyway, as discussed above, the beacon chain state transition has three elements:

- 1. slot processing, which is performed for every slot regardless of what else is happening;
- 2. epoch processing, which happens every SLOTS_PER_EPOCH (32) slots, again regardless of whatever else is going on; and,
- 3. block processing, which happens only in slots for which a beacon block has been received.

Although the beacon chain's state transition is conceptually slot-driven, as the spec is written a state transition is triggered by receiving a block to process. That means that we first need to fast-forward from our current slot number in the state (which is the slot at which we last processed a block) to the slot of the block we are processing. We treat intervening slots, if any, as empty. This "fast-forward" is done by process_slots(), which also triggers epoch processing as required.

In actual client implementations, state updates will usually be time-based, triggered by moving to the next slot if a block has not been received. However, the fast-forward functionality will be used when exploring different forks in the block tree.

The validate_result parameter defaults to True, meaning that the block's signature will be checked, and that the result of applying the block to the state results in the same state root that the block claims it does (the "post-states" must match). When creating blocks, however, proposers can set validate_result to False in order to allow the state root to be calculated, else we'd have a circular dependency. The signature over the initial candidate block is omitted to avoid bad interactions with slashing protection when signing twice in a slot.

Check that the signature on the block matches the block's contents and the public key of the claimed proposer of the block. This ensures that blocks cannot be forged, or tampered with in transit. All the public keys for validators are stored in the Validators list in state.

```
Used by state_transition()
Uses compute_signing_root(), get_domain(), bls.Verify()
See also DOMAIN_BEACON_PROPOSER
```

Updates the state from its current slot up to the given slot number assuming that all the intermediate slots are empty (that they do not contain blocks). Iteratively calls process_slot() to apply the empty slot state-transition.

This is where epoch processing is triggered when required. Empty slot processing is lightweight, but any epoch transitions that need to be processed require the full rewards and penalties, and justification–finalisation apparatus.

```
Used by state_transition()
Uses process_slot(), process_epoch()
See also SLOTS_PER_EPOCH
```

```
def process_slot(state: BeaconState) -> None:
    # Cache state root
    previous_state_root = hash_tree_root(state)
    state.state_roots[state.slot % SLOTS_PER_HISTORICAL_ROOT] = previous_state_root
    # Cache latest block header state root
    if state.latest_block_header.state_root == Bytes32():
        state.latest_block_header.state_root = previous_state_root
    # Cache block root
    previous_block_root = hash_tree_root(state.latest_block_header)
    state.block roots[state.slot % SLOTS PER HISTORICAL ROOT] = previous_block_root
```

Apply a single slot state-transition (but updating the slot number, and any required epoch processing is handled by process_slots()). This is done at each slot whether or not there is a block present; if there is no block present then it is the only thing that is done.

Slot processing is almost trivial and consists only of calculating the updated state and block hash tree roots (as necessary), and storing them in the historical lists in the state. In a circular way, the state roots only change over an empty slot state transition due to updating the lists of state and block roots.

SLOTS_PER_HISTORICAL_ROOT is a multiple of SLOTS_PER_EPOCH, so there is no danger of overwriting the circular lists of state_roots and block_roots. These will be dealt with correctly during epoch processing.

The only curiosity here is the lines,

```
if state.latest_block_header.state_root == Bytes32():
    state.latest_block_header.state_root = previous_state_root
```

This logic was introduced to avoid a circular dependency while also keeping the state transition clean. Each block that we receive contains a post-state root, but as part of state processing we store the block in the state (in state.latest_block_header), thus changing the post-state root.

Therefore, to be able to verify the state transition, we use the convention that the state root of the incoming block, and the state root that we calculate after inserting the block into the state, are both based on a *temporary* block header that has a stubbed state root, namely Bytes32(). This allows the block's claimed post-state root to validated without the circularity. The next time that process_slots() is called, the block's stubbed state root is updated to the actual post-state root, as above.

```
Used by process_slots()
Uses hash_tree_root
See also SLOTS_PER_HISTORICAL_ROOT
```

Execution engine

Ethereum's "Merge" to proof of stake occurred on the 15th of September 2022. As far as the beacon chain was concerned, the most significant change was that an extra block validity condition now applies. Post-Merge Beacon blocks contain a new ExecutionPayload object which is basically an Eth1 block. For the beacon block to be valid, the contents of its execution payload must be valid according to Ethereum's longstanding block and transaction execution rules (minus any proof of work conditions).

The beacon chain does not know how to validate Ethereum transactions. The entire point of the Merge was to enable beacon chain clients to hand off the validation of the execution payload to a locally

connected execution client (formerly an Eth1 client). The beacon chain consensus client does this hand-off via the notify_new_payload() function described below.

Architecturally, the notify_new_payload() function is accessed via a new interface called the Engine API which the Bellatrix specification characterises as follows.

The implementation-dependent ExecutionEngine protocol encapsulates the execution sub-system logic via:

- a state object $self.execution_state$ of type ExecutionState
- a notification function self.notify_new_payload which may apply changes to the self.execution state

Note: notify_new_payload is a function accessed through the <code>EXECUTION_ENGINE</code> module which instantiates the <code>ExecutionEngine</code> protocol.

The body of this function is implementation dependent. The Engine API may be used to implement this and similarly defined functions via an external execution engine.

notify_new_payload

This function is called during block processing to verify the validity of a beacon block's execution payload. The contents of the execution payload are largely opaque to the consensus layer (hence the ... in the function definition) and validation of the execution payload relies almost entirely on the execution client. You can think of it as just an external black-box library call if that helps.

```
Used by process_execution_payload()
```

Epoch processing

```
def process_epoch(state: BeaconState) -> None:
    process_justification_and_finalization(state) # [Modified in Altair]
    process_inactivity_updates(state) # [New in Altair]
    process_rewards_and_penalties(state) # [Modified in Altair]
    process_registry_updates(state)
    process_slashings(state) # [Modified in Altair]
    process_ethl_data_reset(state)
    process_effective_balance_updates(state)
    process_slashings_reset(state)
    process_randao_mixes_reset(state)
    process_historical_summaries_update(state) # [Modified in Capella]
    process_participation_flag_updates(state) # [New in Altair]
    process_sync_committee_updates(state) # [New in Altair]
```

The long laundry list of things that need to be done at the end of an epoch. You can see from the comments that a bunch of extra work was added in the Altair upgrade.

```
Used by process_slots()
Uses All the things below
```

Justification and finalization

I believe the corner cases mentioned in the comments are related to Issue 849¹⁰⁸. In any case, skipping justification and finalisation calculations during the first two epochs definitely simplifies things.

For the purposes of the Casper FFG finality calculations, we want attestations that have both source and target votes we agree with. If the source vote is incorrect, then the attestation is never processed into the state, so we just need the validators that voted for the correct target, according to their participation flag indices.

Since correct target votes can be included up to 32 slots after they are made, we collect votes from both the previous epoch and the current epoch to ensure that we have them all.

Once we know which validators voted for the correct source and head in the current and previous epochs, we add up their effective balances (not actual balances). total_active_balance is the sum of the effective balances for all validators that ought to have voted during the current epoch. Slashed, but not exited validators are not included in these calculations.

These aggregate balances are passed to weigh_justification_and_finalization() to do the actual work of updating justification and finalisation.

```
def weigh_justification_and_finalization(state: BeaconState,
                                         total_active_balance: Gwei,
                                         previous epoch target balance: Gwei,
                                         current epoch target balance: Gwei) -> None:
    previous epoch = get previous epoch(state)
    current epoch = get current epoch(state)
    old_previous_justified_checkpoint = state.previous_justified_checkpoint
   old_current_justified_checkpoint = state.current_justified_checkpoint
   # Process justifications
   state.previous_justified_checkpoint = state.current_justified_checkpoint
   state.justification\_bits[1:] = state.justification\_bits[:JUSTIFICATION\_BITS\_LENGTH \ - \ 1]
   state.justification\_bits[0] = 0b0
    if previous epoch target balance * 3 >= total active balance * 2:
        state.current_justified_checkpoint = Checkpoint(epoch=previous_epoch,
                                                        root=get block root(state, previous epoch))
        state.justification_bits[1] = 0b1
   if current_epoch_target_balance * 3 >= total_active_balance * 2:
```

¹⁰⁸Worth a visit if only to have a chuckle at Jacek's description of uints as "ugly integers".

```
state.current_justified_checkpoint = Checkpoint(epoch=current_epoch,
                                                    root=get block root(state, current epoch))
    state.justification bits[0] = 0b1
# Process finalizations
bits = state.justification bits
# The 2nd/3rd/4th most recent epochs are justified, the 2nd using the 4th as source
if all(bits[1:4]) and old_previous_justified_checkpoint.epoch + 3 == current_epoch:
    state.finalized_checkpoint = old_previous_justified_checkpoint
# The 2nd/3rd most recent epochs are justified, the 2nd using the 3rd as source
if all(bits[1:3]) and old_previous_justified_checkpoint.epoch + 2 == current_epoch:
    state.finalized_checkpoint = old_previous_justified_checkpoint
# The 1st/2nd/3rd most recent epochs are justified, the 1st using the 3rd as source
if all(bits[0:3]) and old current justified checkpoint.epoch + 2 == current epoch:
    state.finalized_checkpoint = old_current_justified_checkpoint
# The 1st/2nd most recent epochs are justified, the 1st using the 2nd as source
if all(bits[0:2]) and old_current_justified_checkpoint.epoch + 1 == current_epoch:
    state.finalized_checkpoint = old_current_justified_checkpoint
```

This routine handles justification first, and then finalisation.

Justification

A supermajority link is a vote with a justified source checkpoint C_m and a target checkpoint C_n that was made by validators controlling more than two-thirds of the stake. If a checkpoint has a supermajority link pointing to it then we consider it justified. So, if more than two-thirds of the validators agree that checkpoint 3 was justified (their source vote) and have checkpoint 4 as their target vote, then we justify checkpoint 4.

We know that all the attestations have source votes that we agree with. The first if statement tries to justify the previous epoch's checkpoint seeing if the (source, target) pair is a supermajority. The second if statement tries to justify the current epoch's checkpoint. Note that the previous epoch's checkpoint might already have been justified; this is not checked but does not affect the logic.

The justification status of the last four epochs is stored in an array of bits in the state. After shifting the bits along by one at the outset of the routine, the justification status of the current epoch is stored in element 0, the previous in element 1, and so on.

Note that the total_active_balance is the current epoch's total balance, so it may not be strictly correct for calculating the supermajority for the previous epoch. However, the rate at which the validator set can change between epochs is tightly constrained, so this is not a significant issue.

Finalisation

The version of Casper FFG described in the Gasper paper uses k-finality, which extends the handling of finality in the original Casper FFG paper. See the k-finality section in the chapter on Consensus for more on how it interacts with the safety guarantees of Casper FFG.

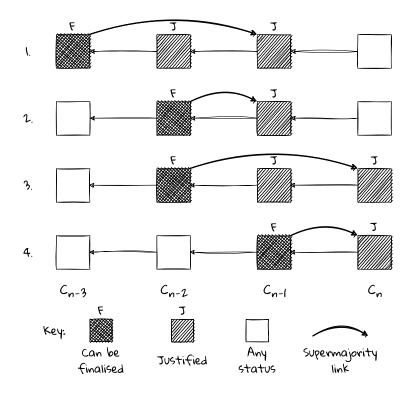
In k-finality, if we have a consecutive set of k justified checkpoints C_j, \dots, C_{j+k-1} , and a supermajority link from C_j to C_{j+k} , then C_j is finalised. Also note that this justifies C_{j+k} , by the rules above.

The Casper FFG version of this is 1-finality. So, a supermajority link from a justified checkpoint C_n to the very next checkpoint C_{n+1} both justifies C_{n+1} and finalises C_n .

On the beacon chain we are using 2-finality, since target votes may be included up to an epoch late. In 2-finality, we keep records of checkpoint justification status for four epochs and have the following conditions for finalisation, where the checkpoint for the current epoch is C_n . Note that we have already updated the justification status of C_n and C_{n-1} in this routine, which implies the existence of supermajority links pointing to them if the corresponding bits are set, respectively.

1. Checkpoints C_{n-3} and C_{n-2} are justified, and there is a supermajority link from C_{n-3} to C_{n-1} : finalise C_{n-3} .

- 2. Checkpoint C_{n-2} is justified, and there is a supermajority link from C_{n-2} to C_{n-1} : finalise C_{n-2} . This is equivalent to 1-finality applied to the previous epoch.
- 3. Checkpoints C_{n-2} and C_{n-1} are justified, and there is a supermajority link from C_{n-2} to C_n : finalise C_{n-2} .
- 4. Checkpoint C_{n-1} is justified, and there is a supermajority link from C_{n-1} to C_n : finalise C_{n-1} . This is equivalent to 1-finality applied to the current epoch.



The four cases of 2-finality. In each case the supermajority link causes the checkpoint at its start (the source) to become finalised and the checkpoint at its end (the target) to become justified. Checkpoint numbers are along the bottom.

Almost always we would expect to see only the 1-finality cases, in particular, case 4. The 2-finality cases would occur only in situations where many attestations are delayed, or when we are very close to the 2/3rds participation threshold. Note that these evaluations stack, so it is possible for rule 2 to finalise C_{n-2} and then for rule 4 to immediately finalise C_{n-1} , for example.

For the uninitiated, in Python's array slice syntax, bits[1:4] means bits 1, 2, and 3 (but not 4). This always trips me up.

Used by process_justification_and_finalization()
Uses get_block_root()
See also JUSTIFICATION_BITS_LENGTH, Checkpoint

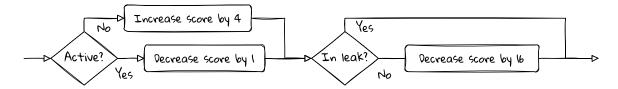
Inactivity scores

```
def process_inactivity_updates(state: BeaconState) -> None:
    # Skip the genesis epoch as score updates are based on the previous epoch participation
    if get_current_epoch(state) == GENESIS_EPOCH:
        return

for index in get_eligible_validator_indices(state):
        # Increase the inactivity score of inactive validators
```

Since the Altair upgrade, each validator has an individual inactivity score in the beacon state which is updated as follows.

- At the end of epoch N, irrespective of the inactivity leak,
 - decrease the score by one when the validator made a correct and timely target vote during epoch N-1, and
 - increase the score by INACTIVITY_SCORE_BIAS otherwise. Note that get_eligible_validator_ indices() includes slashed but not yet withdrawable validators: slashed validators are treated as not participating, whatever they actually do.
- When not in an inactivity leak
 - decrease all validators' scores by INACTIVITY_SCORE_RECOVERY_RATE.



How each validator's inactivity score is updated. The happy flow is right through the middle. "Active", when updating the scores at the end of epoch N, means having made a correct and timely target vote in epoch N-1.

There is a floor of zero on the score. So, outside a leak, validators' scores will rapidly return to zero and stay there, since INACTIVITY_SCORE_RECOVERY_RATE is greater than INACTIVITY_SCORE_BIAS.

Used by	<pre>process_epoch()</pre>
Uses	<pre>get_eligible_validator_indices(), get_unslashed_participating_indices(), is_in_inactivity_leak()</pre>
See also	INACTIVITY_SCORE_BIAS, INACTIVITY_SCORE_RECOVERY_RATE, INACTIVITY_SCORE_RECOVERY_RATE

Reward and penalty calculations

Without wanting to go full Yellow Paper on you, I am going to adopt a little notation to help analyse the rewards.

We will define a base reward B that we will see turns out to be the expected long-run average income of an optimally performing validator per epoch (ignoring validator set size changes). The total number of active validators is N.

The base reward is calculated from a base reward per increment, b. An "increment" is a unit of effective balance in terms of Effective_balance_increment. B=32b because MAX_EFFECTIVE_BALANCE = 32 * EFFECTIVE_BALANCE_INCREMENT

Other quantities we will use in rewards calculation are the incentivization weights: W_s , W_t , W_h , and W_y being the weights for correct source, target, head, and sync committee votes respectively; W_p being the proposer weight; and the weight denominator W_{Σ} which is the sum of the weights.

Issuance for regular rewards happens in four ways:

- I_A is the maximum total reward for all validators attesting in an epoch;
- $I_{A_{R}}$ is the maximum reward issued to proposers in an epoch for including attestations;
- I_S is the maximum total reward for all sync committee participants in an epoch; and
- I_{S_R} is the maximum reward issued to proposers in an epoch for including sync aggregates;

Under $get_flag_index_deltas()$, process_attestation(), and process_sync_aggregate() we find that these work out as follows in terms of B and N:

$$\begin{split} I_A &= \frac{W_s + W_t + W_h}{W_\Sigma} NB \\ I_{A_P} &= \frac{W_p}{W_\Sigma - W_p} I_A \\ I_S &= \frac{W_y}{W_\Sigma} NB \\ I_{S_P} &= \frac{W_p}{W_\Sigma - W_p} I_S \end{split}$$

To find the total optimal issuance per epoch, we can first sum I_A and I_S ,

$$I_A + I_S = \frac{W_s + W_t + W_h + W_y}{W_{\Sigma}} NB = \frac{W_{\Sigma} - W_p}{W_{\Sigma}} NB$$

Now adding in the proposer rewards,

$$I_{A} + I_{S} + I_{A_{P}} + I_{S_{P}} = \frac{W_{\Sigma} - W_{p}}{W_{\Sigma}} (1 + \frac{W_{p}}{W_{\Sigma} - W_{p}}) NB = (\frac{W_{\Sigma} - W_{p}}{W_{\Sigma}} + \frac{W_{p}}{W_{\Sigma}}) NB = NB$$

So, we see that every epoch, NB Gwei is awarded to N validators. Every validator participates in attesting, and proposing and sync committee duties are uniformly random, so the long-term expected income per optimally performing validator per epoch is B Gwei.

Helpers

The base reward per increment is the fundamental unit of reward in terms of which all other regular rewards and penalties are calculated. We will denote the base reward per increment, b.

As I noted under BASE_REWARD_FACTOR, this is the big knob to turn if we wish to increase or decrease the total reward for participating in Eth2, otherwise known as the issuance rate of new Ether.

An increment is a single unit of a validator's effective balance, denominated in terms of Effective_Balance, and maximally effective validator has 32 increments.

The base reward per increment is inversely proportional to the square root of the total balance of all active validators. This means that, as the number N of validators increases, the reward per validator decreases as $\frac{1}{\sqrt{N}}$, and the overall issuance per epoch increases as \sqrt{N} .

The decrease with increasing N in per-validator rewards provides a price discovery mechanism: the idea is that an equilibrium will be found where the total number of validators results in a reward similar to returns available elsewhere for similar risk. A different curve could have been chosen for the rewards profile. For example, the inverse of total balance rather than its square root would keep total issuance constant. The section on Issuance has a deeper exploration of these topics.

```
Used by get_base_reward(), process_sync_aggregate()
Uses integer_squareroot(), get_total_active_balance()
```

```
def get_base_reward(state: BeaconState, index: ValidatorIndex) -> Gwei:
    """
    Return the base reward for the validator defined by ``index`` with respect to the current ``state``.
    """
    increments = state.validators[index].effective_balance // EFFECTIVE_BALANCE_INCREMENT
    return Gwei(increments * get_base_reward_per_increment(state))
```

The base reward is the reward that an optimally performing validator can expect to earn on average per epoch, over the long term. It is proportional to the validator's effective balance; a validator with MAX_EFFECTIVE_BALANCE can expect to receive the full base reward B=32b per epoch on a long-term average.

```
Used by get_flag_index_deltas(), process_attestation()
Uses get_base_reward_per_increment()
See also EFFECTIVE_BALANCE_INCREMENT
```

```
def get_finality_delay(state: BeaconState) -> uint64:
    return get_previous_epoch(state) - state.finalized_checkpoint.epoch
```

Returns the number of epochs since the last finalised checkpoint (minus one). In ideal running this ought to be zero: during epoch processing we aim to have justified the checkpoint in the current epoch and finalised the checkpoint in the previous epoch. A delay in finalisation suggests a chain split or a large fraction of validators going offline.

```
Used by is_in_inactivity_leak()
```

```
def is_in_inactivity_leak(state: BeaconState) -> bool:
    return get_finality_delay(state) > MIN_EPOCHS_TO_INACTIVITY_PENALTY
```

If the beacon chain has not managed to finalise a checkpoint for MIN_EPOCHS_TO_INACTIVITY_PENALTY epochs (that is, four epochs), then the chain enters the inactivity leak. In this mode, penalties for non-participation are heavily increased, with the goal of reducing the proportion of stake controlled by non-participants, and eventually regaining finality.

```
Used by get_flag_index_deltas(), process_inactivity_updates()
Uses get_finality_delay()
See also inactivity leak, MIN_EPOCHS_TO_INACTIVITY_PENALTY
```

These are the validators that were subject to rewards and penalties in the previous epoch.

The list differs from the active validator set returned by <code>get_active_validator_indices()</code> by including slashed but not fully exited validators in addition to the ones marked active. Slashed validators are subject to penalties right up to when they become withdrawable and are thus fully exited.

```
Used by get_flag_index_deltas(), process_inactivity_updates(), get_inactivity_penalty_deltas()

Uses is_active_validator()
```

Inactivity penalty deltas

Validators receive penalties proportional to their individual inactivity scores, even when the beacon chain is not in an inactivity leak. However, these scores reduce to zero fairly rapidly outside a leak. This is a change from Phase 0 in which inactivity penalties were applied only during leaks.

All unslashed validators that made a correct and timely target vote in the previous epoch are identified by get_unslashed_participating_indices(), and all other active validators receive a penalty, including slashed validators.

The penalty is proportional to the validator's effective balance and its inactivity score. See INACTIVITY_PENALTY_QUOTIENT_BELLATRIX for more details of the calculation, and INACTIVITY_SCORE_RECOVERY_RATE for some charts of how the penalties accrue.

The returned rewards array always contains only zeros. It's here just to make the Python syntax simpler in the calling routine.

Process rewards and penalties

This is where validators are rewarded and penalised according to their attestation records.

Attestations included in beacon blocks were processed by process_attestation as blocks were received, and flags were set in the beacon state according to their timeliness and correctness. These flags are now processed into rewards and penalties for each validator by calling get_flag_index_deltas() for each of the flag types.

Once the normal attestation rewards and penalties have been calculated, additional penalties based on validators' inactivity scores are accumulated.

As noted elsewhere, rewards and penalties are handled separately from each other since we don't do negative numbers.

For reference, the only other places where rewards and penalties are applied are as follows:

- during block processing: for sync committee participation, when applying the proposer reward, and when applying initial slashing rewards and penalties.
- during epoch processing: when applying extended slashing penalties.

Registry updates

```
def process_registry_updates(state: BeaconState) -> None:
   # Process activation eligibility and ejections
   for index, validator in enumerate(state.validators):
       if is_eligible_for_activation_queue(validator):
           validator.activation_eligibility_epoch = get_current_epoch(state) + 1
           is active validator(validator, get current epoch(state))
           and validator.effective balance <= EJECTION BALANCE
           initiate_validator_exit(state, ValidatorIndex(index))
   # Queue validators eligible for activation and not yet dequeued for activation
   activation_queue = sorted([
       index for index, validator in enumerate(state.validators)
       if is_eligible_for_activation(state, validator)
       # Order by the sequence of activation eligibility epoch setting and then index
   ], key=lambda index: (state.validators[index].activation eligibility epoch, index))
   # Dequeued validators for activation up to churn limit
   for index in activation queue[:get validator churn limit(state)]:
        validator = state.validators[index]
        validator.activation_epoch = compute_activation_exit_epoch(get_current_epoch(state))
```

The Registry is the part of the beacon state that stores Validator records. These particular updates are, for the most part, concerned with moving validators through the activation queue.

is_eligible_for_activation_queue() finds validators that have a sufficient deposit amount yet their activation_eligibility_epoch is still set to FAR_FUTURE_EPOCH. These will be at most the validators for which deposits were processed during the last epoch, potentially up to MAX_DEPOSITS * SLOTS_PER_EPOCH, which is 512 (minus any partial deposits that don't yet add up to a whole deposit). These have their activation_eligibility_epoch set to the next epoch. They will become eligible for activation once that epoch is finalised — "eligible for activation" means only that they can be added to the activation queue; they will not become active until they reach the end of the queue.

Next, any validators whose effective balance has fallen to EJECTION_BALANCE have their exit initiated.

is_eligible_for_activation() selects validators whose activation_eligibility_epoch has just been finalised. The list of these is ordered by eligibility epoch, and then by index. There might be multiple eligibility epochs in the list if finalisation got delayed for some reason.

Finally, the first get_validator_churn_limit() validators in the list get their activation epochs set to compute_activation_exit_epoch().

On first sight, you'd think that the activation epochs of the whole queue could be set here, rather than just a single epoch's worth. But at some point, <code>get_validator_churn_limit()</code> will change unpredictably (we don't know when validators will exit), which makes that infeasible. Though, curiously, that is exactly what <code>initiate_validator_exit()</code> does. Anyway, clients could optimise this by persisting the sorted activation queue rather than recalculating it.

```
Used by process_epoch()

Uses is_eligible_for_activation_queue(), is_active_validator(), initiate_validator_exit(), is_eligible_for_activation(), get_validator_churn_limit(), compute_activation_exit_epoch()

See also Validator, EJECTION_BALANCE
```

Slashings

Slashing penalties are applied in two stages: the first stage is in slash_validator(), immediately on detection; the second stage is here.

In slash_validator() the withdrawable epoch is set EPOCHS_PER_SLASHINGS_VECTOR in the future, so in this function we are considering all slashed validators that are halfway to being withdrawable, that is, completely exited from the protocol. Equivalently, they were slashed EPOCHS_PER_SLASHINGS_VECTOR // 2 epochs ago (about 18 days).

To calculate the additional slashing penalty, we do the following:

- 1. Find the sum of the effective balances (at the time of the slashing) of all validators that were slashed in the previous EPOCHS_PER_SLASHINGS_VECTOR epochs (36 days). These are stored as a vector in the state.
- 2. Multiply this sum by PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX, but cap the result at total_balance, the total active balance of all validators.
- 3. For each slashed validator being considered, multiply its effective balance by the result of #2 and then divide by the total_balance. This results in an amount between zero and the full effective balance of the validator. That amount is subtracted from its actual balance as the penalty. Note that the effective balance could exceed the actual balance in odd corner cases, but decrease_balance() ensures the balance does not go negative.

If only a single validator were slashed within the 36 days, then this secondary penalty is tiny (actually zero, see below). If one-third of validators are slashed (the minimum required to finalise conflicting

blocks), then, with PROPORTIONAL_SLASHING_MULTIPLIER_BELLATRIX set to three, a successful chain attack will result in the attackers losing their entire effective balances.

Interestingly, due to the way the integer arithmetic is constructed in this routine, in particular the factoring out of increment, the result of this calculation will be zero if validator.effective_balance * adjusted_total_slashing_balance is less than total_balance. Effectively, the penalty is rounded down to the nearest whole amount of Ether. Issues 1322 and 2161 discuss this. In the end, the consequence is that when there are few slashings there is no extra correlated slashing penalty at all, which is probably a good thing.

Eth1 data votes updates

```
def process_eth1_data_reset(state: BeaconState) -> None:
    next_epoch = Epoch(get_current_epoch(state) + 1)
    # Reset eth1 data votes
    if next_epoch % EPOCHS_PER_ETH1_VOTING_PERIOD == 0:
        state.eth1_data_votes = []
```

There is a fixed period during which beacon block proposers vote on their view of the Eth1 deposit contract and try to come to a simple majority agreement. At the end of the period, the record of votes is cleared and voting begins again, whether or not agreement was reached during the period.

```
Used by process_epoch()
See also EPOCHS_PER_ETH1_VOTING_PERIOD, Eth1Data
```

Effective balances updates

Each validator's balance is represented twice in the state: once accurately in a list separate from validator records, and once in a coarse-grained format within the validator's record. Only effective balances are used in calculations within the spec, but rewards and penalties are applied to actual balances. This routine is where effective balances are updated once per epoch to follow the actual balances.

A hysteresis mechanism is used when calculating the effective balance of a validator when its actual balance changes. See Hysteresis Parameters for more discussion of this, and the values of the related constants. With the current values, a validator's effective balance drops to X ETH when its actual balance drops below X.75 ETH, and increases to Y ETH when its actual balance rises above Y.25 ETH. The hysteresis mechanism ensures that effective balances change infrequently, which means that the list of validator records needs to be re-hashed only infrequently when calculating the state root, saving considerably on work.

```
Used by process_epoch()
See also Hysteresis Parameters
```

Slashings balances updates

```
def process_slashings_reset(state: BeaconState) -> None:
    next_epoch = Epoch(get_current_epoch(state) + 1)
# Reset slashings
state.slashings[next_epoch % EPOCHS_PER_SLASHINGS_VECTOR] = Gwei(0)
```

state.slashings is a circular list of length EPOCHS_PER_SLASHINGS_VECTOR that contains the total of the effective balances of all validators that have been slashed at each epoch. These are used to apply a correlated slashing penalty to slashed validators before they are exited. Each epoch we overwrite the oldest entry with zero, and it becomes the current entry.

```
Used by process_epoch()
See also process_slashings(), EPOCHS_PER_SLASHINGS_VECTOR
```

Randao mixes updates

```
def process_randao_mixes_reset(state: BeaconState) -> None:
    current_epoch = get_current_epoch(state)
    next_epoch = Epoch(current_epoch + 1)
# Set randao mix
    state.randao mixes[next epoch % EPOCHS PER HISTORICAL VECTOR] = get randao mix(state, current epoch)
```

 $\label{thm:condomixes} state.randao_mixes is a circular list of length EPOCHS_PER_HISTORICAL_VECTOR. The current value of the RANDAO, which is updated with every block that arrives, is stored at position state.randao_mixes[current_epoch % EPOCHS_PER_HISTORICAL_VECTOR], as per get_randao_mix().$

At the end of every epoch, final value of the RANDAO for this epoch is copied over to become the starting value of the randao for the next, preserving the remaining entries as historical values.

```
Used by process_epoch()
Uses get_randao_mix()
See also process_randao(), EPOCHS_PER_HISTORICAL_VECTOR
```

Historical summaries updates

```
def process_historical_summaries_update(state: BeaconState) -> None:
    # Set historical block root accumulator.
    next_epoch = Epoch(get_current_epoch(state) + 1)
    if next_epoch % (SLOTS_PER_HISTORICAL_ROOT // SLOTS_PER_EPOCH) == 0:
        historical_summary = HistoricalSummary(
            block_summary_root=hash_tree_root(state.block_roots),
            state_summary_root=hash_tree_root(state.state_roots),
    )
    state.historical_summaries.append(historical_summary)
```

This routine replaced process_historical_roots_update() at the Capella upgrade.

Previously, both the state.block_roots and state.state_roots lists were Merkleized together into a single root before being added to the state.historical_roots double batched accumulator. Now they are separately Merkleized and appended to state.historical_summaries via the HistoricalSummary container. The Capella upgrade changed this to make it possible to validate past block history without having to know the state history.

The summary is appended to the list every SLOTS_PER_HISTORICAL_ROOT slots. At 64 bytes per summary, the list will grow at the rate of 20 KB per year. The corresponding block and state root lists in the beacon state are circular and just get overwritten in the next period.

The process_historical_roots_update() function that this replaces remains documented in the Bellatrix edition.

```
Used by process_epoch()
See also HistoricalSummary, SLOTS_PER_HISTORICAL_ROOT
```

Participation flags updates

Two epochs' worth of validator participation flags (that record validators' attestation activity) are stored. At the end of every epoch the current becomes the previous, and a new empty list becomes current.

```
Used by process_epoch()
See also ParticipationFlags
```

Sync committee updates

```
def process_sync_committee_updates(state: BeaconState) -> None:
    next_epoch = get_current_epoch(state) + Epoch(1)
    if next_epoch % EPOCHS_PER_SYNC_COMMITTEE_PERIOD == 0:
        state.current_sync_committee = state.next_sync_committee
        state.next_sync_committee = get_next_sync_committee(state)
```

Sync committees are rotated every EPOCHS_PER_SYNC_COMMITTEE_PERIOD. The next sync committee is ready and waiting so that validators can prepare in advance by subscribing to the necessary subnets. That becomes the current sync committee, and the next is calculated.

```
Used by process_epoch()
Uses get_next_sync_committee()
See also EPOCHS_PER_SYNC_COMMITTEE_PERIOD
```

Block processing

These are the tasks that the beacon node performs in order to process a block and update the state. If any of the called functions triggers the failure of an assert statement, or any other kind of exception, then the entire block is invalid, and any state changes must be rolled back.

Note: The call to the process_execution_payload must happen before the call to the process_randao as the former depends on the randao_mix computed with the reveal of the previous block.

The call to process_execution_payload() was added in the Bellatrix pre-Merge upgrade. The EXECUTION_ENGINE object is not really defined in the beacon chain spec, but corresponds to an API that calls out to an attached execution client (formerly Eth1 client) that will do most of the payload validation.

process_operations() covers the processing of any slashing reports (proposer and attester) in the block, any attestations, any deposits, and any voluntary exits.

```
Used by state_transition()
Uses process_block_header(), is_execution_enabled(), process_execution_payload(), process_randao(), process_ethl_data(), process_operations(), process_sync_aggregate()
```

Block header

```
def process_block_header(state: BeaconState, block: BeaconBlock) -> None:
   # Verify that the slots match
   assert block.slot == state.slot
   # Verify that the block is newer than latest block header
   assert block.slot > state.latest_block_header.slot
   # Verify that proposer index is the correct index
   assert block.proposer_index == get_beacon_proposer_index(state)
   # Verify that the parent matches
   assert block.parent root == hash tree root(state.latest block header)
   # Cache current block as the new latest block
   state.latest_block_header = BeaconBlockHeader(
       slot=block.slot.
       proposer_index=block.proposer_index,
       parent_root=block.parent_root,
       state_root=Bytes32(), # Overwritten in the next process_slot call
       body_root=hash_tree_root(block.body),
   )
   # Verify proposer is not slashed
   proposer = state.validators[block.proposer_index]
   assert not proposer.slashed
```

A straightforward set of validity conditions for the block header data.

The version of the block header object that this routine stores in the state is a duplicate of the incoming block's header, but with its state_root set to its default empty Bytes32() value. See process_slot() for the explanation of this.

```
Used by process_block()
Uses get_beacon_proposer_index(), hash_tree_root()
See also BeaconBlockHeader, process_slot()
```

Withdrawals

get expected withdrawals

```
def get_expected_withdrawals(state: BeaconState) -> Sequence[Withdrawal]:
    epoch = get_current_epoch(state)
    withdrawal_index = state.next_withdrawal_index
    validator_index = state.next_withdrawal_validator_index
    withdrawals: List[Withdrawal] = []
    bound = min(len(state.validators), MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP)
    for _ in range(bound):
```

```
validator = state.validators[validator_index]
   balance = state.balances[validator_index]
   if is fully withdrawable validator(validator, balance, epoch):
       withdrawals.append(Withdrawal(
           index=withdrawal_index,
            validator_index=validator_index,
           address=ExecutionAddress(validator.withdrawal_credentials[12:]),
           amount=balance,
       ))
       withdrawal_index += WithdrawalIndex(1)
   elif is_partially_withdrawable_validator(validator, balance):
       withdrawals.append(Withdrawal(
           index=withdrawal index,
           validator index=validator index,
            address=ExecutionAddress(validator.withdrawal_credentials[12:]),
            amount=balance - MAX_EFFECTIVE_BALANCE,
       ))
       withdrawal_index += WithdrawalIndex(1)
   if len(withdrawals) == MAX_WITHDRAWALS_PER_PAYLOAD:
   validator_index = ValidatorIndex((validator_index + 1) % len(state.validators))
return withdrawals
```

This is used in both block processing and block building to construct the list of automatic validator withdrawals that we expect to see in the block.

At most MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP validators will be considered for a withdrawal. As described under that heading, this serves to bound the load on nodes when eligible validators are few and far between.

Picking up where the previous sweep left off (state.next_withdrawal_validator_index), we consider validators in turn, in increasing order of their validator indices. If a validator is eligible for a full withdrawal transaction for its entire balance is added to the list. If a validator is eligible for a partial_withdrawal then a withdrawal transaction for its excess balance above MAX_EFFECTIVE BALANCE is added to the list.

Each withdrawal transaction is associated with a unique, consecutive withdrawal index, which is the total number of previous withdrawals.

Once either MAX_WITHDRAWALS_PER_PAYLOAD transactions have been assembled, or MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP have been considered, the sweep terminates and returns the list of transactions.

The next_withdrawal_index and next_withdrawal_validator_index counters in the beacon state are not updated here, but in the calling function.

```
Used by process_withdrawals()
Uses is_fully_withdrawable_validator(), is_partially_withdrawable_validator()
See also MAX_WITHDRAWALS_PER_PAYLOAD, MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP, Withdrawal
```

process_withdrawals

```
def process_withdrawals(state: BeaconState, payload: ExecutionPayload) -> None:
    expected_withdrawals = get_expected_withdrawals(state)
    assert len(payload.withdrawals) == len(expected_withdrawals)

for expected_withdrawal, withdrawal in zip(expected_withdrawals, payload.withdrawals):
    assert withdrawal == expected_withdrawal
    decrease_balance(state, withdrawal.validator_index, withdrawal.amount)

# Update the next withdrawal index if this block contained withdrawals
    if len(expected_withdrawals) != 0:
        latest_withdrawal = expected_withdrawals[-1]
```

The withdrawal transactions in a block appear in its ExecutionPayload since they span both the consensus and execution layers. When processing the withdrawals, we first check that they match what we expect to see. This is taken care of by the call to get_expected_withdrawals() and the pairwise comparison within the for loop¹⁰⁹. If any of the assert tests fails then the entire block is invalid and all changes, including balance updates already made, must be rolled back. For each withdrawal, the corresponding validator's balance is decreased; the execution client will add the same amount to the validator's Eth1 withdrawal address on the execution layer.

After that we have some trickery for updating the values of next_withdrawal_index and next_withdrawal_validator_index in the beacon state.

For next_withdrawal_index, which just counts the number of withdrawals every made, we take the index of the last withdrawal in our list and add one. Adding the length of the list to our current value would be equivalent.

For next_withdrawal_validator_index, we have two cases. If we have a full list of MAX_WITHDRAWALS_PER_PAYLOAD withdrawal transactions then we know that this is the condition that terminated the sweep. Therefore the first validator we need to consider next time is the one after the validator in the last withdrawal transaction. Otherwise, the sweep was terminated by reaching MAX_VALIDATORS_PER_WITHDRAWALS SWEEP, and the first validator we need to consider next time is the one after that.

I can't help thinking that it would have been easier to return these both from get_expected_withdrawals(), where they have just been calculated independently.

```
Used by process_block()
Uses get_expected_withdrawals(), decrease_balance()
See also WithdrawalIndex, ValidatorIndex, MAX_WITHDRAWALS_PER_PAYLOAD,
MAX_VALIDATORS_PER_WITHDRAWALS_SWEEP
```

Execution payload

process_execution_payload

¹⁰⁹The use of zip() here is quite Pythonic, but just means that with two lists of equal length we take their elements pairwise in turn.

```
# Cache execution payload header
state.latest execution payload header = ExecutionPayloadHeader(
    parent hash=payload.parent hash,
    fee_recipient=payload.fee_recipient,
    state_root=payload.state_root,
    receipts_root=payload.receipts_root,
    logs_bloom=payload.logs_bloom,
    prev_randao=payload.prev_randao,
    block_number=payload.block_number,
    gas_limit=payload.gas_limit,
    gas_used=payload.gas_used,
    timestamp=payload.timestamp,
    extra data=payload.extra data,
    base_fee_per_gas=payload.base_fee_per_gas,
    block_hash=payload.block_hash,
    transactions_root=hash_tree_root(payload.transactions),
    withdrawals_root=hash_tree_root(payload.withdrawals), # [New in Capella]
)
```

Since the Merge, the execution payload (formerly an Eth1 block) now forms part of the beacon block.

There isn't much beacon chain processing to be done for execution payloads as they are for the most part opaque blobs of data that are meaningful only to the execution client. However, the beacon chain does need to know whether the execution payload is valid in the view of the execution client. An execution payload that is invalid by the rules of the execution (Eth1) chain makes the beacon block containing it invalid.

Some initial sanity checks are performed:

- Unless this is the very first execution payload that we have seen then its parent_hash must match the block_hash that we have in the beacon state, that of the last execution payload we processed. This ensures that the chain of execution payloads is continuous, since it is essentially a blockchain within a blockchain.
- We check that the prev_randao value is correctly set, otherwise a block proposer could trivially
 control the randomness on the execution layer.
- The timestamp on the execution payload must match the slot timestamp. Again, this prevents proposers manipulating the execution layer time for any smart contracts that depend on it.

Next we send the payload over to the execution engine via the Engine API, using the notify_new_payload() function it provides. This serves two purposes: first it requests that the execution client check the validity of the payload, and second, if the payload is valid, it allows the execution layer to update its own state by running the transactions contained in the payload.

Finally, the header of the execution payload is stored in the beacon state, primarily so that the block_hash-parent_hash check can be made next time this function is called. The remainder of the execution header data is not currently used in the beacon chain specification, despite being stored.

This function was added in the Bellatrix pre-Merge upgrade.

RANDAO

```
def process_randao(state: BeaconState, body: BeaconBlockBody) -> None:
    epoch = get_current_epoch(state)
    # Verify RANDAO reveal
    proposer = state.validators[get_beacon_proposer_index(state)]
    signing_root = compute_signing_root(epoch, get_domain(state, DOMAIN_RANDAO))
```

```
assert bls.Verify(proposer.pubkey, signing_root, body.randao_reveal)
# Mix in RANDAO reveal
mix = xor(get_randao_mix(state, epoch), hash(body.randao_reveal))
state.randao_mixes[epoch % EPOCHS_PER_HISTORICAL_VECTOR] = mix
```

A good source of randomness is foundational to the operation of the beacon chain. Security of the protocol depends significantly on being able to unpredictably and uniformly select block proposers and committee members. In fact, the very name "beacon chain" was inspired by Dfinity's concept of a randomness beacon.

The current mechanism for providing randomness is a RANDAO, in which each block proposer provides some randomness and all the contributions are mixed together over the course of an epoch. This is not unbiasable (a malicious proposer may choose to skip a block if it is to its advantage to do so), but is good enough. In future, Ethereum might use a verifiable delay function (VDF) to provide unbiasable randomness.

Early designs had the validators pre-committing to "hash onions", peeling off one layer of hashing at each block proposal. This was changed to using a BLS signature over the epoch number as the entropy source. Using signatures is both a simplification, and an enabler for multi-party (distributed) validators. The (reasonable) assumption is that sufficient numbers of validators generated their secret keys with good entropy to ensure that the RANDAO's entropy is adequate.

The process_randao() function simply uses the proposer's public key to verify that the RANDAO reveal in the block is indeed the epoch number signed with the proposer's private key. It then mixes the hash of the reveal into the current epoch's RANDAO accumulator. The hash is used in order to reduce the signature down from 96 to 32 bytes, and to make it uniform. EPOCHS_PER_HISTORICAL_VECTOR past values of the RANDAO accumulator at the ends of epochs are stored in the state.

From Justin Drake's notes: > Using xor in process_randao is (slightly) more secure than using hash. To illustrate why, imagine an attacker can grind randomness in the current epoch such that two of his validators are the last proposers, in a different order, in two resulting samplings of the next epochs. The commutativity of xor makes those two samplings equivalent, hence reducing the attacker's grinding opportunity for the next epoch versus hash (which is not commutative). The strict security improvement may simplify the derivation of RANDAO security formal lower bounds.

Note that the assert statement means that the whole block is invalid if the RANDAO reveal is incorrectly formed.

Eth1 data

```
def process_eth1_data(state: BeaconState, body: BeaconBlockBody) -> None:
    state.eth1_data_votes.append(body.eth1_data)
    if state.eth1_data_votes.count(body.eth1_data) * 2 > EPOCHS_PER_ETH1_VOTING_PERIOD * SLOTS_PER_EPOCH:
        state.eth1_data = body.eth1_data
```

Blocks may contain Eth1Data which is supposed to be the proposer's best view of the Eth1 chain and the deposit contract at the time. There is no incentive to get this data correct, or penalty for it being incorrect.

If there is a simple majority of the same vote being cast by proposers during each voting period of EPOCHS_PER_ETH1_VOTING_PERIOD epochs (6.8 hours) then the Eth1 data is committed to the beacon state. This updates the chain's view of the deposit contract, and new deposits since the last update will start being processed.

This mechanism has proved to be fragile in the past, but appears to be workable if not perfect.

Used by	process_block()
See also	Eth1Data, EPOCHS_PER_ETH1_VOTING_PERIOD

Operations

Just a dispatcher for handling the various optional contents in a block.

Deposits are optional only in the sense that some blocks have them and some don't. However, as per the assert statement, if, according to the beacon chain's view of the Eth1 chain, there are deposits pending, then the block *must* include them, otherwise the block is invalid.

Regarding incentives for block proposers to include each of these elements:

- Proposers are explicitly rewarded for including any available attestations and slashing reports.
- There is a validity condition, and thus an implicit reward, related to including deposit messages.
- The incentive for including voluntary exits is that a smaller validator set means higher rewards for the remaining validators.
- There is no incentive, implicit or explicit, for including BLS withdrawal credential change messages. These are handled on a purely altruistic basis.

Proposer slashings

```
def process_proposer_slashing(state: BeaconState, proposer_slashing: ProposerSlashing) -> None:
    header_1 = proposer_slashing.signed_header_1.message
    header_2 = proposer_slashing.signed_header_2.message

# Verify header slots match
    assert header_1.slot == header_2.slot
    # Verify header proposer indices match
    assert header_1.proposer_index == header_2.proposer_index
# Verify the headers are different
    assert header_1 != header_2
# Verify the proposer is slashable
    proposer = state.validators[header_1.proposer_index]
    assert is_slashable_validator(proposer, get_current_epoch(state))
# Verify signatures
for signed_header in (proposer_slashing.signed_header_1, proposer_slashing.signed_header_2):
```

A ProposerSlashing is a proof that a proposer has signed two blocks at the same height. Up to MAX_PROPOSER_SLASHINGS of them may be included in a block. It contains the evidence in the form of a pair of SignedBeaconBlockHeaders.

The proof is simple: the two proposals come from the same slot, have the same proposer, but differ in one or more of parent_root, state_root, or body_root. In addition, they were both signed by the proposer. The conflicting blocks do not need to be valid: any pair of headers that meet the criteria, irrespective of the blocks' contents, are liable to be slashed.

As ever, the assert statements ensure that the containing block is invalid if it contains any invalid slashing claims.

Fun fact: the first slashing to occur on the beacon chain was a proposer slashing. Two clients running side-by-side with the same keys will often produce the same attestations since the protocol is designed to encourage that. Independently producing the same block is very unlikely as blocks contain much more data.

Attester slashings

```
def process_attester_slashing(state: BeaconState, attester_slashing: AttesterSlashing) -> None:
    attestation_1 = attester_slashing.attestation_1
    attestation_2 = attester_slashing.attestation_2
    assert is_slashable_attestation_data(attestation_1.data, attestation_2.data)
    assert is_valid_indexed_attestation(state, attestation_1)
    assert is_valid_indexed_attestation(state, attestation_2)

slashed_any = False
    indices = set(attestation_1.attesting_indices).intersection(attestation_2.attesting_indices)
    for index in sorted(indices):
        if is_slashable_validator(state.validators[index], get_current_epoch(state)):
            slash_validator(state, index)
            slashed_any = True
    assert slashed_any
```

AttesterSlashings are similar to proposer slashings in that they just provide the evidence of the two aggregate IndexedAttestations that conflict with each other. Up to MAX_ATTESTER_SLASHINGS of them may be included in a block.

The validity checking is done by is_slashable_attestation_data(), which checks the double vote and surround vote conditions, and by is_valid_indexed_attestation() which verifies the signatures on the attestations.

Any validators that appear in both attestations are slashed. If no validator is slashed, then the attester slashing claim was not valid after all, and therefore its containing block is invalid.

Examples: a double vote attester slashing; surround vote attester slashings.

```
Used by process_block()
```

```
Uses is_slashable_attestation_data(), is_valid_indexed_attestation(), is_slashable_validator() See also AttesterSlashing
```

Attestations

```
def process_attestation(state: BeaconState, attestation: Attestation) -> None:
    data = attestation.data
   assert data.target.epoch in (get previous epoch(state), get current epoch(state))
   assert data.target.epoch == compute_epoch_at_slot(data.slot)
   assert data.slot + MIN_ATTESTATION_INCLUSION_DELAY <= state.slot <= data.slot + SLOTS_PER_EPOCH
   assert data.index < get_committee_count_per_slot(state, data.target.epoch)</pre>
    committee = get_beacon_committee(state, data.slot, data.index)
   assert len(attestation.aggregation_bits) == len(committee)
   # Participation flag indices
   participation_flag_indices = get_attestation_participation_flag_indices(state, data, state.slot -
                                        → data.slot)
   # Verify signature
   assert is_valid_indexed_attestation(state, get_indexed_attestation(state, attestation))
   # Update epoch participation flags
    if data.target.epoch == get_current_epoch(state):
        epoch_participation = state.current_epoch_participation
    else:
        epoch_participation = state.previous_epoch_participation
   proposer_reward_numerator = 0
    for index in get_attesting_indices(state, data, attestation.aggregation_bits):
        for flag_index, weight in enumerate(PARTICIPATION_FLAG_WEIGHTS):
            if flag_index in participation_flag_indices and not has_flag(epoch_participation[index],
                                         \hookrightarrow flag_index):
                epoch_participation[index] = add_flag(epoch_participation[index], flag_index)
                proposer_reward_numerator += get_base_reward(state, index) * weight
   # Reward proposer
   proposer_reward_denominator = (WEIGHT_DENOMINATOR - PROPOSER_WEIGHT) * WEIGHT_DENOMINATOR //
                                         \hookrightarrow PROPOSER WEIGHT
   proposer_reward = Gwei(proposer_reward_numerator // proposer_reward_denominator)
    increase_balance(state, get_beacon_proposer_index(state), proposer_reward)
```

Block proposers are rewarded here for including attestations during block processing, while attesting validators receive their rewards and penalties during epoch processing.

This routine processes each attestation included in the block. First a bunch of validity checks are performed. If any of these fails, then the whole block is invalid (it is most likely from a proposer on a different fork, and so useless to us):

- The target vote of the attestation must be either the previous epoch's checkpoint or the current epoch's checkpoint.
- The target checkpoint and the attestation's slot must belong to the same epoch.
- The attestation must be no newer than MIN_ATTESTATION_INCLUSION_DELAY slots, which is one. So this condition rules out attestations from the current or future slots.
- The attestation must be no older than SLOTS_PER_EPOCH slots, which is $32.^{110}$

¹¹⁰This is due to change in EIP-7045, scheduled for inclusion in the Deneb upgrade. The change will allow attestations to be included from the whole of current and previous epochs.

- The attestation must come from a committee that existed when the attestation was created.
- The size of the committee and the size of the aggregate must match (aggregation bits).
- The (aggregate) signature on the attestation must be valid and must correspond to the aggregated public keys of the validators that it claims to be signed by. This (and other criteria) is checked by is_valid_indexed_attestation().

Once the attestation has passed the checks it is processed by converting the votes from validators that it contains into flags in the state.

It's easy to skip over amidst all the checking, but the actual attestation processing is done by get_attestation_participation_flag_indices(). This takes the source, target, and head votes of the attestation, along with its inclusion delay (how many slots late was it included in a block) and returns a list of up to three flags corresponding to the votes that were both correct and timely, in participation_flag_indices.

For each validator that signed the attestation, if each flag in participation_flag_indices is not already set for it in its epoch_participation record, then the flag is set, and the proposer is rewarded. Recall that the validator making the attestation is not rewarded until the end of the epoch. If the flag is already set in the corresponding epoch for a validator, no proposer reward is accumulated: the attestation for this validator was included in an earlier block.

The proposer reward is accumulated, and weighted according to the weight assigned to each of the flags (timely source, timely target, timely head).

If a proposer includes all the attestations only for one slot, and all the relevant validators vote, then its reward will be, in the notation established earlier,

$$I_{A_P} = \frac{W_p}{32(W_\Sigma - W_p)}I_A$$

Where I_A is the total maximum reward per epoch for attesters, calculated in get_flag_index_deltas(). The total available reward in an epoch for proposers including attestations is 32 times this.

Deposits

The code in this section handles deposit transactions that were included in a block. A deposit is created when a user transfers one or more ETH to the deposit contract. We need to check that the data sent with the deposit is valid. If it is, we either create a new validator record (for the first deposit for a validator) or update an existing record.

Create a newly initialised validator object based on deposit data. This was factored out of process_deposit() for better code reuse between the Phase 0 spec and the (now deprecated) sharding spec.

The pubkey is supplied in the initial deposit transaction. The depositor generates the validator's public key from the its private key.

```
Used by apply_deposit()
See also Validator, FAR_FUTURE_EPOCH, EFFECTIVE_BALANCE_INCREMENT, MAX_EFFECTIVE_BALANCE
```

```
def apply_deposit(state: BeaconState,
                  pubkey: BLSPubkey,
                  withdrawal_credentials: Bytes32,
                  amount: uint64,
                  signature: BLSSignature) -> None:
   validator_pubkeys = [validator.pubkey for validator in state.validators]
    if pubkey not in validator_pubkeys:
        # Verify the deposit signature (proof of possession) which is not checked by the deposit contract
        deposit message = DepositMessage(
            pubkey=pubkey,
            withdrawal_credentials=withdrawal_credentials,
            amount=amount,
        domain = compute_domain(DOMAIN_DEPOSIT) # Fork-agnostic domain since deposits are valid across
                                        \hookrightarrow forks
        signing_root = compute_signing_root(deposit_message, domain)
        # Initialize validator if the deposit signature is valid
        if bls.Verify(pubkey, signing_root, signature):
            state.validators.append(get_validator_from_deposit(pubkey, withdrawal_credentials, amount))
            state.balances.append(amount)
            # [New in Altair]
            state.previous_epoch_participation.append(ParticipationFlags(0b0000_0000))
            state.current_epoch_participation.append(ParticipationFlags(0b0000_0000))
            state.inactivity_scores.append(uint64(0))
    else:
        # Increase balance by deposit amount
        index = ValidatorIndex(validator_pubkeys.index(pubkey))
        increase_balance(state, index, amount)
```

The apply_deposit() function was factored out of process_deposit() in the Capella release for better code reuse between the Phase 0 spec and the EIP-6110 spec¹¹¹.

Deposits are signed with the private key of the depositing validator, and the corresponding public key is included in the deposit data. This constitutes a "proof of possession" of the private key, and prevents nastiness like the rogue key attack. Note that compute_domain() is used directly here when validating the deposit's signature, rather than the more usual get_domain() wrapper. This is because deposit messages are valid across beacon chain upgrades (such as Phase 0, Altair, and Bellatrix), so we don't want to mix the fork version into the domain. In addition, deposits can be made before genesis_validators_root is known

An interesting quirk of this routine is that only the first deposit for a validator needs to be signed. Subsequent deposits for the same public key do not have their signatures checked. This could allow one staker (the key holder) to make an initial deposit (1 ETH, say), and for that to be topped up by others who do not have the private key. I don't know of any practical uses for this feature, but would be glad to hear of any. It slightly reduces the risk for stakers making multiple deposits for the same validator as they don't need to worry about incorrectly signing any but the first deposit.

Similarly, once a validator's withdrawal credentials have been set by the initial deposit transaction, the withdrawal credentials of subsequent deposits for the same validator are ignored. Only the credentials

 $^{^{111}}$ EIP-6110 is a potential future upgrade that would allow deposits to be processed more or less instantly, rather than having to go through the Eth1 follow distance and Eth1 voting period as they do now.

appearing on the initial deposit are stored on the beacon chain. This is an important security measure. If an attacker steals a validator's signing key (which signs deposit transactions), we don't want them to be able to change the withdrawal credentials in order to steal the stake for themselves. However, it works both ways, and a vulnerability was identified for staking pools in which a malicious operator could potentially front-run a deposit transaction with a 1 ETH deposit to set the withdrawal credentials to their own.

Note that the withdrawal_credential in the deposit data is not checked in any way. It's up to the depositor to ensure that they are using the correct prefix and contents to be able to receive their rewards and retrieve their stake back after exiting the consensus layer.

```
def process_deposit(state: BeaconState, deposit: Deposit) -> None:
   # Verify the Merkle branch
    assert is_valid_merkle_branch(
        leaf=hash_tree_root(deposit.data),
        branch=deposit.proof,
        depth=DEPOSIT CONTRACT TREE DEPTH + 1, # Add 1 for the List length mix-in
        index=state.ethl deposit index,
        root=state.ethl_data.deposit_root,
    )
   # Deposits must be processed in order
   state.eth1_deposit_index += 1
   apply_deposit(
        state=state.
        pubkev=deposit.data.pubkev.
        withdrawal credentials=deposit.data.withdrawal credentials,
        amount=deposit.data.amount,
        signature=deposit.data.signature,
    )
```

Here, we process a deposit from a block. If the deposit is valid, either a new validator is created or the deposit amount is added to an existing validator.

The call to is_valid_merkle_branch() ensures that it is not possible to fake a deposit. The ethldata.deposit_root from the deposit contract has been agreed by the beacon chain and includes all pending deposits visible to the beacon chain. The deposit itself contains a Merkle proof that it is included in that root. The state.ethl_deposit_index counter ensures that deposits are processed in order. In short, the proposer provides leaf and branch, but neither index nor root.

If the Merkle branch check fails, then the whole block is invalid. However, individual deposits can fail the signature check without invalidating the block.

Deposits must be processed in order, and all available deposits must be included in the block (up to MAX_DEPOSITS - checked in process_operations()). This ensures that the beacon chain cannot censor deposit transactions, except at the expense of stopping block production entirely.

```
Used by process_operations()
Uses is_valid_merkle_branch(), hash_tree_root(), apply_deposit()
See also Deposit, DEPOSIT_CONTRACT_TREE_DEPTH
```

```
def process_voluntary_exit(state: BeaconState, signed_voluntary_exit: SignedVoluntaryExit) -> None:
   voluntary_exit = signed_voluntary_exit.message
   validator = state.validators[voluntary_exit.validator_index]
   # Verify the validator is active
   assert is_active_validator(validator, get_current_epoch(state))
   # Verify exit has not been initiated
   assert validator.exit_epoch == FAR_FUTURE_EPOCH
   # Exits must specify an epoch when they become valid; they are not valid before then
   assert get_current_epoch(state) >= voluntary_exit.epoch
   # Verify the validator has been active long enough
   assert get_current_epoch(state) >= validator.activation_epoch + SHARD_COMMITTEE_PERIOD
   # Verify signature
   domain = get domain(state, DOMAIN VOLUNTARY EXIT, voluntary exit.epoch)
   signing root = compute signing root(voluntary exit, domain)
   assert bls.Verify(validator.pubkey, signing_root, signed_voluntary_exit.signature)
   initiate_validator_exit(state, voluntary_exit.validator_index)
```

A voluntary exit message is submitted by a validator to indicate that it wishes to cease being an active validator. A proposer receives voluntary exit messages via gossip or via its own API and then includes the message in a block so that it can be processed by the network.

Most of the checks are straightforward, as per the comments in the code. Note the following.

- Voluntary exits are invalid if they are included in blocks before the given epoch, so nodes should buffer any future-dated exits they see before putting them in a block.
- A validator must have been active for at least SHARD_COMMITTEE_PERIOD epochs (27 hours). See there for the rationale.
- Voluntary exits are signed with the validator's usual signing key. There is some discussion about changing this to also allow signing of a voluntary exit with the validator's withdrawal key.

If the voluntary exit message is valid then the validator is added to the exit queue by calling initiate_validator_exit().

At present, it is not possible for a validator to exit and re-enter, but this functionality may be introduced in future.

process bls to execution change

```
validator.withdrawal_credentials = (
   ETH1_ADDRESS_WITHDRAWAL_PREFIX
   + b'\x00' * 11
   + address_change.to_execution_address
)
```

The Capella upgrade provides a one-time operation to allow stakers to change their withdrawal credentials from BLS type (BLS_WITHDRAWAL_PREFIX), which do not allow withdrawals, to Eth1 style (ETH1_ADDRESS_WITHDRAWAL_PREFIX), which enable automatic withdrawals.

Stakers can make the change by signing a BLSToExecutionChange message and broadcasting it to the network. At some point a proposer will include the change message in a block and it will arrive at this function in the state transition.

For BLS credentials the withdrawal credential contains the last 31 bytes of the SHA256 hash of a public key. That public key is the validator's withdrawal key, distinct from its signing key, although often derived from the same mnemonic. By checking its hash, we are confirming that the public key provided in the change message is the same one that created the withdrawal credential in the initial deposit.

Once we are satisfied that the public key is the same on previously committed to, then we can use it to verify the signature on the withdrawal transaction. Again, this transaction must be signed with the validator's withdrawal private key, not its usual signing key.

Having verified the signature, we can finally, and irrevocably, update the validator's withdrawal credentials from BLS style to Eth1 style.

```
Used by process_operations()
Uses compute_signing_root(), compute_domain(), bls.Verify()
See also BLS_WITHDRAWAL_PREFIX, BLSToExecutionChange
```

Sync aggregate processing

```
def process_sync_aggregate(state: BeaconState, sync_aggregate: SyncAggregate) -> None:
    # Verify sync committee aggregate signature signing over the previous slot block root
    committee_pubkeys = state.current_sync_committee.pubkeys
   participant_pubkeys = [pubkey for pubkey, bit in zip(committee_pubkeys,
                                          \hookrightarrow {\tt sync\_aggregate.sync\_committee\_bits)} \ {\tt if} \ {\tt bit]}
   previous_slot = max(state.slot, Slot(1)) - Slot(1)
   domain = get_domain(state, DOMAIN_SYNC_COMMITTEE, compute_epoch_at_slot(previous_slot))
   signing_root = compute_signing_root(get_block_root_at_slot(state, previous_slot), domain)
   assert eth_fast_aggregate_verify(participant_pubkeys, signing_root,

    ⇒ sync aggregate.sync committee signature)

   # Compute participant and proposer rewards
    total_active_increments = get_total_active_balance(state) // EFFECTIVE_BALANCE_INCREMENT
    total_base_rewards = Gwei(get_base_reward_per_increment(state) * total_active_increments)
   max_participant_rewards = Gwei(total_base_rewards * SYNC_REWARD_WEIGHT // WEIGHT_DENOMINATOR //
                                          \hookrightarrow SLOTS_PER_EPOCH)
    participant_reward = Gwei(max_participant_rewards // SYNC_COMMITTEE_SIZE)
   proposer_reward = Gwei(participant_reward * PROPOSER_WEIGHT // (WEIGHT_DENOMINATOR - PROPOSER WEIGHT))
   # Apply participant and proposer rewards
    all pubkeys = [v.pubkey for v in state.validators]
    committee_indices = [ValidatorIndex(all_pubkeys.index(pubkey)) for pubkey in
                                          \hookrightarrow state.current_sync_committee.pubkeys]
    for participant_index, participation_bit in zip(committee_indices,
                                          \hookrightarrow \verb| sync_aggregate.sync_committee_bits|):
        if participation_bit:
            increase_balance(state, participant_index, participant_reward)
            increase_balance(state, get_beacon_proposer_index(state), proposer_reward)
            decrease_balance(state, participant_index, participant_reward)
```

Similarly to how attestations are handled, the beacon block proposer includes in its block an aggregation of sync committee votes that agree with its local view of the chain. Specifically, the sync committee votes are for the head block that the proposer saw in the previous slot. (If the previous slot is empty, then the head block will be from an earlier slot.)

We validate these votes against our local view of the chain, and if they agree then we reward the participants that voted. If they do not agree with our local view, then the entire block is invalid: it is on another branch.

To perform the validation, we form the signing root of the block at the previous slot, with <code>DOMAIN_SYNC_COMMITTEE</code> mixed in. Then we check if the aggregate signature received in the <code>SyncAggregate</code> verifies against it, using the aggregate public key of the validators who claimed to have signed it. If either the signing root (that is, the head block) is wrong, or the list of participants is wrong, then the verification will fail and the block is invalid.

Like proposer rewards, but unlike attestation rewards, sync committee rewards are not weighted with the participants' effective balances. This is already taken care of by the committee selection process that weights the probability of selection with the effective balance of the validator.

Running through the calculations:

- total_active_increments: the sum of the effective balances of the entire active validator set normalised with the EFFECTIVE BALANCE INCREMENT to give the total number of increments.
- total_base_rewards: the maximum rewards that will be awarded to all validators for all duties this epoch. It is at most NB in the notation established earlier.
- max_participant_rewards: the amount of the total reward to be given to the entire sync committee in this slot.
- participant_reward: the reward per participating validator, and the penalty per non-participating validator.
- proposer_reward: one seventh of the participant reward.

Each committee member that voted receives a reward of participant_reward, and the proposer receives one seventh of this in addition.

Each committee member that failed to vote receives a penalty of participant_reward, and the proposer receives nothing.

In our notation the maximum issuance (reward) due to sync committees per slot is as follows.

$$I_S = \frac{W_y}{32 \cdot W_\Sigma} NB$$

The per-epoch reward is thirty-two times this. The maximum reward for the proposer in respect of sync aggregates:

$$I_{S_P} = \frac{W_p}{W_\Sigma - W_p} I_S$$

Used by	<pre>process_operations()</pre>
Uses	<pre>get_domain(), compute_signing_root(), eth_fast_aggregate_verify(), get_total_active_balance(), get_base_reward_per_increment(), increase_balance(), decrease_balance()</pre>
See also	Incentivization weights, SYNC_COMMITTEE_SIZE

Initialise State

Introduction

TODO: rework and synthesis - this text is from the original Genesis.

Before the Ethereum beacon chain genesis has been triggered, and for every Ethereum proof-of-work block, let candidate_state = initialize_beacon_state_from_eth1(eth1_block_hash, eth1_timestamp, deposits) where:

- eth1 block hash is the hash of the Ethereum proof-of-work block
- eth1 timestamp is the Unix timestamp corresponding to eth1 block hash
- deposits is the sequence of all deposits, ordered chronologically, up to (and including) the block with hash eth1_block_hash

Proof of work blocks must only be considered once they are at least SECONDS_PER_ETH1_BLOCK * ETH1_FOLLOW_DISTANCE seconds old (i.e. eth1_timestamp + SECONDS_PER_ETH1_BLOCK * ETH1_FOLLOW_DISTANCE <= current_unix_time). Due to this constraint, if GENESIS_DELAY < SECONDS_PER_ETH1_BLOCK * ETH1_FOLLOW_DISTANCE, then the genesis_time can happen before the time/state is first known. Values should be configured to avoid this case.

Initialisation

Aka genesis.

This helper function is only for initializing the state for pure Capella testnets and tests.

```
def initialize_beacon_state_from_eth1(eth1_block_hash: Hash32,
                                                                                               eth1_timestamp: uint64,
                                                                                               deposits: Sequence[Deposit],
                                                                                               execution_payload_header:
                                                                                                     \hookrightarrow \ {\tt ExecutionPayloadHeader=ExecutionPayloadHeader()}
                                                                                                ) -> BeaconState:
         fork = Fork(
                   previous_version=CAPELLA_FORK_VERSION, # [Modified in Capella] for testing only
                   current_version=CAPELLA_FORK_VERSION, # [Modified in Capella]
                   epoch=GENESIS_EPOCH,
         state = BeaconState(
                   genesis_time=eth1_timestamp + GENESIS_DELAY,
                   \tt eth1\_data=Eth1Data(block\_hash=eth1\_block\_hash, \ deposit\_count=uint64(len(deposits))), \\ \tt eth1\_data=Eth1Data(block\_hash=eth1\_block\_hash, \ deposit\_count=uint64(len(deposits)))), \\ \tt eth1\_data=Eth1Data(block\_hash=eth1\_block\_hash), \\ \tt eth1\_data=Eth1Data(block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_hash=eth1\_block\_h
                   latest\_block\_header=BeaconBlockHeader(body\_root=hash\_tree\_root(BeaconBlockBody())),\\
                   randao_mixes=[eth1_block_hash] * EPOCHS_PER_HISTORICAL_VECTOR, # Seed RANDAO with Eth1 entropy
         )
         # Process deposits
         leaves = list(map(lambda deposit: deposit.data, deposits))
         for index, deposit in enumerate(deposits):
                   deposit_data_list = List[DepositData, 2**DEPOSIT_CONTRACT_TREE_DEPTH](*leaves[:index + 1])
                    state.ethl_data.deposit_root = hash_tree_root(deposit_data_list)
                   process_deposit(state, deposit)
         # Process activations
          for index, validator in enumerate(state.validators):
                   balance = state.balances[index]
                   validator.effective_balance = min(balance - balance % EFFECTIVE_BALANCE_INCREMENT,
                                                                                                    \hookrightarrow MAX_EFFECTIVE_BALANCE)
                   if validator.effective balance == MAX EFFECTIVE BALANCE:
                              validator.activation_eligibility_epoch = GENESIS_EPOCH
                              validator.activation_epoch = GENESIS_EPOCH
         # Set genesis validators root for domain separation and chain versioning
```

```
state.genesis_validators_root = hash_tree_root(state.validators)

# Fill in sync committees

# Note: A duplicate committee is assigned for the current and next committee at genesis
state.current_sync_committee = get_next_sync_committee(state)
state.next_sync_committee = get_next_sync_committee(state)

# Initialize the execution payload header
state.latest_execution_payload_header = execution_payload_header
return state
```

Each state fields start with its default SSZ value unless a value is explicitly provided. So, for example, state.next_withdrawal_index will be initialised to zero, and state.historical_summaries to an empty list.

Genesis state

Let genesis_state = candidate_state whenever is_valid_genesis_state(candidate_state) is True for the first time.

```
def is_valid_genesis_state(state: BeaconState) -> bool:
    if state.genesis_time < MIN_GENESIS_TIME:
        return False
    if len(get_active_validator_indices(state, GENESIS_EPOCH)) < MIN_GENESIS_ACTIVE_VALIDATOR_COUNT:
        return False
    return True</pre>
```

TODO

Genesis block

```
\label{eq:lock} Let \ genesis\_block = BeaconBlock(state\_root=hash\_tree\_root(genesis\_state)). \\ TODO
```

Fork Choice

Introduction

The beacon chain's fork choice is documented separately from the main state transition specification. Like the main specification, the fork choice spec is incremental, with later versions specifying only the changes since the previous version. When annotating the main spec I combined the incremental versions into a single up-to-date document. In the following, however, I will deal separately with the original Phase 0 fork choice and the incremental Bellatrix fork choice update as the latter mainly introduced one-off functionality specific to the Merge transition.

What's a fork choice?

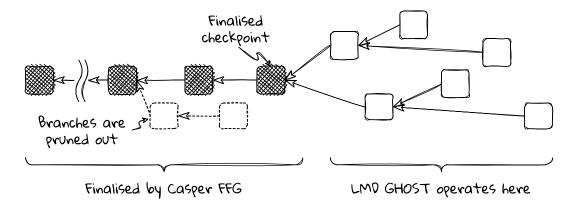
As described in the introduction to consensus, a fork choice rule is the means by which a node decides, given the information available to it, which block is the "best" head of the chain. A good fork choice rule results in the network of nodes eventually converging on the same canonical chain: it is able to resolve forks consistently, even under a degree of faulty or adversarial behaviour.

Ethereum's proof of stake consensus introduces a Store object that contains all the data necessary for determining a best head. A node's Store is the "source of truth" for its fork choice rule. In classical consensus terms it is a node's local view: all the relevant information that a node has about the network state. The fork choice rule can be characterised as a function, $GetHead(Store) \rightarrow HeadBlock$.

During the Merge event, the beacon chain's fork choice was temporarily augmented to be able to consider blocks on the Eth1 chain, in order to agree which (of potentially multiple candidates) would become the terminal proof of work block.

Overview

Ethereum's fork choice comprises the LMD GHOST fork choice rule, modified by (constrained by) the Casper FFG fork choice rule. The Casper FFG rule modifies the LMD GHOST fork choice by only allowing blocks descended from the last finalised¹¹² checkpoint to be candidates for the chain head. All earlier branches are effectively pruned out of a node's local view of the network state.



Casper FFG's role is to finalise a checkpoint. History prior to the finalised checkpoint is a linear chain of blocks with all branches pruned away. LMD GHOST is used to select the best head block at any time. LMD GHOST is constrained by Casper FFG in that it operates on the block tree only after the finalised checkpoint.

This combination has come to be known as "Gasper", and appears to be relatively simple at first sight. However, the emergence of various edge cases, and a relentless stream of potential attacks has led third

¹¹² I'm simplifying here. LMD GHOST can only consider descendants of the last justified checkpoint at any one time. But the last justified checkpoint can change. LMD GHOST will never consider branches from before the last finalised checkpoint. More on this later.

party researchers to declare that "The Gasper protocol is complex". And that remark was made before implementing many of the fixes that we'll be reviewing in the following sections. Vitalik himself has written that

The "interface" between Casper FFG finalization and LMD GHOST fork choice is a source of significant complexity, leading to a number of attacks that have required fairly complicated patches to fix, with more weaknesses being regularly discovered.

Despite all this, we are happily running Ethereum on top of the Gasper protocol today. We continue to incrementally add defences against known attacks, and one day we may move on from Gasper entirely perhaps to a single slot finality protocol, or to Casper CBC. Meanwhile, Gasper is proving to be "good enough" in practice. ¹¹³

Scope and terminology

These fork choice specification documents don't cover the whole mechanism. They are largely concerned only with the LMD GHOST fork choice; the Casper FFG side of things (justification and finalisation) is dealt with in the main state-transition specification.

The terms attestation, vote, and message appear frequently. An attestation is a collection of three votes: a vote for a source checkpoint, a vote for a target checkpoint, and a vote for a head block. The source and target votes are used by Casper FFG, and the head vote is used by LMD GHOST. We will mostly be concerned with head votes in the following sections, except when stated otherwise. LMD GHOST head votes are also called messages, being the "M" in "LMD".

Where we discuss attestations, they can be a single attestation from one validator, or aggregate attestations containing the attestations of multiple validators that made the same set of votes. It will be clear from the context which of these applies.

Decoding dev-speak

Sometimes you'll hear protocol devs say slightly obscure things like, "we can deal with that in fork choice". For example, "we can handle censorship via the fork choice".

This framing makes sense when we understand that a node's fork choice rule is its expression of which chain it prefers to follow, or prefers not to follow. No honest node wants to follow a chain that contains invalid blocks (according to the state transition), so the fork choice of all honest nodes will never select a head block that has an invalid block in its ancestry.

Similarly, nodes could modify their fork choice rule so that branches with blocks that appear to censor transactions are never selected. If nodes with sufficient validators do this, then any such block will be orphaned, strongly discouraging censorship. This works both ways, of course. A government could declare that the fork choice must ignore any branches with blocks that do *not* censor transactions. If enough validators – over half – choose to comply, then the whole chain will become censoring.

The goal of the fork choice is for the network to converge onto a single history, so there is a strong incentive to try to agree with one's peers. However, it also provides a mechanism that can be used (perhaps as an outcome of social coordination) to be opinionated about what kind of blocks are eventually included in that history.

History

Proof of stake Ethereum has a long history that we shall review elsewhere. The following milestones are significant for the current Casper FFG plus LMD GHOST implementation.

Vitalik published the original mini-spec for the beacon chain's proof of stake consensus on July 31st 2018, shortly after we had abandoned prior designs for moving Ethereum to PoS. The initial design used IMD GHOST (Immediate Message Driven GHOST) in which attestations have a limited lifetime in the fork

¹¹³Appendix C.1 of the Goldfish, "No More Attacks on Proof-of-Stake Ethereum?" paper is a useful overview of known weaknesses of Gasper consensus.

choice¹¹⁴. IMD GHOST was changed to LMD GHOST (Latest Message Driven GHOST) in November 2018 due to concerns about the stability property of IMD.

The initial fork choice spec was published to GitHub in April 2019, numbering a mere 96 lines. The current Phase 0 fork choice spec has 576 lines.

Various issues have caused the fork choice specification to balloon in complexity.

In August 2019, a "decoy flip-flop attack" on LMD GHOST was identified that could be used by an adversary to delay finalisation (for a limited period of time). The defence against this is to add a check that newly considered attestations are from either the current or previous epoch only. We'll cover this under validate on attestation().

In September 2019 a "bouncing attack" on Casper FFG was identified that can delay finalisation indefinitely. Up to the Capella spec release we had a fix for this that only allowed the fork choice's justified checkpoint to be updated during the early part of an epoch. The fix was removed in the Capella upgrade since it adds significant complexity to the fork choice, and in any case can be worked around by splitting honest validators' views. The bouncing attack is very difficult to set up and an adversary with the power to do this could probably attack the chain in more interesting ways. The bouncing attack and its original fix remain documented in the Bellatrix edition.

In July 2021, an edge case was identified in which (if 1/3 of validators were prepared to be slashed) the invariant that the store's justified checkpoint must be a descendant of the finalised checkpoint could become violated. A fix to the on_tick() handler was implemented to maintain the invariant.

In November 2021, some overly complicated logic was identified in the on_block() handler that could lead to the Store retaining inconsistent finalised and justified checkpoints, which would in turn cause filter_block_tree() to fail. Over one third of validators would have had to be slashed to trigger the fault, but the resulting fix turned out to be a nice simplification in any case.

Proposer boost was also added in November 2021. This is a defence against potential balancing attacks on LMD GHOST that could prevent Casper FFG from finalising. We'll cover this in detail in the proposer boost section.

A new type of balancing attack was published in January 2022 that relies on the attacker's validators making equivocating attestations (multiple different attestations at the same slot). To counter this, a defence against equivocating indices was added in March 2022. We'll discuss this when we get to the on_attester_slashing() handler. This defence was bolstered in the Capella spec update by excluding all slashed validators from having an influence in the fork choice.

Several issues involving "unrealised justification" were discovered during the first half of 2022. First, an unrealised justification reorg attack that allowed the proposer of the first block of an epoch to easily fork out up to nine blocks from the end of the previous epoch. A variant of that attack was also found to be able to cause validators to make slashable attestations. Second, a justification withholding attack that an adversary could use to reorg arbitrary numbers of blocks at the start of an epoch. These issues were addressed in the Capella spec update with the "pull up tips" and unrealised justification logic that it introduced.

A reader might infer from this catalogue of issues that the fork choice is fiendishly difficult to reason about, and the reader would not be wrong. Some long-overdue formal verification work on the fork choice rule has recently been completed. It seeks to prove certain desirable properties, such as that an honest validator following the rules can never make slashable attestations.

We will study each of the issues above in more detail as we work through the fork choice specification in the following two sections.

- Phase 0 fork choice is the main fork choice specification.
- Bellatrix fork choice covers the changes to the fork choice around the Merge.

Note that the Capella upgrade included a substantial rewrite of the fork choice specification. The rewrite removed the bouncing attack fix and introduced the "pull up tips" defence against a new attack, among other things. The following sections are based on the updated Capella version, but the previous

 $^{^{114}}$ If I've understood correctly. Traces of IMD GHOST are difficult to find these days, and that's probably for the better.

annotated fork choice remains available. All of these changes were quietly rolled out prior to Capella, buried within various client software updates, while the updated spec was held back until the Capella upgrade itself¹¹⁵. A public disclosure of the issues was made a few weeks after the Capella upgrade.

Phase 0 Fork Choice

This section covers the Phase 0 Fork Choice document. It is based on the Capella, v1.3.0, spec release version. For an alternative take, I recommend Vitalik's annotated fork choice document.

Block-quoted content below (with a sidebar) has been copied over verbatim from the specs repo, as has all the function code.

The head block root associated with a store is defined as get_head(store). At genesis, let store = get_forkchoice_store(genesis_state, genesis_block) and update store by running:

- on_tick(store, time) whenever time > store.time where time is the current Unix time
- on_block(store, block) whenever a block block: SignedBeaconBlock is received
- on_attestation(store, attestation) whenever an attestation attestation is received
- on_attester_slashing(store, attester_slashing) whenever an attester slashing attester_slashing is received

Any of the above handlers that trigger an unhandled exception (e.g. a failed assert or an out-of-range list access) are considered invalid. Invalid calls to handlers must not modify store.

Updates to the Store arise only through the four handler functions: on_tick(), on_block(), on_attestation(), and on_attester_slashing(). These are the four senses through which the fork choice gains its knowledge of the world.

Notes: 1) Leap seconds: Slots will last SECONDS_PER_SLOT + 1 or SECONDS_PER_SLOT - 1 seconds around leap seconds. This is automatically handled by UNIX time.

Leap seconds will no longer occur after 2035. We can remove this note after that.

2) **Honest clocks**: Honest nodes are assumed to have clocks synchronized within SECONDS_PER_ SLOT seconds of each other.

In practice, the synchrony assumptions are stronger than this. Any node whose clock is more than SECONDS_PER_SLOT / INTERVALS_PER_SLOT (four seconds) adrift will suffer degraded performance and can be considered Byzantine (faulty), at least for the LMD GHOST fork choice.

3) Eth1 data: The large ETH1_FOLLOW_DISTANCE specified in the honest validator document should ensure that state.latest_eth1_data of the canonical beacon chain remains consistent with the canonical Ethereum proof-of-work chain. If not, emergency manual intervention will be required.

Post-Merge, consistency between the execution and consensus layers is no longer an issue, although we retain the ETH1_FOLLOW_DISTANCE for now.

4) **Manual forks**: Manual forks may arbitrarily change the fork choice rule but are expected to be enacted at epoch transitions, with the fork details reflected in state.fork.

Manual forks are sometimes called hard forks or upgrades, and are planned in advance and coordinated. They are different from the inadvertent forks that the fork choice rule is designed to resolve.

¹¹⁵When issues are found with the fork choice it is common for them to be "silently" fixed in client releases before being made public. Paradoxically, changes to the fork choice rule are not consensus breaking and do not usually require simultaneous activation in clients. Hard fork upgrades such as Capella ensure that all node operators have, of necessity, upgraded to the latest software versions, at which point it is safe to publish details of the problems and fixes. This is one good reason for keeping your software up to date, even between mandatory upgrades.

5) **Implementation**: The implementation found in this specification is constructed for ease of understanding rather than for optimization in computation, space, or any other resource. A number of optimized alternatives can be found here.

After reading the spec you may be puzzled by the "ease of understanding" claim. However, it is certainly true that several of the algorithms are far from efficient, and a great deal of optimisation is needed for practical implementations.

Constant

Name	Value
INTERVALS_PER_SLOT	uint64(3)

Only blocks that arrive during the first 1 / INTERVALS_PER_SLOT of a slot's duration are eligible to have the proposer score boost added. This moment is the point in the slot at which validators are expected to publish attestations declaring their view of the head of the chain.

In the Ethereum consensus specification INTERVALS_PER_SLOT neatly divides SECONDS_PER_SLOT, and all time quantities are strictly uint64 numbers of seconds. However, other chains that run the same basic protocol as Ethereum might not have this property. For example, the Gnosis Beacon Chain has five-second slots. We changed Teku's internal clock from seconds to milliseconds to support this, which is technically off-spec, but nothing broke.

Configuration

Name	Value
PROPOSER_SCORE_BOOST	uint64(40)

• The proposer score boost is worth PROPOSER_SCORE_BOOST percentage of the committee's weight, i.e., for slot with committee weight committee_weight the boost weight is equal to (committee_weight * PROPOSER_SCORE_BOOST) // 100.

Proposer boost is a modification to the fork choice rule that defends against a so-called balancing attack. When a timely block proposal is received, proposer boost temporarily adds a huge weight to that block's branch in the fork choice calculation, namely PROPOSER_SCORE_BOOST percent of the total effective balances of all the validators assigned to attest in that slot.

The value of PROPOSER_SCORE_BOOST has changed over time as the balancing attack has been analysed more thoroughly.

- Vitalik's original proposed mitigation discussed using a value of 25%.
- The initial implementation on November 23, 2021, changed it to 70% (without any recorded rationale for that number).
- On May 9, 2022, it was changed to 33% as the result of much more detailed analysis.
- On May 20, 2022, it was changed to 40%, due to an off-by-one calculation in the above analysis.

The basic trade-off in choosing a value for PROPOSER_SCORE_BOOST is between allowing an adversary to perform "ex-ante" or "ex-post" reorgs. Setting PROPOSER_SCORE_BOOST too high makes it easier for an adversarial proposer to perform ex-post reorgs - it gives the proposer disproportionate power compared with the votes of validators. Setting PROPOSER_SCORE_BOOST too low makes it easier for an adversary to perform ex-ante reorgs. Caspar Schwarz-Schilling covers these trade-offs nicely in his Liscon talk, The game of reorgs in PoS Ethereum. 116

¹¹⁶"Ex-post" reorgs occur when a proposer orphans the block in the previous slot by building on an ancestor. "Ex-ante"

Helpers

LatestMessage

```
class LatestMessage(object):
    epoch: Epoch
    root: Root
```

This is just a convenience class for tracking the most recent head vote from each validator - the "LM" (latest message) in LMD GHOST. Epoch is a uint64 type, and Root is a Bytes32 type. The Store holds a mapping of validator indices to their latest messages.

Store

The Store is responsible for tracking information required for the fork choice algorithm. The important fields being tracked are described below:

- justified_checkpoint: the justified checkpoint used as the starting point for the LMD GHOST fork choice algorithm.
- finalized_checkpoint: the highest known finalized checkpoint. The fork choice only considers blocks that are not conflicting with this checkpoint.
- unrealized_justified_checkpoint & unrealized_finalized_checkpoint: these track the highest justified & finalized checkpoints resp., without regard to whether on-chain *realization* has occurred, i.e. FFG processing of new attestations within the state transition function. This is an important distinction from justified_checkpoint & finalized_checkpoint, because they will only track the checkpoints that are realized on-chain. Note that on-chain processing of FFG information only happens at epoch boundaries.
- unrealized_justifications: stores a map of block root to the unrealized justified checkpoint observed in that block.

These explanatory points were added in the Capella upgrade¹¹⁷. We will expand on them below in the appropriate places.

```
class Store(object):
    time: uint64
    genesis_time: uint64
    justified_checkpoint: Checkpoint
    finalized_checkpoint: Checkpoint
    unrealized_justified_checkpoint: Checkpoint
    unrealized_finalized_checkpoint: Checkpoint
    proposer_boost_root: Root
    equivocating_indices: Set[ValidatorIndex]
    blocks: Dict[Root, BeaconBlock] = field(default_factory=dict)
    block_states: Dict[Root, BeaconState] = field(default_factory=dict)
    checkpoint_states: Dict[Checkpoint, BeaconState] = field(default_factory=dict)
    latest_messages: Dict[ValidatorIndex, LatestMessage] = field(default_factory=dict)
    unrealized justifications: Dict[Root, Checkpoint] = field(default_factory=dict)
```

A node's Store records all the fork choice related information that it has about the outside world. In more classical terms, the Store is the node's view of the network. The Store is updated only by the four handler functions.

The basic fields are as follows.

- time: The wall-clock time (Unix time) of the last call to the on_tick() handler. In theory this is update continuously; in practice only at least two or three times per slot.
- justified_checkpoint: Our node's view of the currently justified checkpoint.

reorgs occur when a proposer arranges to orphan the next block by submitting its own proposal late. Caspar Schwarz-Schilling made a nice Twitter thread explainer.

¹¹⁷It's interesting to see some explanation finding its way back into the spec documents now, after it was all diligently stripped out a while ago. Turns out that people appreciate explanations, I guess.

- finalized checkpoint: Our node's view of the currently finalised checkpoint.
- blocks: All the blocks that we know about that are descended from the finalized_checkpoint. The fork choice spec does not describe how to prune the Store, so we would end up with all blocks since genesis if we were to follow it precisely. However, only blocks descended from the last finalised checkpoint are ever considered in the fork choice, and the finalised checkpoint only increases in height. So it is safe for client implementations to remove from the Store all blocks (and their associated states) belonging to branches not descending from the last finalised checkpoint.
- block_states: For every block in the Store, we also keep its corresponding (post-)state. These states are mostly used for information about justification and finalisation.
- checkpoint_states: If there are empty slots immediately before a checkpoint then the checkpoint state will not correspond to a block state, so we store checkpoint states as well, indexed by Checkpoint rather than block root. The state at the last justified checkpoint is used for validator balances, and for validating attestations in the on attester slashing() handler.
- latest_messages: The set of latest head votes from validators. When the on_attestation() handler processes a new head vote for a validator, it gets added to this set and the old vote is discarded.

The following fields were added at various times as new attacks and defences were found.

- proposer_boost_root was added when proposer boost was implemented as a defence against the LMD balancing attack. It is set to the root of the current block for the duration of a slot, as long as that block arrived within the first third of a slot.
- The equivocating_indices set was added to defend against the equivocation balancing attack. It contains the indices of any validators reported as having committed an attester slashing violation. These validators must be removed from consideration in the fork choice rule until the last justified checkpoint state catches up with the fact that the validators have been slashed.
- The unrealized_justified_checkpoint and unrealized_finalized_checkpointfields were added in the Capella update. They are used to avoid certain problems with unrealised justification that the old version of filter_block_tree() suffered.
- Also added in the Capella update was unrealized_justifications, which is a map of block roots to unrealised justification checkpoints. It is maintained by compute_pulled_up_tip(). For every block, it stores the justified checkpoint that results from running process_justification_and_finalization() on the block's post-state. In the beacon state, that calculation is done only on epoch boundaries, so, within the fork choice, we call the result "unrealised".

For non-Pythonistas, Set and Dict are Python generic types. A Set is an unordered collection of objects; a Dict provides key-value look-up.

$\verb"is_previous_epoch_justified"$

```
def is_previous_epoch_justified(store: Store) -> bool:
    current_slot = get_current_slot(store)
    current_epoch = compute_epoch_at_slot(current_slot)
    return store.justified_checkpoint.epoch + 1 == current_epoch
```

Based on the current time in the Store, this function returns True if the checkpoint at the start of the previous epoch has been justified - that is, has received a super-majority Casper FFG vote.

```
Used by filter_block_tree()
```

get forkchoice store

The provided anchor-state will be regarded as a trusted state, to not roll back beyond. This should be the genesis state for a full client.

Note With regards to fork choice, block headers are interchangeable with blocks. The spec is likely to move to headers for reduced overhead in test vectors and better encapsulation. Full implementations

store blocks as part of their database and will often use full blocks when dealing with production fork choice.

```
def get forkchoice store(anchor state: BeaconState, anchor block: BeaconBlock) -> Store:
   assert anchor_block.state_root == hash_tree_root(anchor_state)
   anchor_root = hash_tree_root(anchor_block)
   anchor_epoch = get_current_epoch(anchor_state)
    justified_checkpoint = Checkpoint(epoch=anchor_epoch, root=anchor_root)
    finalized_checkpoint = Checkpoint(epoch=anchor_epoch, root=anchor_root)
    proposer_boost_root = Root()
    return Store(
        time=uint64(anchor_state.genesis_time + SECONDS_PER_SLOT * anchor_state.slot),
        genesis_time=anchor_state.genesis_time,
        justified checkpoint=justified checkpoint,
        finalized_checkpoint=finalized_checkpoint,
        unrealized_justified_checkpoint=justified_checkpoint,
        unrealized_finalized_checkpoint=finalized_checkpoint,
        proposer_boost_root=proposer_boost_root,
        equivocating_indices=set(),
        blocks={anchor_root: copy(anchor_block)},
        block_states={anchor_root: copy(anchor_state)},
        checkpoint states={justified checkpoint: copy(anchor state)},
        unrealized_justifications={anchor_root: justified_checkpoint}
    )
```

get_forkchoice_store() initialises the fork choice Store object from an anchor state and its corresponding block (header). As noted, the anchor state could be the genesis state. Equally, when using a checkpoint sync, the anchor state will be the finalised checkpoint state provided by the node operator, which will be treated as if it is a genesis state. In either case, the latest_messages store will be empty to begin with.

get_slots_since_genesis

```
def get_slots_since_genesis(store: Store) -> int:
    return (store.time - store.genesis_time) // SECONDS_PER_SLOT
```

Self explanatory. This one of only two places that store.time is used, the other being in the proposer boost logic in the on block() handler.

```
Used by get_current_slot()
```

get_current_slot

```
def get_current_slot(store: Store) -> Slot:
    return Slot(GENESIS_SLOT + get_slots_since_genesis(store))
```

Self explanatory. GENESIS_SLOT is usually zero.

compute_slots_since_epoch_start

```
def compute_slots_since_epoch_start(slot: Slot) -> int:
    return slot - compute_start_slot_at_epoch(compute_epoch_at_slot(slot))
```

Self explanatory.

```
Used by on_tick_per_slot()
Uses compute_epoch_at_slot(), compute_start_slot_at_epoch()
```

get_ancestor

```
def get_ancestor(store: Store, root: Root, slot: Slot) -> Root:
   block = store.blocks[root]
   if block.slot > slot:
       return get_ancestor(store, block.parent_root, slot)
   return root
```

Given a block root root, get_ancestor() returns the ancestor block (on the same branch) that was published at slot slot. If there was no block published at slot, then the ancestor block most recently published prior to slot is returned.

This function is sometimes used just to confirm that the block with root root is descended from a particular block at slot slot, and sometimes used actually to retrieve that ancestor block's root.

```
Uses get_ancestor() (recursively)
Used by get_weight(), filter_block_tree(), validate_on_attestation(), on_block(), get_ancestor() (recursively)
```

get_weight

```
def get weight(store: Store, root: Root) -> Gwei:
    state = store.checkpoint_states[store.justified_checkpoint]
    unslashed_and_active_indices = [
        i for i in get_active_validator_indices(state, get_current_epoch(state))
        if not state.validators[i].slashed
   attestation_score = Gwei(sum(
        state.validators[i].effective_balance for i in unslashed_and_active_indices
        if (i in store.latest_messages
            and i not in store.equivocating_indices
            and get_ancestor(store, store.latest_messages[i].root, store.blocks[root].slot) == root)
    ))
    if store.proposer_boost_root == Root():
        # Return only attestation score if ``proposer_boost_root`` is not set
        return attestation_score
   # Calculate proposer score if ``proposer_boost_root`` is set
   proposer_score = Gwei(0)
    # Boost is applied if ``root`` is an ancestor of ``proposer_boost_root``
    if get_ancestor(store, store.proposer_boost_root, store.blocks[root].slot) == root:
        committee_weight = get_total_active_balance(state) // SLOTS_PER_EPOCH
        proposer_score = (committee_weight * PROPOSER_SCORE_BOOST) // 100
    return attestation_score + proposer_score
```

Here we find the essence of the GHOST^{118} protocol: the weight of a block is the sum of the votes for that block, plus the votes for all of its descendant blocks. We include votes for descendants when calculating a block's weight because a vote for a block is an implicit vote for all of that block's ancestors as well - if a particular block gets included on chain, all its ancestors must also be included. To put it another way, we treat validators as voting for entire branches rather than just their leaves.

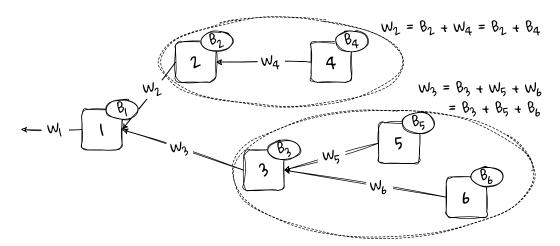
Ignoring the proposer boost part for the time being, the main calculation being performed is as follows.

¹¹⁸"Greedy Heaviest-Observed Sub-Tree", named by Sompolinsky and Zohar.

```
state = store.checkpoint_states[store.justified_checkpoint]
unslashed_and_active_indices = [
    i for i in get_active_validator_indices(state, get_current_epoch(state))
    if not state.validators[i].slashed
]
attestation_score = Gwei(sum(
    state.validators[i].effective_balance for i in unslashed_and_active_indices
    if (i in store.latest_messages
        and i not in store.equivocating_indices
        and get_ancestor(store, store.latest_messages[i].root, store.blocks[root].slot) == root)
))
```

We only consider the votes of active and unslashed validators. (Slashed validators might still be in the exit queue and are technically "active", at least according to is_active_validator().) The exclusion of validators that have been slashed in-protocol at the last justified checkpoint was added in the Capella specification to complement the on_attester_slashing() handler. It will additionally exclude validators slashed via proposer slashings, and validators slashed long ago (when the exit queue is long) and for which we have discarded the attester slashing from the Store.

Given a block root, root, this adds up all the votes for blocks that are descended from that block. More precisely, it calculates the sum of the effective balances of all validators whose latest head vote was for a descendant of root or for root itself. It's the fact that we're basing our weight calculations only on each validator's *latest* vote that makes this "LMD" (latest message drive) GHOST.



 B_N is the sum of the effective balances of the validators whose most recent head vote was for block N, and W_N is the weight of the branch starting at block N.

Some obvious relationships apply between the weights, W_x , of blocks, and B_x , the latest attesting balances of blocks.

- For a leaf block N (a block with no children), $W_N = B_N$.
- The weight of a block is its own latest attesting balance plus the sum of the weights of its direct children. So, in the diagram, $W_1 = B_1 + W_2 + W_3$.

These relationships can be used to avoid repeating lots of work by memoising the results.

Proposer boost

In September 2020, shortly before mainnet genesis, a theoretical "balancing attack" on the LMD GHOST consensus mechanism was published, with an accompanying Ethresear.ch post.

The balancing attack allows a very small number of validators controlled by an adversary to perpetually maintain a forked network, with half of all validators following one fork and half the other. This would delay finalisation indefinitely, which is a kind of liveness failure. Since the attack relies on some unrealistic

assumptions about the power an adversary has over the network – namely, fine-grained control over who can see what and when – we felt that the potential attack was not a significant threat to the launch of the beacon chain. Later refinements to the attack appear to have made it more practical to execute, however.

A modification to the fork choice to mitigate the balancing attack was first suggested by Vitalik. This became known as proposer boost, and a version of it was adopted into the consensus layer specification in late 2021 with the various client teams releasing versions with mainnet support for proposer boost in April and May 2022.

Changes to the fork choice can be made outside major protocol upgrades; it is not strictly necessary for all client implementations to make the change simultaneously, as they must for hard-fork upgrades. Given this, mainnet client releases supporting proposer boost were made at various times in April and May 2022, and users were not forced to upgrade on a fixed schedule. Unfortunately, having a mix of nodes on the network, around half applying proposer boost and half not, led to a seven block reorganisation of the beacon chain on May 25, 2022. As a result, subsequent updates to the fork choice have tended to be more tightly coordinated between client teams.

Proposer boost details

Proposer boost modifies our nice, intuitive calculation of a branch's weight, based only on latest votes, by adding additional weight to a block that was received on time in the current slot. In this way, it introduces a kind of synchrony weighting. Vitalik calls this "an explicit 'synchronization bottleneck' gadget". In short, it treats a timely block as being a vote with a massive weight that is temporarily added to the branch that it is extending.

The simple intuition behind proposer boost is summarised by Barnabé Monnot as, "a block that is timely shouldn't expect to be re-orged". In respect of the balancing attack, proposer boost is designed to overwhelm the votes from validators controlled by the adversary and instead allow the proposer of the timely block to choose the fork that will win. Quoting Francesco D'Amato, "the general strategy is to empower honest proposers to impose their view of the fork-choice, but without giving them too much power and making committees irrelevant".

The default setting for store.proposer_boost_root is Root(). That is, the "empty" or "null" default SSZ root value, with all bytes set to zero. Whenever a block is received during the first 1 / INTERVALS_PER_SLOT portion of a slot – that is, when the block is timely – store.proposer_boost_root is set to the hash tree root of that block by the on_block() handler. At the end of each slot it is reset to Root() by the on_tick() handler. Thus, proposer boost has an effect on the fork choice calculation from the point at which a timely block is received until the end of that slot, where "timely" on Ethereum's beacon chain means "within the first four seconds".

Proposer boost causes entire branches to be favoured when the block at their tip is timely. When proposer boost is in effect, and the timely block in the current slot (which has root, store.proposer_boost_root) is descended from the block we are calculating the weight for, then that block's weight is also increased, since the calculation includes the weights of all its descendants. In this way, proposer boost weighting propagates to the boosted block's ancestors in the same way as vote weights do.

The weight that proposer boost adds to the block's branch is a percentage PROPOSER_SCORE_BOOST of the total effective balance of all validators due to attest at that slot. Rather, it is an approximation to the total effective balance for that slot, derived by dividing the total effective balance of all validators by the number of slots per epoch.

The value of PROPOSER_SCORE_BOOST has changed over time before settling at its current 40%. See the description there for the history, and links to how the current value was calculated.

Proposer boost and late blocks

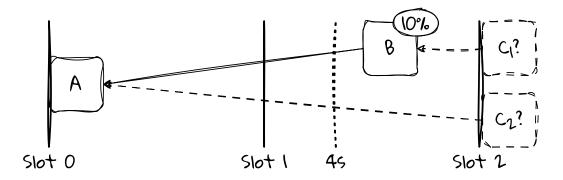
A side-effect of proposer boost is that it enables clients to reliably re-org out (orphan) blocks that were published late. Instead of building on a late block, the proposer can choose to build on the late block's parent.

A block proposer is supposed to publish its block at the start of the slot, so that it has time to be received and attested to by the whole committee within the first four seconds. However, post-merge, it

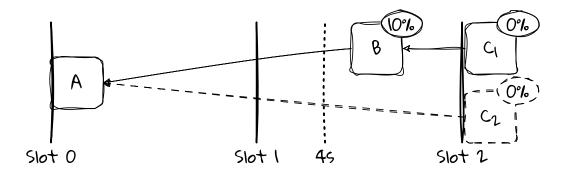
can be profitable to delay block proposals by several seconds in order to collect more transaction income and better extractable value opportunities. Although blocks published five or six seconds into a slot will not gain many votes, they are still likely to remain canonical under the basic consensus spec. As long as the next block proposer receives the late block by the end of the slot, it will usually build on it as the best available head. This is undesirable as it punishes the vast majority of honest validators, that (correctly) voted for an empty slot, by depriving them of their reward for correct head votes, and possibly even penalising them for incorrect target votes at the start of an epoch.

Without proposer boost, it is a losing strategy for the next proposer not to build on a block that it received late. Although the late block may have few votes, it has more votes than your block initially, so validators will still attest to the late block as the head of the chain, keeping it canonical and orphaning the alternative block that you built on its parent.

With proposer boost, as long as the late block has fewer votes than the proposer boost percentage, the honest proposer can be confident that its alternative block will win the fork choice for long enough that the next proposer will build on that rather than on the late block it skipped.



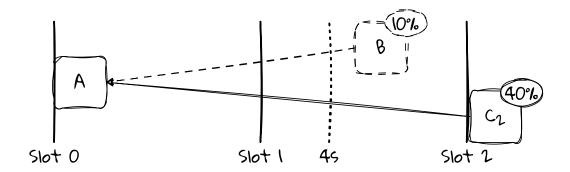
Block B was published late, well after the 4 second attestation cut-off time. However, it still managed to acquire a few attestations (say, 10% of the committee) due to dishonest or misconfigured validators. Should the next proposer build C_1 on top of the late block, or C_2 on top of its parent?



Without proposer boost, it only makes sense to build C_1 , on top of the late block B. Since B has some weight, albeit small, the top branch will win the fork choice (if the network is behaving synchronously at the time). Block C_2 would be orphaned.

An implementation of this strategy in the Lighthouse client seems to have been effective in reducing the number of late blocks on the network. Publishing of late blocks is strongly disincentivised when they

¹¹⁹For example, blocks in slot 4939809 and slot 4939815 had almost no votes and yet became canonical. They were almost certainly published late – apparently by the same operator, Legend – but in time for the next proposer to build on them. The late publishing may have been due to a simple clock misconfiguration, or it may have been a deliberate strategy to gain more transaction income post-merge. In either case, it is undesirable.



With proposer boost, the proposer of C can safely publish either C_1 or C_2 . Due to the proposer score boost of 40%, it is safe to publish block C_2 that orphans B since the lower branch will have greater weight during the slot.

are likely to be orphaned. It may be adopted as standard behaviour in the consensus specs at some point, but remains optional for the time-being. Several safe-guards are present in order to avoid liveness failures.

Note that Proposer boost does not in general allow validators to re-org out timely blocks (that is, an ex-post reorg). A timely block ought to gain enough votes from the committees that it will always remain canonical.

Alternatives to proposer boost

Proposer boost is not a perfect solution to balancing attacks or ex-ante reorgs. It makes ex-post reorgs easier to accomplish; it does not scale with participation, meaning that if only 40% of validators are online, then proposers can reorg at will; it can fail when an attacker controls several consecutive slots over which to store up votes.

Some changes to, or replacements for, LMD GHOST have been suggested that do not require proposer score boosting.

View-merge¹²⁰ is a mechanism in which attesters freeze their fork choice some time Δ before the end of a slot. The next proposer does not freeze its fork choice, however. The assumed maximum network delay is Δ , so the proposer will see all votes in time, and it will circulate a summary of them to all validators, contained within its block. This allows the whole network to synchronise on a common view. Balancing attacks rely on giving two halves of the network different views, and would be prevented by view-merge.

The Goldfish protocol, described in the paper No More Attacks on Proof-of-Stake Ethereum?, builds on view-merge (called "message buffering" there) and adds vote expiry so that head block votes expire almost immediately (hence the name - rightly or wrongly, goldfish are famed for their short memories). The resulting protocol is provably reorg resilient and supports fast confirmations.

Both view-merge and Goldfish come with nice proofs of their properties under synchronous conditions, which improve on Gasper under the same conditions. However, they may not fare so well under more realistic asynchronous conditions. The original view-merge article says of latency greater than 2 seconds, "This is bad". One of the authors of the Goldfish paper has said that Goldfish "is extremely brittle to asynchrony, allowing for catastrophic failures such as arbitrarily long reorgs" and elsewhere, "even a single slot of asynchrony can lead to a catastrophic failure, jeopardizing the safety of any previously confirmed block". At least with proposer boost, we know that it only degrades to normal Gasper under conditions of high latency.

¹²⁰View-merge, though not by that name, was first proposed for Ethereum in October 2021 in the Ethresear.ch post, Change fork choice rule to mitigate balancing and reorging attacks. See also this Twitter thread for more explanation of view-merge.

¹²¹To find the section 6.3 that this quote refers to, you need to see the original v1 version of the Goldfish paper. That section is omitted from the later version of the paper.

Francesco D'Amato argues in Reorg resilience and security in post-SSF LMD-GHOST that the real origin of the reorg issues with LMD GHOST is our current committee-based voting: "The crux of the issue is that honest majority of the committee of a slot does not equal a majority of the eligible fork-choice weight", since an adversary is able to influence the fork choice with votes from other slots. The ultimate cure for this would be single slot finality (SSF), in which all validators vote at every slot. SSF is a long way from being practical today, but a candidate for its fork choice is RLMD-GHOST (Recent Latest Message Driven GHOST), which expires votes after a configurable time period.

get voting source

```
def get_voting_source(store: Store, block_root: Root) -> Checkpoint:
    """
    Compute the voting source checkpoint in event that block with root ``block_root`` is the head block
    """
    block = store.blocks[block_root]
    current_epoch = compute_epoch_at_slot(get_current_slot(store))
    block_epoch = compute_epoch_at_slot(block.slot)
    if current_epoch > block_epoch:
        # The block is from a prior epoch, the voting source will be pulled-up
        return store.unrealized_justifications[block_root]
    else:
        # The block is not from a prior epoch, therefore the voting source is not pulled up
        head_state = store.block_states[block_root]
        return head_state.current_justified_checkpoint
```

If the given block (which is a leaf block in the Store's block tree) is from a prior epoch, then return its unrealised justification. Otherwise return the justified checkpoint from its post-state (its realised justification).

Returning the unrealised justification is called "pulling up" the block (or "pulling the tip of a branch") as it is equivalent to running the end-of-epoch state transition accounting on the block's post-state: the block is notionally pulled up from its actual slot to the first slot of the next epoch.

The Casper FFG source vote is the checkpoint that a validator believes is the highest justified at the time of the vote. As such, this function returns the source checkpoint that validators with this block as head will use when casting a Casper FFG vote in the current epoch. This has an important role in filter_block_tree() and is used in the formal proof of non-self-slashability.

```
Used by filter_block_tree()
Uses compute_epoch_at_slot()
```

filter_block_tree

Note: External calls to filter_block_tree (i.e., any calls that are not made by the recursive logic in this function) MUST set block_root to store.justified_checkpoint.

The only external call to filter_block_tree() comes from get_filtered_block_tree(), which uses store.justified_checkpoint.root. So we're all good. This is a requirement of Hybrid LMD GHOST - it enforces Casper FFG's fork choice rule.

```
def filter_block_tree(store: Store, block_root: Root, blocks: Dict[Root, BeaconBlock]) -> bool:
    block = store.blocks[block_root]
    children = [
        root for root in store.blocks.keys()
        if store.blocks[root].parent root == block root
```

```
]
# If any children branches contain expected finalized/justified checkpoints,
# add to filtered block-tree and signal viability to parent.
if any(children):
    filter_block_tree_result = [filter_block_tree(store, child, blocks) for child in children]
    if any(filter_block_tree_result):
        blocks[block_root] = block
        return True
    return False
current_epoch = compute_epoch_at_slot(get_current_slot(store))
voting_source = get_voting_source(store, block_root)
# The voting source should be at the same height as the store's justified checkpoint
correct justified = (
    store.justified_checkpoint.epoch == GENESIS_EPOCH
    or voting_source.epoch == store.justified_checkpoint.epoch
)
# If the previous epoch is justified, the block should be pulled-up. In this case, check that
                                    \hookrightarrow unrealized
# justification is higher than the store and that the voting source is not more than two epochs ago
if not correct_justified and is_previous_epoch_justified(store):
    correct_justified = (
        store.unrealized_justifications[block_root].epoch >= store.justified_checkpoint.epoch and
        voting_source.epoch + 2 >= current_epoch
    )
finalized_slot = compute_start_slot_at_epoch(store.finalized_checkpoint.epoch)
correct finalized = (
    store.finalized_checkpoint.epoch == GENESIS_EPOCH
    or store.finalized_checkpoint.root == get_ancestor(store, block_root, finalized_slot)
# If expected finalized/justified, add to viable block-tree and signal viability to parent.
if correct_justified and correct_finalized:
    blocks[block_root] = block
    return True
# Otherwise, branch not viable
return False
```

The filter_block_tree() function is at the heart of how LMD GHOST and Casper FFG are bolted together.

The basic structure is fairly simple. Given a block, filter_block_tree() recursively walks the Store's block tree visiting the block's descendants in depth-first fashion. When it arrives at a leaf block (the tip of a branch), if the leaf block is "viable" as head then it and all its ancestors (the whole branch) will be added to the blocks list, otherwise the branch will be ignored.

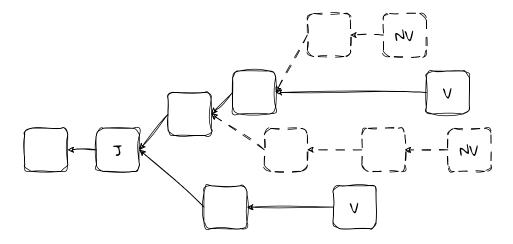
In other words, the algorithm prunes out branches that terminate in an unviable head block, and keeps branches that terminate in a viable head block.

Viability

What dictates whether a leaf block is viable or not?

Pre-Capella, there was a fairly straightforward requirement for a leaf block to be a viable head block: viable head blocks had a post-state that agreed with the Store about the justified and finalised checkpoints. This was encapsulated in the following code from the Bellatrix spec,

```
correct_justified = (
   store.justified_checkpoint.epoch == GENESIS_EPOCH
   or head_state.current_justified_checkpoint == store.justified_checkpoint
```



Block J is the Store's justified checkpoint. There are four candidate head blocks descended from it. Two are viable (V), and two are nonviable (NV). Blocks in branches terminating at viable heads are returned by the filter; blocks in branches terminating at nonviable heads are filtered out.

```
)
correct_finalized = (
    store.finalized_checkpoint.epoch == GENESIS_EPOCH
    or head_state.finalized_checkpoint == store.finalized_checkpoint
)
# If expected finalized/justified, add to viable block-tree and signal viability to parent.
if correct_justified and correct_finalized:
    blocks[block_root] = block
    return True
```

The code we have in the Capella update is considerably more complex and less intuitive. But before we get to that we need to take a step back and discuss why we should filter the block tree at all.

Why prune unviable branches?

Filtering the block tree like this ensures that the Casper FFG fork choice rule, "follow the chain containing the justified checkpoint of the greatest height", is applied to the block tree before the LMD GHOST fork choice is evaluated.

Very early versions of the spec considered the tip of any branch descended from the Store's justified checkpoint as a potential head block. However, a scenario was identified in which this could result in a deadlock, in which finality would not be able to advance without validators getting themselves slashed a kind of liveness failure¹²².

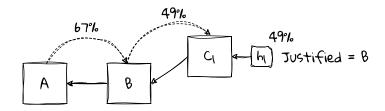
The filter_block_tree() function was added as a fix for this issue. Given a Store and a block root, filter_block_tree() returns the list of all the blocks that we know about in the tree descending from the given block, having pruned out any branches that terminate in a leaf block that is not viable in some sense

To illustrate the problem, consider the situation shown in the following diagrams, based on the original description of the issue. The context is that there is an adversary controlling 18% of validators that takes advantage of (or causes) a temporary network partition. We will illustrate the issue mostly in terms of checkpoints, and omit the intermediate blocks that carry the attestations - you can mentally insert these as necessary.

We begin with a justified checkpoint A that all nodes agree on.

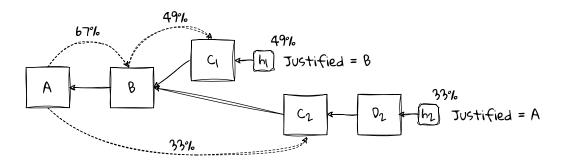
¹²²This scenario doesn't strictly break Casper FFG's "plausible liveness" property as, in principle, voters can safely ignore the LMD GHOST fork choice and switch back to the original chain in order to advance finality. But it does create a conflict between the LMD GHOST fork choice rule and advancing finality.

Due to the network partition, only 49% of validators, plus the adversary's 18%, see checkpoint B. They all make Casper FFG votes $[A \to B]$, thereby justifying B. A further checkpoint C_1 is produced on this branch, and the 49% that are honest validators dutifully make the Casper FFG vote $[B \to C_1]$, but the adversary does not, meaning that C_1 is not justified. Validators on this branch see h_1 as the head block, and have a highest justified checkpoint of B.



The large blocks represent checkpoints. After checkpoint A there is a network partition: 49% of validators plus the adversary see checkpoints B and C_1 . Casper votes are shown by the dashed arrows. The adversary votes for B, but not for C_1 .

The remaining 33% of validators do not see checkpoint B, but see C_2 instead and make Casper FFG votes $[A \to C_2]$ for it. But this is not enough votes to justify C_2 . Checkpoint D_2 is produced on top of C_2 , and a further block h_2 . On this branch, h_2 is the head of the chain according to LMD GHOST, and A remains the highest justified checkpoint.



Meanwhile, the remaining 33% of validators do not see the branch starting at B, but start a new branch containing C_2 and its descendants. They do not have enough collective weight to justify any of the checkpoints.

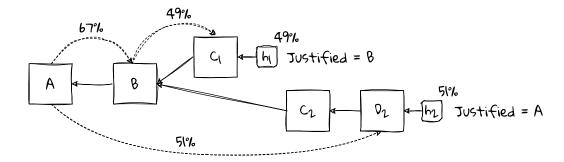
Now for the cunning part. The adversary switches its LMD GHOST vote (and implicitly its Casper FFG vote, although that does not matter for this exercise) from the first branch to the second branch, and lets the validators in the first branch see the blocks and votes on the second branch.

Block h_2 now has votes from the majority of validators – 33% plus the adversary's 18% – so all honest validators should make it their head block.

However, the justified checkpoint on the h_2 branch remains at A. This means that the 49% of validators who made Casper FFG vote $[B \to C]$ cannot switch their chain head from h_1 to h_2 without committing a Casper FFG surround vote, and thereby getting slashed. Switching branch would cause their highest justified checkpoint to go backwards. Since they have previously voted $[B \to C_1]$, they cannot now vote $[A \to X]$ where X has a height greater than C_1 , which they must do if they were to switch to the h_2 branch.

In conclusion, the chain can no longer finalise (by creating higher justified checkpoints) without a substantial proportion of validators (at least 16%) being willing to get themselves slashed.

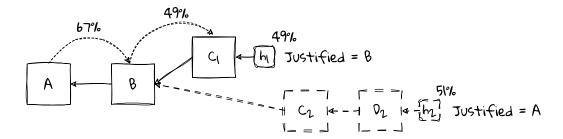
It should never be possible for the chain to get into a situation in which honest validators, following the rules of the protocol, end up in danger of being slashed. The situation here arises due to a conflict



The adversary switches to the second branch, giving h_2 the majority LMD GHOST vote. This deadlocks finalisation: the 49% who made Casper FFG vote $[B \to C_1]$ cannot switch to h_2 without being slashed.

between the Casper FFG fork choice (follow the chain containing the justified checkpoint of the greatest height) and the LMD GHOST fork choice (which, in this instance, ignores that rule). It is a symptom of the clunky way in which the two have been bolted together.

The chosen fix for all this is to filter the block tree before applying the LMD GHOST fork choice, so as to remove all "unviable" branches from consideration. That is, all branches whose head block's state does not agree with me about the current state of justification and finalisation.



When validators that followed branch 1 apply filter_block_tree(), branch 2 is pruned out (as indicated by the dashed lines). This is because their Store has B as the best justified checkpoint, while branch 2's leaf block has a state with A as the justified checkpoint. For these validators h_2 is no longer a candidate head block.

With this fix, the chain will recover the ability to finalise when the validators on the second branch eventually become aware of the first branch. On seeing h_1 and its ancestors, they will update their Stores' justified checkpoints to B and mark the h_2 branch unviable.

Unrealised justification

A major feature of the Capella update to the fork choice specification is the logic for handling "unrealised justification" when filtering the block tree.

Several issues had arisen in the former fork choice spec. First, an unrealised justification reorg attack that allowed the proposer of the first block of an epoch to easily fork out up to nine blocks from the end of the previous epoch. A variant of that attack was also found to be able to cause validators to make slashable attestations - the very issue the filter is intended to prevent. Second, a justification withholding attack that an adversary could use to reorg arbitrary numbers of blocks at the start of an epoch.

The root issue is that, within the consensus layer's state transition, the calculations that update justification and finality are done only at epoch boundaries. An adversary had a couple of ways

they could use this to filter out competing branches within filter_block_tree(). Essentially, in not accounting for unrealised justifications, the filtering was being applied too aggressively.

To be clear, both of the attacks described here apply to the old version of filter_block_tree() and have been remedied in the current release. This is the old, much simpler, code for evaluating correct_justified and correct_finalized,

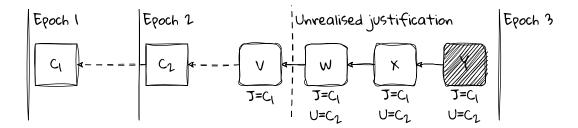
```
correct_justified = (
    store.justified_checkpoint.epoch == GENESIS_EPOCH
    or head_state.current_justified_checkpoint == store.justified_checkpoint
)
correct_finalized = (
    store.finalized_checkpoint.epoch == GENESIS_EPOCH
    or head_state.finalized_checkpoint == store.finalized_checkpoint
)
```

This meant that the tip of a branch was included for consideration if (a) the justified checkpoint in its post-state matched that in the store, and (b) the finalised checkpoint in its post-state matched that in the store. These nice simple criteria have been changed to the mess we have today, which we'll look at in a moment. But first, let's see what was wrong with the old criteria.

Unrealised justification reorg

The unrealised justification reorg allowed an adversary assigned to propose a block in the first slot of an epoch to reorg out a chain of up to nine blocks at the end of the previous epoch.

The key to this is the idea of *unrealised justification*. Towards the end of an epoch (within the last third of an epoch, that is, the last nine slots), the beacon chain might have gathered enough Casper FFG votes to justify the checkpoint at the start of that epoch. However, justification and finalisation calculations take place only at epoch boundaries, so the achieved justification is "unrealised": until the end of the epoch, all the blocks will continue have a post-state justification that points to an earlier checkpoint.

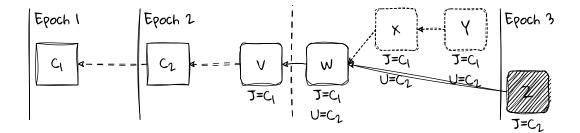


The solid vertical lines are epoch boundaries, and the squares C_1 and C_2 are their checkpoints. A block's J value shows the justified checkpoint in its poststate. Its U value is the hypothetical unrealised justification. During an epoch, the chain may gather enough Casper FFG votes to justify a new checkpoint, but justification in the beacon state happens only at epoch boundaries, so it is unrealised in the interim. Block Y is clearly the head block.

When the adversary is the proposer in the first slot of an epoch, it could have used the unrealised justification in the previous epoch to fork out the last blocks of that epoch - up to around nine of them, depending on the FFG votes the adversary's block contains. By building a competing head block the adversary could trick filter_block_tree() into filtering out the previous head branch from consideration.

Unrealised justification deadlock

It also became apparent that the pre-Capella formulation of filter_block_tree() did not fully prevent the possibility of deadlock - the very thing that filtering the block tree is intended to prevent. Deadlock is a situation in which honest validators are forced to choose between making a slashable attestation or not voting at all.



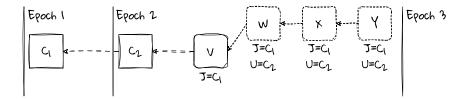
The adversary adds a block Z in the first slot of the next epoch. It builds on W, which has unrealised justification. At the epoch boundary, the state's justified checkpoint is calculated, so W's post-state has C_2 . In the former fork choice, only branches with tips that agreed with the Store about the justified checkpoint could be considered. On that basis, the branch ending in Y would have been excluded by the filter, making Z the head, even though it might have zero LMD GHOST support. Blocks X and Y would be orphaned (reorged out).

The setup and attack is described in Aditya Asgaonkar's document, and is a variant of the reorg above. The original deadlock attack relied on the network being partitioned, so that validators had split views. This newer deadlock attack did not need a network partition, but under some fairly specific unrealised justification conditions, the adversary could make the justified checkpoint go backwards. Doing this after some honest validators had already used the higher checkpoint as their Casper FFG source vote forced them subsequently to either make a surround vote, or not to vote.

Justification withholding attack

The justification withholding attack was similar to the unrealised justification reorg in that it involved using unrealised justification to get filter_block_tree() to exclude other branches besides the adversary's.

In this attack, the adversary needs to have several proposals in a row at the end of an epoch - enough that, if the adversary does not publish the blocks, the epoch does not get justified by the time it finishes. That is, without the adversary's blocks, there is no unrealised justification, with the adversary's blocks there would be unrealised justification.



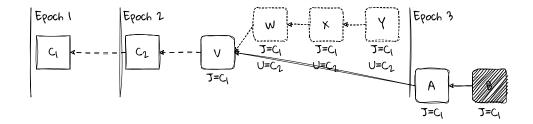
The adversary has a string of proposals at the end of an epoch. These blocks contain enough FFG votes to justify the epoch's checkpoint C_2 , but the adversary withholds them for now.

The remainder of the chain is unaware of the adversary's blocks, so continues to build as if they were skipped slots.

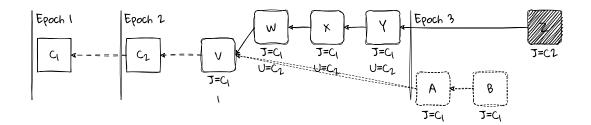
The adversary has a block proposal at some point in epoch 3 - it does not matter when.

Viable and unviable branches

The block tree filtering is done by checking that blocks at the tip of branches have the "correct" justification and finalisation in some sense. Both the correct_justified and correct_finalised flags must be true for the branch to be considered viable.



The remainder of the validators continue to build blocks A and B at the start of the next epoch. Without the adversary's blocks, checkpoint 2 is not justified, so A and B have C_1 as justified in their post-states (their unrealised justification is irrelevant here). Block B is the chain's head.



When the adversary publishes block Z in epoch 3, it releases its withheld blocks at the same time. Block Z has a post-state justified checkpoint of C_2 (updated at the epoch boundary). Under the old filter_block_tree() that would have excluded B from consideration as head, and the adversary's block Z would have become head, even with no LMD support.

correct_justified

The newer, more complex, correct justified evaluation from the Capella update is as follows.

I'm not going to pretend that I understand this fully - it seems very far from intuitive, and its correctness far from obvious ¹²³. For now I will quote some explanation that Aditya shared with me directly.

The correct_justified condition ensures that: (a) we pick a head block that has a "good" justification in its chain, and (b) that validators can vote for the chosen head block without the risk of creating slashable messages.

I describe (a) here informally, but you can think of the fork choice as a heuristic to choose where to vote so that we advance our finalized checkpoint as fast as possible. Generally, this means we vote on the highest justified checkpoint we know of, but the "that we know of" part is tricky because of the nuances of unrealized justifications and the associated reorg attacks.

Now, if you ignore unrealized justification and the reorg attacks, this first appearance of $correct_justified$ [Line A] is sufficient to address (a) & (b). Then, to fix the reorg attacks, we add an additional version of $correct_justified$ for pulled-up blocks, where the first line [line C] addresses (a) and the second line [line D] addresses (b).

Recall that the chief goal of filtering the block tree is to avoid honest validators being forced to make surround votes in Casper FFG, as these are slashable. However, earlier remedies for this were too eager in filtering out candidate heads, and an adversary could use unrealised justification to force reorgs, and even the kind of self-slashing we want to avoid.

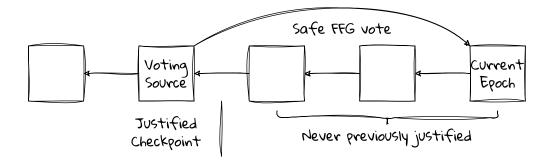
The current fork choice apparatus preserves two key properties¹²⁴.

- 1. The voting_source.epoch of a candidate head block is always less than or equal to the store.justified_checkpoint.epoch.
 - This is because on_block() always calls update_checkpoints(), and the way that the get_voting_source() function is constructed.
 - The voting_source.epoch is the Casper FFG source vote that validators with that block as head will use when making a Casper FFG vote in the current epoch.
- 2. store.justified_checkpoint.epoch never decreases (it is monotonically increasing).
 - It is only ever written to in update_checkpoints(), and it is easy to see from there that this is true.

¹²³ Some evidence for how challenging the fork choice is to reason about is provided by the formal proofs of correctness created by Roberto Saltini and team at Consensys. One of the proofs alone is 28 pages long when printed.

¹²⁴I am grateful to Mikhail Kalinin for helping me with his very lucid and careful explanation. My explanation is based on his; any errors and over-simplifications are all my own work.

With respect to the line I've marked A in the source code, if the voting source matches the Store's justified checkpoint, then all is good, we have no reason not to consider the block as head, and we can short-circuit the rest of the logic. By property 2, the Store's justified checkpoint never decreases, so a validator's Casper FFG vote based on this cannot ever be a surround vote. (Since the target vote strictly increases, it cannot be a surrounded vote either.)

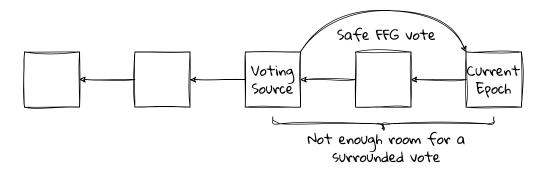


When the voting source is the same as the store's justified checkpoint, it is always safe to vote. The store's justified checkpoint never decreases, so we cannot commit a surround vote.

If the block is not a viable head by the first criterion, it might still be a viable head by the second (line D). Recall that the reorg attacks above rely on the adversary taking advantage of unrealised justification to update the Store's justified checkpoint, leaving the previous head of the chain "stale" with respect to its realised justification, although based on its unrealised justification it would still be viable. To avoid this, we wish to safely include as many viable heads as possible.

We know that any Casper FFG vote we make at this point will have voting_source.epoch strictly less than store.justified_checkpoint.epoch, by property 1, and since we already dealt with the equality case.

Line D in the source code says that it is safe to allow votes where voting_source.epoch == current_epoch - 2 and voting_source.epoch == current_epoch - 1. Any honest vote's target epoch will be current_epoch, so the gap between source and target is at most two epochs, which is not enough to surround a previous vote. That is, a vote $[s_2 \to t_2]$ that surrounds a previous vote $[s_1 \to t_1]$ requires that $s_2 < s_1 < t_1 < t_2$. This is not possible if $t_2 - s_2 \le 2$. This exception is required for the analysis of the safe block confirmation rule, and is discussed in section 3.3 of the Confirmation Rule paper.



When the voting source is within two epochs of the current epoch then it is safe to vote as a surround vote must encompass at least two intervening checkpoints.

Both line B (the condition on justification of the previous epoch) and line C seem to be unnecessary, and may be removed in future. See sections 3.3 and 3.4 of the (draft) A Confirmation Rule for the Ethereum Consensus Protocol paper for discussion of this. Note, though, that the proof of the honest viable head property described below relies on the weaker condition that store.justified_checkpoint.epoch >= current_epoch - 2 (that either the previous or previous but one epoch is justified).

correct_finalized

The Capella update's change to correct finalized is more limited, and more intuitive.

```
finalized_slot = compute_start_slot_at_epoch(store.finalized_checkpoint.epoch)
correct_finalized = (
    store.finalized_checkpoint.epoch == GENESIS_EPOCH
    or store.finalized_checkpoint.root == get_ancestor(store, block_root, finalized_slot)
)
```

This simply ensures that a viable block is descended from the Store's finalised checkpoint

The previous version made use the post-state of the block being considered for viability, which caused it to suffer from similar complications to correct_justified with respect to unrealised finality. We don't actually care about the block's post-state view of finalisation, since finality is a global property: as long as the block is descended from the finalised checkpoint it should be eligible for consideration to become viable.

The correct_finalized check might appear redundant at first sight since we are always filtering based on a tree rooted at the last justified checkpoint, which (in the absence of a mass slashing) must be descended from the last finalised checkpoint. The check, however, guarantees the further condition that a node's own view of the finalised checkpoint is irreversible, even if there were to be a mass slashing - this is the irreversible local finality formal property in the next section. Maintaining this invariant is a huge help in building efficient clients - we are free to forget about everything prior to the last finalised checkpoint.

Formal proofs

As referenced in the Ethereum Foundation's disclosure on the Capella fork choice spec updates, some properties of the new fork choice have been formally verified by Roberto Saltini and his team at Consensys.

This formal verification process involves selecting some properties that we wish to be true for the fork choice, and manually constructing proofs that they are always preserved by the specification. It is a much more robust and rigorous process than manual testing, fuzz testing, or general hand-waving that have hitherto been the main approaches.

Four properties were proved in the documents.

- Non-Self-Slashability
 - Any validator that follows the honest validator guide will never slash itself.
- Honest Viable Head
 - Assuming a synchronous network, current_epoch 2 being justified, and honest nodes having received enough attestations to justify the highest possible justified checkpoint, any block proposed by an honest node during the current epoch that is a descendent of the highest possible justified checkpoint is included in the output of get_filtered_block_tree().
- Deadlock Freedom
 - A distributed system running the Ethereum protocol can never end up in a state in which it is impossible to finalise a new epoch.
- Irreversible Local Finality
 - A block, once finalized in the local view of an honest validator, is never reverted from the canonical chain in the local view.

Given the complexity of reasoning about the fork choice, and it's rather chequered history, it is hugely reassuring now to have these proofs of correctness¹²⁵.

¹²⁵However, there remain some assumptions in the proofs that are over-simplified, such as, "No bound on the amount of attestations that can be included in a block", and, "Honest nodes do not discard any attestation that they receive regardless of how old it is". There is some history of failed proofs around the fork choice that were based on assumptions that were too broad. Hopefully these will stand; I am not equipped to judge.

Conclusion

This has been a long section on a short function. As I said at the start of the section, filter_block_tree() is at the heart of how LMD GHOST and Casper FFG are bolted together, and I think it has surprised everybody how many complexities lurk here.

As an exercise for the reader, we can imagine life without having to filter the block tree. Potuz has documented some thoughts on this in, Fork choice without on-state FFG filtering.

Ultimately, as with proposer boost, the complexities around the Gasper fork choice largely arise from our slot-based voting, with votes accumulated gradually through an epoch. This results in unrealised justification and the rest of it. The long-term fix is also probably the same: moving to single slot finality.

get filtered block tree

```
def get_filtered_block_tree(store: Store) -> Dict[Root, BeaconBlock]:
    """
    Retrieve a filtered block tree from ``store``, only returning branches
    whose leaf state's justified/finalized info agrees with that in ``store``.
    """
    base = store.justified_checkpoint.root
    blocks: Dict[Root, BeaconBlock] = {}
    filter_block_tree(store, base, blocks)
    return blocks
```

A convenience wrapper that passes the Store's justified checkpoint to filter_block_tree(). On returning, the blocks dictionary structure will contain the blocks from all viable branches rooted at that checkpoint, and nothing that does not descend from that checkpoint. For the meaning of "viable", see above.

```
Used by get_head()
Uses filter_block_tree()
```

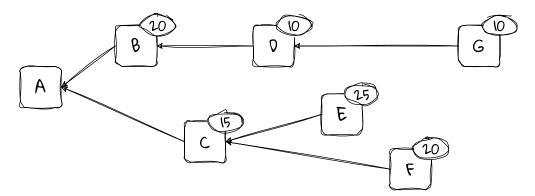
get_head

```
def get_head(store: Store) -> Root:
    # Get filtered block tree that only includes viable branches
    blocks = get_filtered_block_tree(store)
    # Execute the LMD-GHOST fork choice
    head = store.justified_checkpoint.root
    while True:
        children = [
            root for root in blocks.keys()
            if blocks[root].parent_root == head
        ]
        if len(children) == 0:
            return head
        # Sort by latest attesting balance with ties broken lexicographically
        # Ties broken by favoring block with lexicographically higher root
        head = max(children, key=lambda root: (get_weight(store, root), root))
```

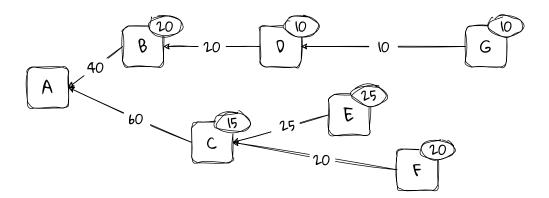
get_head() encapsulates the fork choice rule: given a Store it returns a head block.

The fork choice rule is objective in that, given the same Store, it will always return the same head block. But the overall process is subjective in that each node on the network will tend to have a different view, that is, a different Store, due to delays in receiving attestations or blocks, or having seen different sets of attestations or blocks because of network asynchrony or an attack.

Looking first at the while True loop, this implements LMD GHOST in its purest form. Starting from a given block (which would be the genesis block in unmodified LMD GHOST), we find the weights of the children of that block. We choose the child block with the largest weight and repeat the process until we end up at a leaf block (the tip of a branch). That is, we Greedily take the Heaviest Observed Sub-Tree, GHOST. Any tie between two child blocks with the same weight is broken by comparing their block hashes, so we end up at a unique leaf block - the head that we return.



get_head() starts from the root block, A, of a block tree. The numbers show each block's weight, which is its latest attesting balance - the sum of the effective balances of the validators that cast their latest vote for that block. Proposer boost can temporarily increase the latest block's score (not shown).



The get_weight() function when applied to a block returns the total weight of the subtree of the block and all its descendants. These weights are shown on the lines between child and parent blocks.

Hybrid LMD GHOST

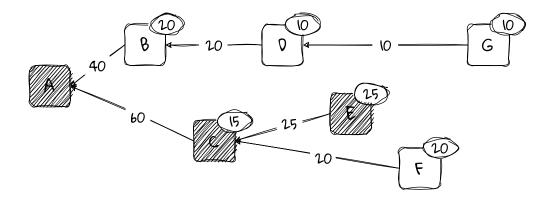
What we've just described is the pure LMD GHOST algorithm. Starting from the genesis block, it walks the entire block tree, taking the heaviest branch at each fork until it reaches a leaf block.

What is implemented in <code>get_head()</code> however, is a modified form of this that the <code>Gasper paper¹²⁷</code> refers to as "hybrid LMD GHOST" (HLMD GHOST). It is not pure LMD GHOST, but LMD GHOST modified by the Casper FFG consensus.

Get filtered block tree that only includes viable branches
blocks = get_filtered_block_tree(store)
Execute the LMD-GHOST fork choice
head = store.justified_checkpoint.root

 $^{^{126}\}mathrm{The}$ algorithm is recursive, although it is not written recursively here.

¹²⁷See section 4.6 of that paper.



Given a block, the loop in get_head() considers its children and selects the one that roots the subtree with the highest weight. It repeats the process with the heaviest child block¹²⁶ until it reaches a block with no children. In this example, it would select the branch $A \leftarrow C \leftarrow E$, returning E as the head block.

Specifically, rather than starting to walk the tree from the genesis block, we start from the last justified checkpoint, and rather than considering all blocks that the Store knows about, we first filter out "unviable" branches with get_filtered_block_tree().

This is the point at which the Casper FFG fork choice rule, "follow the chain containing the justified checkpoint of the greatest height", meets the LMD GHOST fork choice rule. The former modifies the latter to give us the HLMD GHOST fork choice rule.

Uses get_filtered_block_tree(), get_weight()

update_checkpoints

Update the checkpoints in the store if either of the given justified or finalised checkpoints is newer.

Justification and finalisation are supposed to be "global" properties of the chain, not specific to any one branch, so we keep our Store up to date with the highest checkpoints we've seen.

Note that, by construction, the Store's justified and finalised checkpoints can only increase monotonically. The former is important for the formal proof of non-self-slashability.

Used by compute_pulled_up_tip(), on_tick_per_slot(), on_block()

update_unrealized_checkpoints

....

```
Update unrealized checkpoints in store if necessary
"""
# Update unrealized justified checkpoint
if unrealized_justified_checkpoint.epoch > store.unrealized_justified_checkpoint.epoch:
    store.unrealized_justified_checkpoint = unrealized_justified_checkpoint
# Update unrealized finalized checkpoint
if unrealized_finalized_checkpoint.epoch > store.unrealized_finalized_checkpoint.epoch:
    store.unrealized_finalized_checkpoint = unrealized_finalized_checkpoint
```

The counterpart to update_checkpoints() for unrealised justified and finalised checkpoints.

```
Used by compute_pulled_up_tip()
```

Pull-up tip helpers

compute_pulled_up_tip

```
def compute_pulled_up_tip(store: Store, block_root: Root) -> None:
    state = store.block_states[block_root].copy()
    # Pull up the post-state of the block to the next epoch boundary
    process_justification_and_finalization(state)

store.unrealized_justifications[block_root] = state.current_justified_checkpoint
    update_unrealized_checkpoints(store, state.current_justified_checkpoint, state.finalized_checkpoint)

# If the block is from a prior epoch, apply the realized values
    block_epoch = compute_epoch_at_slot(store.blocks[block_root].slot)
    current_epoch = compute_epoch_at_slot(get_current_slot(store))
    if block_epoch < current_epoch:
        update_checkpoints(store, state.current_justified_checkpoint, state.finalized_checkpoint)</pre>
```

compute_pulled_up_tip() is called for every block processed in order to maintain the update_unrealized_ checkpoints map. It was added in the Capella spec update.

The major work in this routine is in the call to process_justification_and_finalization(). In the state transition, this is called once per epoch. Now we are calling it once per block, which would add significant load if implemented naively.

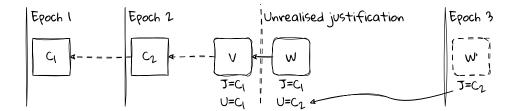
Since the state transition only calls process_justification_and_finalization() at epoch boundaries, the beacon state's justification and finalisation information cannot change mid-epoch. However, Casper FFG votes accumulate throughout the progress of the epoch, and at some point prior to the end of the epoch, enough votes will usually have been included on chain to justify a new checkpoint. When this occurs, we call it "unrealised justification" since it is not yet reflected on chain (in the beacon state). Unrealised justification reflects what the beacon state would be if the end of epoch accounting were to be run immediately on the block - hence the "pulled up tip" naming.

We simulate "pulling up" the block to the next epoch boundary to find out what the justification and finalisation status would be. When the next epoch begins, the unrealised values will become realised.

As illustrated, the unrealised justification, U, can differ from the realised justification, J, due to unprocessed Casper FFG votes accumulating during an epoch. However, an epoch's own checkpoint cannot gain unrealised justification until at least 2/3 of the way through an epoch (23 slots, since attestations are included one slot after the slot they attest to). That is, the earliest that block W could occur is in slot 22 of epoch 2 (slot counting is zero-based).

After adding the block and its unrealised justification checkpoint to the store.unrealized_justifications map, the Store's unrealized_justified_checkpoint and unrealized_finalized_checkpoint are updated if the block's values are newer.

If the block is from a previous epoch, then its justification and finalisation are no longer unrealised, since the beacon state has gone through an actual epoch transition since then, so we can update the Store's justified_checkpoint and finalized_checkpoint if the block has newer ones.



Each block has a J value, which is the justified checkpoint its post-state knows about. J is updated only at epoch boundaries. We notionally add a U value, which is the justified checkpoint that would be in the block's post-state were it to be "pulled up" to the next epoch boundary, where the beacon state's justification and finalisation calculations are done (shown as W').

on_tick helpers

on_tick_per_slot

The on_tick_per_slot() helper is called at least once every slot. If a tick hasn't been processed for multiple slots, then the on_tick() handler calls it repeatedly to process (synthetic) ticks for the those slots. This ensures that update_checkpoints() is called when there is no tick processed during the first slot of an epoch.

The on_tick_per_slot() helper has three duties,

- updating the time,
- resetting proposer boost, and
- updating checkpoints on epoch boundaries.

Updating the time

```
# update store time
store.time = time
```

The store has a notion of the current time that is used when calculating the current slot and when applying proposer boost. The time parameter does not need to be very granular. If it weren't for proposer boost, it would be fine to measure time in whole slots, at least within the fork choice¹²⁸.

Resetting proposer boost

```
# Reset store.proposer_boost_root if this is a new slot
if current_slot > previous_slot:
    store.proposer_boost_root = Root()
```

Proposer boost is a defence against balancing attacks on LMD GHOST. It rewards timely blocks with extra weight in the fork choice, making it unlikely that an honest proposer's block will become orphaned.

The Store's proposer_boost_root field is set in the on_block() handler when a block is received and processed in a timely manner (within the first four seconds of its slot). For the remainder of the slot this allows extra weight to be added to the block in get_weight().

The logic here resets proposer_boost_root to a default value at the start of the next slot, thereby removing the extra proposer boost weight until the next timely block is processed.

Updating checkpoints

If it's the first slot of an epoch, then we have gone through an epoch boundary since the last tick, and our unrealised justification and finalisation have become realised. They should now be in-sync with the justified and finalised checkpoints in the beacon state.

```
Used by on_tick()
Uses on_tick()
get_current_slot(), compute_slots_since_epoch_start(), update_checkpoints()
```

on_attestation helpers

validate_target_epoch_against_current_time

```
def validate_target_epoch_against_current_time(store: Store, attestation: Attestation) -> None:
    target = attestation.data.target

# Attestations must be from the current or previous epoch
    current_epoch = compute_epoch_at_slot(get_current_slot(store))

# Use GENESIS_EPOCH for previous when genesis to avoid underflow
    previous_epoch = current_epoch - 1 if current_epoch > GENESIS_EPOCH else GENESIS_EPOCH

# If attestation target is from a future epoch, delay consideration until the epoch arrives
    assert target.epoch in [current_epoch, previous_epoch]
```

This function simply checks that an attestation came from the current or previous epoch, based on its target checkpoint vote. The Store has a notion of the current time, maintained by the on_tick() handler, so it's a straightforward calculation. The timeliness check was introduced to defend against the "decoy flip-flop" attack described below.

Note that there is a small inconsistency here. Attestations may be included in blocks only for 32 slots after the slot in which they were published. However, they are valid for consideration in the fork choice for two epochs, which is up to 64 slots.

```
Used by validate_on_attestation()
```

¹²⁸Changing time from seconds to slots in the fork choice has been suggested, but never adopted.

Uses get_current_slot(), compute_epoch_at_slot()

validate_on_attestation

```
def validate on attestation(store: Store, attestation: Attestation, is from block: bool) -> None:
    target = attestation.data.target
   # If the given attestation is not from a beacon block message, we have to check the target epoch
                                         \hookrightarrow scope.
    if not is_from_block:
        validate_target_epoch_against_current_time(store, attestation)
   # Check that the epoch number and slot number are matching
   assert target.epoch == compute epoch at slot(attestation.data.slot)
   # Attestation target must be for a known block. If target block is unknown, delay consideration until
                                         \hookrightarrow block is found
   assert target.root in store.blocks
    # Attestations must be for a known block. If block is unknown, delay consideration until the block is
                                         \hookrightarrow found
   assert attestation.data.beacon_block_root in store.blocks
   # Attestations must not be for blocks in the future. If not, the attestation should not be considered
   assert store.blocks[attestation.data.beacon block root].slot <= attestation.data.slot</pre>
   # LMD vote must be consistent with FFG vote target
    target_slot = compute_start_slot_at_epoch(target.epoch)
   assert target.root == get_ancestor(store, attestation.data.beacon_block_root, target_slot)
   # Attestations can only affect the fork choice of subsequent slots.
   # Delay consideration in the fork choice until their slot is in the past.
    assert get_current_slot(store) >= attestation.data.slot + 1
```

This is a utility function for the on_attestation() handler that collects together the various validity checks we want to perform on an attestation before we make any changes to the Store. Recall that a failed assertion means that the handler will exit and any changes made to the Store must be rolled back.

Attestation timeliness

First, we check the attestation's timeliness. Newly received attestations are considered for insertion into the Store only if they came from the current or previous epoch at the time when we heard about them.

This check was introduced to defend against a "decoy flip-flop attack" on LMD GHOST. The attack depends on two competing branches having emerged due to some network failure. An adversary with some fraction of the stake (but less than 33%) can store up votes from earlier epochs and release them at carefully timed moments to switch the winning branch (according to the LMD GHOST fork choice) so that neither branch can gain the necessary 2/3 weight for finalisation. The attack can continue until the adversary runs out of stored votes.

Allowing only attestations from the current and previous epoch to be valid for updates to the Store seems to be an effective defence as it prevents the attacker from storing up attestations from previous epochs. The PR implementing this describes it as "FMD GHOST" (fresh message driven GHOST). However, the fork choice still relies on the latest message ("LMD") from each validator in the Store, no matter how old it is. We seem to have ended up with a kind of hybrid FMD/LMD GHOST in practice¹²⁹.

¹²⁹FMD vs LMD GHOST is discussed further in the Ethresear.ch article, Saving strategy and FMD GHOST. Later work, such as the Goldfish protocol and RLMD GHOST, take vote-expiry further.

As for the if not is_from_block test, this allows the processing of old attestations by the on_attestation handler if they were received in a block. It seems to have been introduced to help with test generation rather than being anything required in normal operation. Here's a comment from the PR that introduced it

Also good to move ahead with processing old attestations from blocks for now - that's the only way to make atomic updates to the store work in our current testing setup. If that changes in the future, this logic should go through security analysis (esp. for flip-flop attacks).

Attestations are valid for inclusion in a block only if they are less than 32 slots old. These will be a subset of the "fresh" votes made at the time (the "current plus previous epoch" criterion for freshness could encompass as many as 64 slots).

Matching epoch and slot

```
# Check that the epoch number and slot number are matching
assert target.epoch == compute_epoch_at_slot(attestation.data.slot)
```

This check addresses an edge case in which validators could fabricate votes for a prior or subsequent epoch. It's probably not a big issue for the fork choice, more for the beacon chain state transition accounting. Nevertheless, the check was implemented in both places.

No attestations for unknown blocks

```
# Attestations target be for a known block. If target block is unknown, delay consideration until the \hookrightarrow block is found assert target.root in store.blocks # Attestations must be for a known block. If block is unknown, delay consideration until the block is \hookrightarrow found assert attestation.data.beacon_block_root in store.blocks
```

This seems like a natural check - if we don't know about a block (either a target checkpoint or the head block), there's no point processing any votes for it. These conditions were added to the spec without further rationale. As noted in the comments, such attestations may become valid in future and should be reconsidered then. When they receive attestations for blocks that they don't yet know about, clients will typically ask their peers to send the block to them directly.

No attestations for future blocks

```
# Attestations must not be for blocks in the future. If not, the attestation should not be considered assert store.blocks[attestation.data.beacon_block_root].slot <= attestation.data.slot
```

This check was introduced alongside the above checks for unknown blocks. Allowing votes for blocks that were published later than the attestation's assigned slot increases the feasibility of the decoy flip-flop attack by removing the need to have had a period of network asynchrony to set it up.

LMD and FFG vote consistency

```
# LMD vote must be consistent with FFG vote target
target_slot = compute_start_slot_at_epoch(target.epoch)
assert target.root == get_ancestor(store, attestation.data.beacon_block_root, target_slot)
```

This check ensures that the block in the attestation's head vote descends from the block in its target vote.

The check was introduced to fix three issues that had come to light.

1. Inconsistencies between the fork choice's validation of attestations and the state transition's validation of attestations. The issue is that, if some attestations are valid with respect to the fork choice but invalid for inclusion in blocks, it is a potential source of differing network views between validators, and could impede fork choice convergence. Validators receive attestations

both via attestation gossip and via blocks. Ideally, each of these channels will contain more or less the same information. 130

- 2. Attestations from incompatible forks. Since committee shufflings are decided only at the start of the previous epoch, it can lead to implementation challenges when processing attestations where the target block is from a different fork. After a while, forks end up with different shufflings. Clients often cache shufflings and it can be a source of bugs having to handle these edge cases. This check removes any ambiguity over the state to be used when validating attestations. It also prevents validators exploiting the ability to influence their own committee assignments in the event of multiple forks.
- 3. Faulty or malicious validators shouldn't be able to influence fork choice via exploiting this inconsistency. An attestation that fails this test would not have been produced by a correctly operating, honest validator. Therefore it is safest to ignore it.

Only future slots

```
# Attestations can only affect the fork choice of subsequent slots.
# Delay consideration in the fork choice until their slot is in the past.
assert get_current_slot(store) >= attestation.data.slot + 1
```

This criterion is discussed in section 8.4 of the Gasper paper: only attestations from slots up to and including slot N-1 may appear in the Store at slot N.

If attestations were included in the Store as soon as being received, an adversary with a number of dishonest validators could use that to probabilistically split the votes of honest validators. The dishonest validators would attest early in the slot, dividing their votes between competing head blocks. Due to network delays, when honest validators run their own fork choices prior to attesting at the proper time, they are likely to see different weights for each of the candidates, based on the subset of dishonest attestations they have received by then. In which case the vote of the honest validators could end up being split. This might keep the chain from converging on a single head block.

Introducing this one slot lag for considering attestations makes it much more likely that honest validators will all vote for the same head block in slot N, as they will have all seen a similar set of attestations up to slot N-1, and cannot be influenced by an adversary's early attestations in the current slot.

```
Used by on_attestation()
Uses validate_target_epoch_against_current_time(), compute_epoch_at_slot(), compute_start_slot_at_epoch(), get_ancestor() get_ancestor()
```

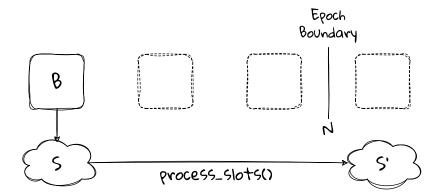
store target checkpoint state

```
def store_target_checkpoint_state(store: Store, target: Checkpoint) -> None:
    # Store target checkpoint state if not yet seen
    if target not in store.checkpoint_states:
        base_state = copy(store.block_states[target.root])
        if base_state.slot < compute_start_slot_at_epoch(target.epoch):
            process_slots(base_state, compute_start_slot_at_epoch(target.epoch))
        store.checkpoint_states[target] = base_state</pre>
```

We need checkpoint states both to provide validator balances (used for weighting votes in the fork choice) and for the validator shufflings (used when validating attestations).

A Checkpoint is a reference to the first slot of an epoch and are what the Casper FFG votes in attestations point to. When an attestation targets a checkpoint that has empty slots preceding it, the checkpoint's state will not match the state of the block that it points to. Therefore, we take that block's state (base_state) and run the simple process_slots() state transition for empty slots on it to bring the state up to date with the checkpoint.

¹³⁰One such inconsistency remains: attestations are valid in gossip for up to two epochs, but for only 32 slots in blocks.



Consider a checkpoint that points to [N, B], where N is the checkpoint height (epoch number) and B is the block root of the most recent block. The shapes with dotted outlines indicate skipped slots. The process_slots() function takes the state S associated with the block and updates it to the slot of the checkpoint by playing empty slots onto it, resulting in state S'.

```
Used by on_attestation()
Uses compute_start_slot_at_epoch(), process_slots(),
```

update_latest_messages

A message comprises a timestamp and a block root (head) vote. These are extracted from the containing attestation in the form of the epoch number of the target checkpoint of the attestation, and the LMD GHOST head block vote respectively. By the time we get here, validate_on_attestation() has already checked that the slot for which the head vote was made belongs to the epoch corresponding to the target vote. Validators vote exactly once per epoch, so the epoch number is granular enough for tracking their latest votes.

All the validators in attesting_indices made this same attestation. The attestation will have travelled the world as a single aggregate attestation, but it has been unpacked in on_attestation() before being passed to this function. Validators on our naughty list of equivocaters are filtered out, and any that are left are considered for updates.

If the validator index is not yet in the store.latest_messages set then its vote is inserted; if the vote that we have is newer than the vote already stored then it is updated. Each validator has at most one entry in the latest_messages set.

Used by	on_attestation()
See also	Attestation, LatestMessage

Handlers

The four handlers below - on_tick(), on_block(), on_attestation(), and on_attester_slashing() - are the fork choice rule's four senses. These are the means by which the fork choice gains its knowledge of the outside world, and the only means by which the Store gets updated.

None of the handlers is explicitly called by any code that appears anywhere in the spec. It is expected that client implementations will call each handler as and when required. As per the introductory material at the top of the fork choice spec, they should be called as follows.

- on tick(store, time) whenever time > store.time where time is the current Unix time.
- on block(store, block) whenever a block block is received.
- on_attestation(store, attestation) whenever an attestation attestation is received.
- on_attester_slashing(store, attester_slashing) whenever an attester slashing attester_slashing is received.

on_tick

```
def on_tick(store: Store, time: uint64) -> None:
    # If the ``store.time`` falls behind, while loop catches up slot by slot
    # to ensure that every previous slot is processed with ``on_tick_per_slot``
    tick_slot = (time - store.genesis_time) // SECONDS_PER_SLOT
    while get_current_slot(store) < tick_slot:
        previous_time = store.genesis_time + (get_current_slot(store) + 1) * SECONDS_PER_SLOT
        on_tick_per_slot(store, previous_time)
    on tick per slot(store, time)</pre>
```

A "tick" is not defined in the specification. Notionally, ticks are used to continually keep the fork choice's internal clock (store.time) updated. In practice, calling on_tick() is only really required at the start of a slot, at SECONDS_PER_SLOT / INTERVALS_PER_SLOT into a slot, and before proposing a block. However, on tick() processing is light and it can be convenient to call it more often.

The Teku client calls on_tick() regularly twice per second since it is used internally to drive other things beside the fork choice. In addition, Teku uses units of milliseconds rather than seconds for its tick interval, which is strictly speaking off-spec, but is necessary for supporting other chains such as the Gnosis Beacon Chain for which the SECONDS_PER_SLOT is not a multiple of INTERVALS_PER_SLOT.

The while loop was introduced in the Capella specification. It ensures that the processing in on_tick_per_slot() is done every slot. When multiple slots have passed since the last tick was processed, the loop calls on_tick_per_slot() for each of them so as to catch up. The only thing this makes a difference to is updating the checkpoints at epoch boundaries. Previously, if a tick was not processed during the first slot of an epoch, then the checkpoint update could be incorrectly skipped. Note that on_tick_per_slot() updates store.time, which in turn updates the output of get_current_slot(), so the loop will terminate.

I expect that the reason time is provided as a parameter rather than looked up via the machine's clock is that it simplifies testing.

```
Uses get_current_slot(), on_tick_per_slot()
See also SECONDS_PER_SLOT
```

on_block

```
assert get_current_slot(store) >= block.slot
# Check that block is later than the finalized epoch slot (optimization to reduce calls to
                                     \hookrightarrow get_ancestor)
finalized_slot = compute_start_slot_at_epoch(store.finalized_checkpoint.epoch)
assert block.slot > finalized_slot
# Check block is a descendant of the finalized block at the checkpoint finalized slot
assert get_ancestor(store, block.parent_root, finalized_slot) == store.finalized_checkpoint.root
# Check the block is valid and compute the post-state
state = pre_state.copy()
block_root = hash_tree_root(block)
state_transition(state, signed_block, True)
# Add new block to the store
store.blocks[block_root] = block
# Add new state for this block to the store
store.block_states[block_root] = state
# Add proposer score boost if the block is timely
time_into_slot = (store.time - store.genesis_time) % SECONDS_PER_SLOT
is_before_attesting_interval = time_into_slot < SECONDS_PER_SLOT // INTERVALS_PER_SLOT</pre>
if get_current_slot(store) == block.slot and is_before_attesting_interval:
    store.proposer_boost_root = hash_tree_root(block)
# Update checkpoints in store if necessary
update_checkpoints(store, state.current_justified_checkpoint, state.finalized_checkpoint)
# Eagerly compute unrealized justification and finality
compute_pulled_up_tip(store, block_root)
```

The on_block() handler should be called whenever a new signed beacon block is received. It does the following.

- Perform some validity checks:
- Update the store with the block and its associated beacon state.
- Handle proposer boost (block timeliness).
- Update the Store's justified and finalised checkpoints if permitted and required.

The on_block() handler does not call the on_attestation() handler for the attestations it contains, so clients need to do that separately for each attestation.

Validity checks

```
# Parent block must be known
assert block.parent_root in store.block_states
# Make a copy of the state to avoid mutability issues
pre_state = copy(store.block_states[block.parent_root])
# Blocks cannot be in the future. If they are, their consideration must be delayed until they are in
                                     \hookrightarrow the past.
assert get_current_slot(store) >= block.slot
# Check that block is later than the finalized epoch slot (optimization to reduce calls to
                                     \hookrightarrow get ancestor)
finalized_slot = compute_start_slot_at_epoch(store.finalized_checkpoint.epoch)
assert block.slot > finalized slot
# Check block is a descendant of the finalized block at the checkpoint finalized slot
assert get_ancestor(store, block.parent_root, finalized_slot) == store.finalized_checkpoint.root
# Check the block is valid and compute the post-state
state = pre_state.copy()
block_root = hash_tree_root(block)
state_transition(state, signed_block, True)
```

First we do some fairly self-explanatory checks. In order to be considered in the fork choice, the block must be joined to the block tree that we already have (that is, its parent must be in the Store), it must not be from a future slot according to our Store's clock, and it must be from a branch that descends from our finalised checkpoint. By the definition of finalised, all prior branches from the canonical chain are pruned away.

The final check is to run a full state transition on the block. This has two purposes, (1) it checks that the block is valid with respect to the consensus rules, and (2) it gives us the block's post-state which we need to add to the Store. We got the block's pre-state from its parent, which we know is already in the store. The True parameter to state_transition() ensures that the block's signature is checked, and that the result of applying the block to the state results in the same state root that the block claims it does (the "post-states" must match). Clients will be running this operation elsewhere when performing the state transition, so it is likely that the result of the state_transition() call will be cached somewhere in an optimal implementation.

Update the Store

```
# Add new block to the store
store.blocks[block_root] = block
# Add new state for this block to the store
store.block_states[block_root] = state
```

Once the block has passed the validity checks, it and its post-state can be added to the Store.

Handle proposer boost

```
# Add proposer score boost if the block is timely
time_into_slot = (store.time - store.genesis_time) % SECONDS_PER_SLOT
is_before_attesting_interval = time_into_slot < SECONDS_PER_SLOT // INTERVALS_PER_SLOT
if get_current_slot(store) == block.slot and is_before_attesting_interval:
    store.proposer_boost_root = hash_tree_root(block)</pre>
```

Proposer boost is a defence against balancing attacks on LMD GHOST. It rewards timely blocks with extra weight in the fork choice, making it unlikely that an honest proposer's block will become orphaned.

Here, in the on_block() handler, is where the block's timeliness is assessed and recorded. If the Store's time (as set by the on_tick() handler) is within the first third of the slot (1 / INTERVALS_PER_SLOT, that is, 4 seconds) when the block is processed, then we set store.proposer_boost_root to the block's root.

The store.proposer_boost_root field can only be set during the first four seconds of a slot, and it is cleared at the start of the next slot by the on_tick() handler. It is used in the get_weight() function to determine whether to add the extra proposer boost weight or not.

Note that, if there is a proposer equivocation in the slot, this code will apply proposer boost to the second block received rather than to the first block received. This becomes important for the security of third-party block production with MEV-Boost - it can allow a proposer to "steal" the transactions in a block builder's block (at the cost of getting slashed), which is deemed to be a Bad Thing. It would be better to apply the proposer boost only to the first block received, and a small patch to on_block() has been proposed to implement this.

Update justified and finalised

```
# Update checkpoints in store if necessary
update_checkpoints(store, state.current_justified_checkpoint, state.finalized_checkpoint)
# Eagerly compute unrealized justification and finality
compute_pulled_up_tip(store, block_root)
```

update_checkpoints() simply updates the Store's justified and finalised checkpoints if those in the block's post-state are better (that is, higher, more recent). The Store always tracks the best known justified and finalised checkpoints that it is able to validate.

compute_pulled_up_tip() runs the epoch transition Casper FFG accounting on the block – notionally "pulling it up" from its current slot to the first slot of the next epoch – to see if it has achieved unrealised justification. The block's unrealised justification will be stored for later use by filter_block_tree(), and the Store's unrealised justification and unrealised finalisation trackers may be updated. If the block is from a previous epoch, then the unrealised checkpoints become realised, and update_checkpoints() will be called again, potentially over-writing the update we just made in the line above.

```
Uses get_current_slot(), compute_start_slot_at_epoch(), get_ancestor(), hash_tree_root(), state_transition(), update_checkpoints(), compute_pulled_up_tip()

See also INTERVALS_PER_SLOT
```

on attestation

Attestations may be useful no matter how we heard about them: they might have been contained in a block, or been received individually via gossip, or via a carrier pigeon¹³¹.

If the attestation was unpacked from a block then the flag is_from_block should be set to True. This causes the timeliness check in validate_on_attestation() to be skipped: attestations not from blocks must be received in the epoch they were produced in, or the next epoch, in order to influence the fork choice. (So, a carrier pigeon would need to be fairly swift.)

The validate_on_attestation() function performs a comprehensive set of validity checks on the attestation to defend against various attacks.

Assuming that the attestation passes the checks, we add its target checkpoint state to the Store for later use, as well as using it immediately. The store_target_checkpoint_state() function is idempotent, so nothing happens if the state is already present.

Having the target checkpoint state, we can use it to look up the correct shuffling for the validators. With the shuffling in hand, calling get_indexed_attestation() turns the Attestation object (containing a bitlist) into an IndexedAttestation object (containing a list of validator indices).

Finally, we can validate the indexed attestation with is_valid_indexed_attestation(), which amounts to checking its aggregate BLS signature against the set of public keys of this indexed validators. Checking the signatures is relatively expensive compared with the other checks, which is one reason for deferring it to last (we also don't want to be checking them against an inconsistent target).

If, and only if, everything has succeeded, we call update_latest_messages() to refresh the Store's list of latest messages for the validators that participated in this vote.

¹³¹This would change were we to adopt view-merge. Only attestations that had been processed by specifically designated aggregators would be considered in the fork choice.

```
Uses validate_on_attestation(), store_target_checkpoint_state(), get_indexed_attestation(), is_valid_indexed_attestation(), update_latest_messages()
```

on_attester_slashing

Note: on_attester_slashing should be called while syncing and a client MUST maintain the equivocation set of AttesterSlashings from at least the latest finalized checkpoint.

```
def on_attester_slashing(store: Store, attester_slashing: AttesterSlashing) -> None:
    """
    Run ``on_attester_slashing`` immediately upon receiving a new ``AttesterSlashing``
    from either within a block or directly on the wire.
    """
    attestation_1 = attester_slashing.attestation_1
    attestation_2 = attester_slashing.attestation_2
    assert is_slashable_attestation_data(attestation_1.data, attestation_2.data)
    state = store.block_states[store.justified_checkpoint.root]
    assert is_valid_indexed_attestation(state, attestation_1)
    assert is_valid_indexed_attestation(state, attestation_2)

indices = set(attestation_1.attesting_indices).intersection(attestation_2.attesting_indices)
    for index in indices:
        store.equivocating indices.add(index)
```

The on_attester_slashing() handler was added to defend against the equivocation balancing attack (described more formally in Two Attacks On Proof-of-Stake GHOST/Ethereum). The attack relies on the adversary's validators equivocating about their attestations – that is, publishing multiple different attestations per epoch – and is not solved by proposer score boosting.

Of course, the equivocating attestations are slashable under the Casper FFG commandments. When the attack finally ends, those validators will be punished and ejected from the validator set. Meanwhile, however, since the fork choice calculations are based on the validator set at the last justified epoch, the adversary's validators could keep the attack going indefinitely.

Rather than add a lot of apparatus within the fork choice to track and detect conflicting attestations, the mechanism relies on third-party slashing claims received via blocks or directly from peers as attester slashing messages. The validity checks are identical to those in the state-transition's process_attester_slashing() method, including the use of is_slashable_attestation_data(). This is broader that we need for our purposes here as it will exclude validators that make surround votes as well as validators that equivocate. But excluding all misbehaving validators is probably a good idea.

Any validators proven to have made conflicting attestations are added to the store.equivocating_indices set ¹³². They will no longer be involved in calculating the weight of branches, and their future attestations will be ignored in the fork choice. We are permitted to clear any equivocating attestation information from before the last finalised checkpoint, but those validators would have been slashed by the state-transition by then, so this ban is permanent.

```
Uses is_slashable_attestation_data(), is_valid_indexed_attestation()
See also AttesterSlashing, process_attester_slashing()
```

Bellatrix Fork Choice

Introduction

This section covers the additional Bellatrix fork choice document, v1.3.0. For a complementary take, see Vitalik's annotated Bellatrix fork choice (based on a slightly older version).

¹³²store.equivocating_indices is a Python Set. Adding an existing element again is a no-op, so it cannot grow without bounds

As usual, text with a side bar is quoted directly from the specification.

This is the modification of the fork choice according to the executable beacon chain proposal.

Note: It introduces the process of transition from the last PoW block to the first PoS block.

The "executable beacon chain proposal" is what became known as The Merge, and is specified by EIP-3675 together with the Bellatrix upgrade on the beacon chain.

Upgrades to Ethereum's protocol are normally planned to take place at pre-determined block heights. For security reasons, the Merge upgrade used a different trigger, specifically a terminal total difficulty of proof of work mining. The first proof of work block to reach that amount of accumulated difficulty became the last proof of work block: all subsequent execution blocks are now merged into the proof of stake beacon chain as execution payloads.

The only functional change to the fork choice that the Bellatrix upgrade introduced was about ensuring that a valid terminal proof of work block was picked up by the beacon chain at the point of the Merge. As such, this section is largely of only historical interest now.

The remainder of the material in this section (mostly Engine API related) isn't really relevant to the fork choice rule at all. It mainly describes one-way communication of fork choice decisions to the execution layer. Altogether, it's a bit of a weird collection of stuff, for want of a better place to put it I suppose.

Custom types

Name	SSZ equivalent	Description
PayloadId	Bytes8	Identifier of a payload building process

PayloadId is used to keep track of stateful requests from the consensus client to the execution client. Specifically, the consensus client can ask the execution client to start creating a new execution payload via the notify_forkchoice_updated() command (which maps to the engine_forkchoiceUpdatedV1 RPC method in the Engine API docs). The execution client will return a PayloadId reference and continue to build the payload asynchronously. Later, the consensus client can obtain the payload with a call to the engine API's engine_getPayloadV1 method by passing it the same PayloadId.

Protocols

ExecutionEngine

 $\it Note:$ The notify_forkchoice_updated function is added to the ExecutionEngine protocol to signal the fork choice updates.

The body of this function is implementation dependent. The Engine API may be used to implement it with an external execution engine.

Post-Merge, every consensus client (beacon chain client) must be paired up with an execution client (ExecutionEngine; formerly, Eth1 client). The execution client has several roles.

- 1. It validates execution payloads.
- 2. It executes execution payloads in order to maintain Ethereum's state (accounts, contracts, balances, receipts, etc.).
- 3. It provides data to applications via its RPC API.
- 4. It maintains a mempool of transactions from which it builds execution payloads and provides them to the consensus layer for distribution.

The first and the last of these are the ones that interest us on the consensus side. The first role is important because beacon blocks are valid only if they contain valid execution payloads. The last is

 $^{^{133}}$ This name comes from Mikhail Kalinin's original article on Ethresear.ch.

important because the consensus side does not directly handle ordinary Ethereum transactions and cannot build its own execution payloads.

The interface between the two sides is called the Engine API. The Engine API is the RPC (remote procedure call) interface that the execution client provides to its companion consensus client. It is one-way in the sense that the consensus client can call methods on the Engine API, but the execution client does not call any methods on the consensus client.

The most interesting methods that the Engine API provides are these three.

• engine_newPayloadV1

- When the consensus client receives a new beacon block, it extracts the block's execution payload and uses this method to send it to the execution client. The execution client will validate the payload and execute the transactions it contains. The method's return value indicates whether the payload was valid or not.

• engine forkchoiceUpdatedV1

The function below, notify_forkchoice_updated(), uses this method for two purposes. First, it is used routinely to update the execution client with the latest consensus information: head block, safe head block, and finalised block. Second, it can be used to prompt the execution client to begin building an execution payload from its mempool. The consensus client will do this when it is about to propose a beacon block.

• engine_getPayloadV1

This is used to retrieve an execution payload previously requested via engine_forkchoiceUpdatedV1, using a PayloadId as a reference.

notify forkchoice updated

This function performs three actions atomically:

- Re-organizes the execution payload chain and corresponding state to make head_block_hash the
 head.
- Updates safe block hash with the value provided by safe_block_hash parameter.
- Applies finality to the execution state: it irreversibly persists the chain of all execution payloads and corresponding state, up to and including finalized_block_hash.

Additionally, if payload_attributes is provided, this function sets in motion a payload build process on top of head_block_hash and returns an identifier of initiated process.

This is a wrapper around the Engine API's engine_forkchoiceUpdatedV1 RPC method as described above. We use it to keep the execution client up to date with the latest fork choice information, and (optionally) from time to time to request it to build a new execution payload for us.

Note: The (head_block_hash, finalized_block_hash) values of the notify_forkchoice_updated function call maps on the POS_FORKCHOICE_UPDATED event defined in the EIP-3675. As per EIP-3675, before a post-transition block is finalized, notify_forkchoice_updated MUST be called with finalized_block_hash = Hash32().

EIP-3675 is the specification of the Merge on the execution layer side (Eth1 side) of things. The POS_FORKCHOICE_UPDATED event described there is triggered by the consensus layer calling the Engine API's engine_forkchoiceUpdatedV1 method, which is in turn triggered by the consensus client calling notify_forkchoice_updated(). The consensus client will do this periodically, in particular whenever a reorg

occurs on the beacon chain so that applications built on the execution layer can know which state is current.

Between the Merge and the first finalised epoch after the Merge there was no guarantee of finality on the execution chain, therefore we could not sent it a finalised block hash and had to use the placeholder default value instead.

Note: Client software MUST NOT call this function until the transition conditions are met on the PoW network, i.e. there exists a block for which is_valid_terminal_pow_block function returns True.

The proof of work chain was not interested in the proof of stake chain's view of the world until after the Merge.

Note: Client software MUST call this function to initiate the payload build process to produce the merge transition block; the head_block_hash parameter MUST be set to the hash of a terminal PoW block in this case.

The first beacon chain proposer after the terminal proof of work block had been detected would call notify_forkchoice_updated() with the payload_attributes parameter in order to request an execution payload to be build for the first merged block.

If there had been multiple candidate terminal PoW blocks (as there were for the Goerli testnet Merge), the beacon block proposer would have been free to choose which of them to ask its execution client to build on.

safe block hash

The safe_block_hash parameter MUST be set to return value of get_safe_execution_payload_hash(store: Store) function.

The "safe block" feature is a way for the consensus protocol to signal to the execution layer that a block is very unlikely ever to be reverted. Application developers could use the safe block information to provide better user experience to their users in the form of a pseudo fast-finality. See the later Safe Block section for more on this.

Helpers

PayloadAttributes

Used to signal to initiate the payload build process via notify_forkchoice_updated.

```
@dataclass
class PayloadAttributes(object):
    timestamp: uint64
    prev_randao: Bytes32
    suggested_fee_recipient: ExecutionAddress
    withdrawals: Sequence[Withdrawal] # [New in Capella]
```

This class maps onto the Engine API's PayloadAttributesV2 class and is used when asking the execution client to start building an execution payload.

The prev_randao field is the beacon state's current RANDAO value, having been updated by the RANDAO reveal in the previous beacon block. It is made available to execution layer applications via the EVM's new PREVRANDAO opcode.

suggested_fee_recipient is the Ethereum account that any fee income from transaction tips should be sent to when the payload is executed (formerly known as the COINBASE). The execution client may override this if it has its own setting for fee recipient, hence "suggested". But allowing it to be set via the Engine API makes it possible for a beacon node hosting multiple validators to use a different fee recipient address for each validator, whereas setting it on the execution side would force them all to use the same fee recipient address.

The withdrawals field was added in the Capella upgrade. It allows the consensus layer to pass a list of withdrawals to the execution layer to include in an execution payload. There will be at most

MAX_WITHDRAWALS_PER_PAYLOAD of them. When the block containing the payload is processed, for each withdrawal, the amount will be deducted from validator's balance on the beacon chain, and will be added to the balance of the Ethereum account in the Withdrawal object's ExecutionAddress field. The ExecutionAddress is derived from the validator's withdrawal credentials.

PowBlock

```
class PowBlock(Container):
   block_hash: Hash32
   parent_hash: Hash32
   total_difficulty: uint256
```

This class is just a succinct way to wrap up the information we need for checking proof of work blocks around the Merge. It is returned by get_pow_block() and consumed by is_valid_terminal_pow_block().

get_pow_block

Let get_pow_block(block_hash: Hash32) -> Optional[PowBlock] be the function that given the hash of the PoW block returns its data. It may result in None if the requested block is not yet available.

Note: The eth_getBlockByHash JSON-RPC method may be used to pull this information from an execution client.

As noted, <code>get_pow_block()</code> is a wrapper around Ethereum's <code>eth_getBlockByHash</code> JSON-RPC method. Given a block hash (not its hash tree root! - Eth1 blocks are encoded with RLP rather than SSZ), it returns the information in the <code>PowBlock</code> structure.

eth_getBlockByHash is a standard Eth1 client RPC method rather than a specific Engine API method. For convenience, execution clients often provide access to this method via the Engine API port in addition to the standard RPC API port so that consensus clients can be configured to connect to only one port on the execution client.

is_valid_terminal_pow_block

Used by fork-choice handler, on block.

```
def is_valid_terminal_pow_block(block: PowBlock, parent: PowBlock) -> bool:
    is_total_difficulty_reached = block.total_difficulty >= TERMINAL_TOTAL_DIFFICULTY
    is_parent_total_difficulty_valid = parent.total_difficulty < TERMINAL_TOTAL_DIFFICULTY
    return is_total_difficulty_reached and is_parent_total_difficulty_valid</pre>
```

Given two PowBlock objects (corresponding to a proof of work block and its parent proof of work block respectively), this function checks whether the block meets the criteria for being the terminal proof of work block. That is, that its total difficulty exceeds the terminal total difficulty and that its parent's total difficulty does not.

validate_merge_block

```
def validate_merge_block(block: BeaconBlock) -> None:
    """
    Check the parent PoW block of execution payload is a valid terminal PoW block.

Note: Unavailable PoW block(s) may later become available,
    and a client software MAY delay a call to ``validate_merge_block``
    until the PoW block(s) become available.
    """

if TERMINAL_BLOCK_HASH != Hash32():
    # If `TERMINAL_BLOCK_HASH` is used as an override, the activation epoch must be reached.
    assert compute_epoch_at_slot(block.slot) >= TERMINAL_BLOCK_HASH_ACTIVATION_EPOCH
    assert block.body.execution_payload.parent_hash == TERMINAL_BLOCK_HASH
    return

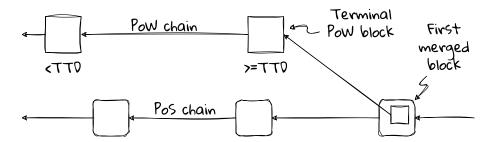
pow_block = get_pow_block(block.body.execution_payload.parent_hash)
```

```
# Check if `pow_block` is available
assert pow_block is not None
pow_parent = get_pow_block(pow_block.parent_hash)
# Check if `pow_parent` is available
assert pow_parent is not None
# Check if `pow_block` is a valid terminal PoW block
assert is_valid_terminal_pow_block(pow_block, pow_parent)
```

This is used by the Bellatrix on_block() handler. The block parameter is a beacon block that claims to be the first merged block. That is, it is the first beacon block (on the current branch) to contain a non-default ExecutionPayload.

The TERMINAL_BLOCK_HASH is a parameter that client operators could have agreed to use to override the terminal total difficulty mechanism if necessary. For example, if the Merge had resulted in beacon chain forks they could have been resolved by manually agreeing an Eth1 Merge block and setting TERMINAL_BLOCK_HASH to its value via client command line parameters. In the event, this was not needed and TERMINAL BLOCK HASH remains at its default value of Hash32().

The remainder of the function checks, (a) that the PoW block that's the parent of the execution payload exists, and has total difficulty greater than the TERMINAL_TOTAL_DIFFICULTY, and (b) that the parent of that block exists and has a total difficulty less than the TERMINAL_TOTAL_DIFFICULTY. (The difficulty checks are performed in is_valid_terminal_pow_block().)



The first beacon chain merged block contains the execution payload whose parent PoW block was the terminal PoW block. The terminal PoW block is the first PoW block to have a total difficulty exceeding the TERMINAL_TOTAL_DIFFICULTY.

The parent and grandparent PoW blocks are retrieved via the <code>get_pow_block()</code> function, which in practice involves making RPC calls to the attached Eth1/execution client. If either of these calls fails, an <code>assert</code> will be triggered, and the <code>on_block()</code> handler will bail out without making any changes.

Updated fork-choice handlers

on_block

Note: The only modification is the addition of the verification of transition block conditions.

```
def on_block(store: Store, signed_block: SignedBeaconBlock) -> None:
    """
    Run ``on_block`` upon receiving a new block.

A block that is asserted as invalid due to unavailable PoW block may be valid at a later time, consider scheduling it for later processing in such case.
    """
    block = signed_block.message
    # Parent block must be known
    assert block.parent_root in store.block_states
# Make a copy of the state to avoid mutability issues
    pre_state = copy(store.block_states[block.parent_root])
```

```
# Blocks cannot be in the future. If they are, their consideration must be delayed until they are in
                                     \hookrightarrow the past.
assert get current slot(store) >= block.slot
# Check that block is later than the finalized epoch slot (optimization to reduce calls to
                                     \hookrightarrow get_ancestor)
finalized_slot = compute_start_slot_at_epoch(store.finalized_checkpoint.epoch)
assert block.slot > finalized_slot
# Check block is a descendant of the finalized block at the checkpoint finalized slot
assert get_ancestor(store, block.parent_root, finalized_slot) == store.finalized_checkpoint.root
# Check the block is valid and compute the post-state
state = pre state.copy()
block root = hash tree root(block)
state_transition(state, signed_block, True)
# [New in Bellatrix]
if is_merge_transition_block(pre_state, block.body):
    validate_merge_block(block)
# Add new block to the store
store.blocks[block_root] = block
# Add new state for this block to the store
store.block_states[block_root] = state
# Add proposer score boost if the block is timely
time_into_slot = (store.time - store.genesis_time) % SECONDS_PER_SLOT
is_before_attesting_interval = time_into_slot < SECONDS_PER_SLOT // INTERVALS_PER_SLOT</pre>
if get_current_slot(store) == block.slot and is_before_attesting_interval:
    store.proposer_boost_root = hash_tree_root(block)
# Update checkpoints in store if necessary
update\_checkpoints(store, \ state.current\_justified\_checkpoint, \ state.finalized\_checkpoint)
# Eagerly compute unrealized justification and finality.
compute_pulled_up_tip(store, block_root)
```

As noted, the only addition here to the normal on_block() handler is the lines,

```
# [New in Bellatrix]
if is_merge_transition_block(pre_state, block.body):
    validate_merge_block(block)
```

The is_merge_transition_block() function will return True when the given block is the first beacon block that contains an execution payload, and False otherwise.

To ensure consistency between the execution chain and the beacon chain at the Merge, this first merged beacon block requires some extra processing. We must check that the PoW block its execution payload is derived from has indeed met the criteria for the merge. Essentially, its total difficulty must exceed the terminal total difficulty and its parent's total difficulty must not. If this test fails then something has gone wrong and the beacon block must be excluded from the fork choice.

There might be several candidate execution blocks that meet this criterion in the event of PoW forks at the point of the Merge – this occurred when merging one of the testnets¹³⁴ – but that's fine. The proposer of the first merged beacon block¹³⁵ that becomes canonical gets to decide which terminal execution block wins.

¹³⁴And triggered an issue with some client implementations.

 $^{^{135}}$ For the record, the first merged beacon block on mainnet was at slot 4700013.

Safe Block

Introduction

The Fork Choice Safe Block spec is not really part of the beacon chain's fork choice and is located in a different document in the consensus repo. It is an heuristic for using the fork choice's Store data to identify a block that will not be reverted, under some reasonable assumptions. It could be used, for example, by applications to implement a settlement period for transactions. There is an analogy with the assumption that, under proof of work, in the absence of a 51% attack, a block becomes safe from reorgs after a certain number of blocks (say, fifteen) have been built on top of it.

Under honest majority and certain network synchronicity assumptions there exist a block that is safe from re-orgs. Normally this block is pretty close to the head of canonical chain which makes it valuable to expose a safe block to users.

This section describes an algorithm to find a safe block.

Of course, the ultimate safe block is the last finalised checkpoint. But that could be several minutes in the past, even under ideal network conditions. If we assume (a) that there is an honest majority of validators, and (b) that their messages are received in a timely fashion, then we can in principle identify a more recent block that will not be at risk of reversion.

get_safe_beacon_block_root

```
def get_safe_beacon_block_root(store: Store) -> Root:
    # Use most recent justified block as a stopgap
    return store.justified_checkpoint.root
```

Note: Currently safe block algorithm simply returns store.justified_checkpoint.root and is meant to be improved in the future.

Returning the justified checkpoint is certainly safe under the assumptions above, but we can almost certainly do better. Substantial progress has been made recently towards providing a more useful safe block. There's more on this in the Confirmation rule section of the Consensus chapter.

get_safe_execution_payload_hash

```
def get_safe_execution_payload_hash(store: Store) -> Hash32:
    safe_block_root = get_safe_beacon_block_root(store)
    safe_block = store.blocks[safe_block_root]

# Return Hash32() if no payload is yet justified
    if compute_epoch_at_slot(safe_block.slot) >= BELLATRIX_FORK_EPOCH:
        return safe_block.body.execution_payload.block_hash
    else:
        return Hash32()
```

Note: This helper uses beacon block container extended in Bellatrix.

Bellatrix was the pre-Merge upgrade that added the execution payload hash to be acon blocks in readiness for the Merge itself. Applications on Ethereum are largely unaware of the beacon chain and will use the execution payload hash rather than the beacon block root as their reference point in the Eth1 blockchain.

Part 4: Upgrades

Hard forks

TODO

Fork Digest

Upgrade History

Introduction

Through an open process in February 2021 we decided that beacon chain (consensus layer) upgrades would be named after stars. We're taking them in English alphabetical order, with the first being Altair. The genesis configuration remains Phase 0 due to its origin in the now defunct three-phase plan for delivering Ethereum 2.0.

A summary of upgrades to date is below, with more detailed descriptions in the following sections.

Name	Epoch	Date (UTC)	Comments	Spec tag	Release name
Phase 0	0	2020-12-01 12:00:23	The genesis configuration	v1.0.0	Cosmic Egg
Altair	74240	2021-10-27 10:56:23	Sync committees and economic reforms	v1.1.0	The Great Machine
Bellatrix	144896	2022-09-06 11:34:47	Merge- readiness upgrade	v1.2.0	Ailuropoda melanoleuca ¹³⁶
Capella	194048	2023-04-12 22:27:35	Withdrawals enabled	v1.3.0	${\rm Gamlum^{137}}$
Deneb	TBD	TBD	EIP-4844 data availability	TBD	TBD
Electra	TBD	TBD	TBD	TBD	TBD

The Merge was a special kind of upgrade in that it was not a manual hard fork. The protocol changes required to support the Merge were done in the Bellatrix upgrade. The Merge itself happened nine days later without any further intervention, simultaneously with the execution layer's Paris upgrade.

The consensus layer specifications are written incrementally. Thus, each version (such as the current Bellatrix v1.3.0 version) contains the unchanged specs for previous versions, plus a separate set of documents detailing the changes for the new version. Thus, to build Bellatrix, for example, you need the Phase 0 specs, the Altair "diff" specs on top of that, and the Bellatrix "diff" specs on top of that, all with the same GitHub release tag (in this case, v1.3.0).

The consensus specs repo contains some other, unreleased, versions such as das (data-availability sampling), custody_game, and sharding. These reflect different research directions and are in varying states of currency.

Upgrade timing

Under proof of work, upgrades (with the exception of the Merge) were performed at block heights that had been chosen several weeks in advance. Due to changes in hash power, predicting their timing was difficult - they could occur several hours, or even a day or two, adrift from their target time.

Under proof of stake, we have the luxury of being able to time network upgrades to the second. Nevertheless, we aim to do upgrades on 256-epoch boundaries. These boundaries correspond both to the batching interval of block and state roots (SLOTS_PER_HISTORICAL_ROOT slots), and the sync committee period (EPOCHS_PER_SYNC_COMMITTEE_PERIOD epochs). Having the protocol not change in the middle of these periods will make it easier to verify proofs using their data later.

A period of 256 epochs is around 27 hours, so we get about one opportunity per day to perform an upgrade.

¹³⁶Ailuropoda melanoleuca is the formal name of the giant panda.

¹³⁷Gamlum may have been a goat-related ancient name for Capella.

Phase 0

For historical reasons, the initial configuration of the beacon chain at its genesis was called Phase 0.

Beacon chain genesis took place at 12:00:23 UTC on the 1st of December 2020. The extra 23 seconds comes from the timestamp of the first Eth1 block to meet the genesis criteria, block 11320899. It is a little remnant of proof of work forever embedded in the beacon chain's history.

```
\begin{array}{ll} \texttt{MIN\_GENESIS\_TIME} & \texttt{uint64(1606824000)} \ (\mathrm{Dec} \ 1, \ 2020, \ 12\mathrm{pm} \ \mathrm{UTC}) \\ \\ \texttt{GENESIS\_FORK\_VERSION} & \texttt{Version('0x000000000')} \end{array}
```

See the Phase 0 specs for the full description. These specs still apply to the beacon chain today, except where they were superseded by the Altair, Bellatrix, or later upgrades.

My Phase 0 annotated specification remains available.

Altair

The Altair upgrade took place at 10:56:23 UTC on October the 27th, 2021.

The main goals of the Altair upgrade were to

- 1. introduce sync committees for supporting light clients,
- 2. significantly rework the beacon chain reward and penalty accounting, and
- 3. begin increasing some penalty parameters towards their final values.

The following changes were made for sync committee support.

- New cryptographic domains for the sync committee functions.
- New data structures to support sync committees. Namely, SyncAggregate and SyncCommittee.
- Functions for managing sync committees:

```
- get_next_sync_committee_indices();
```

- get_next_sync_committee();
- process_sync_aggregate(), which takes care of reward and penalty accounting for sync committee participation; and
- process_sync_committee_updates().
- Gossip topics were added to the P2P specification to support sync committee activity

The reforms to the accounting were extensive, and I won't list them all here as they are thoroughly covered elsewhere in the annotated spec and book. But in summary,

- There was a move away from doing all the accounting for attestation inclusion at epoch boundaries to performing much of the work on an ongoing basis during epochs. The epoch transition is quite heavy in any case; this spreads the workload and is simpler overall.
- Incentives were tweaked for different behaviours, such as late attestations and block proposal rewards. We also took the opportunity to simplify the rewards and penalties calculations.
- The inactivity leak was changed so that it is now applied on a per-validator basis rather than globally.

As for the penalty parameters, the following parameters were updated. These had been softened at genesis as we got used to running the beacon chain:

• INACTIVITY_PENALTY_QUOTIENT decreased from 2^{26} to 3×2^{24} . This reduces stakes more quickly during an inactivity leak.

- MIN_SLASHING_PENALTY_QUOTIENT decreased from 128 to 64. This sets the initial slashing penalty to 0.5 ETH for a validator with a full stake rather than the 0.25 ETH of Phase 0.
- PROPORTIONAL_SLASHING_MULTIPLIER increased from 1 to 2 so that, in the event of over one-third of validators being slashed together, the full penalty would be the removal of two-thirds of their stakes rather than the one-third of Phase 0.

The full description of the changes between Phase 0 and Altair is in the Altair specs.

My Altair annotated specification remains available.

Bellatrix

The Bellatrix upgrade took place at 11:34:47 UTC on September the 6th, 2022.

BELLATRIX_FORK_VERSION	Version('0x02000000')
BELLATRIX_FORK_EPOCH	Epoch(144896) (Sept 6 , 2022 , $11:34:47am\ UTC$)

The primary goal of Bellatrix was to ready the beacon chain for the Merge that took place nine days later. It included the following elements.

- Data structures for holding execution payloads were added, namely ExecutionPayload and ExecutionPayloadHeader.
- The processing of execution payloads was added to block processing.
- The fork choice was updated to recognise the transition from proof of work to proof of stake on the beacon chain side.
- The maximum size of gossip messages and Req/Resp chunks was increased in the P2P spec to allow for the extra size of beacon blocks due to the execution payload. Also, the validity rules for gossiped blocks were updated.

In addition, continuing the changes from Altair, some penalty parameters were updated to their final values. These had been softened for the pre-Merge releases as we got used to running the beacon chain:

- INACTIVITY_PENALTY_QUOTIENT decreased from 3×2^{24} to 2^{24} . This reduces stakes more quickly during an inactivity leak.
- MIN_SLASHING_PENALTY_QUOTIENT decreased from 64 to 32. This sets the initial slashing penalty to 1 ETH for a validator with a full stake rather than 0.5 ETH.
- PROPORTIONAL_SLASHING_MULTIPLIER increased from 2 to 3 so that, in the event of over one-third of validators being slashed together, the full penalty would be the removal of their entire stakes.

The full description of the changes between Altair and Bellatrix is in the Bellatrix specs.

My Bellatrix annotated specification remains available.

Capella

The Capella upgrade took place at 22:27:35 UTC on April the 12th, 2023.

Capella included the following updates:

- it enabled automatic withdrawals from the beacon chain to Eth1 accounts;
- it provided a way for stakers to make a one-time change from BLS-style withdrawal credentials to Eth1-style withdrawal credentials;
- the way historical roots are stored in the beacon state was modified; and,
- there was a big refactor of the fork choice rule specification, along with some behavioural changes.

By finally enabling withdrawals, Capella in some sense completed The Merge, fulfilling the promise to stakers made 2.5 years earlier that they would eventually be able to claim their rewards and reclaim their stakes.

Two withdrawal mechanisms were implemented.

- 1. Exited and withdrawable validators have their full balances automatically transferred to their withdrawal addresses.
- 2. Excess balances from active validators are regularly swept into their withdrawal addresses.

The consensus layer's Capella upgrade took place at the same time as the execution layer's Shanghai upgrade.

The full description of the changes between Bellatrix and Capella is in the Capella specs.

Deneb

The consensus layer upgrade following Capella has been given the name Deneb and will take place simultaneously with the execution layer's Cancun upgrade.

The main work included in Deneb will be the work needed for the consensus layer to support EIP-4844 data availability.

The following changes are also planned for inclusion.

- EIP-7044: Lock voluntary exit domain on Capella #3288
- EIP-7045: Increase max attestation inclusion slot #3360
- EIP-4788: Expose parent beacon block root in execution layer #3421
- EIP-7514: Add Max Epoch Churn Limit #3499
- Apply proposer boost to first block in case of equivocation #3352

Electra

The consensus layer upgrade following Deneb has been given the name Electra and will take place simultaneously with the execution layer's Prague upgrade.

An early stage discussion around the potential scope of the Electra upgrade is taking place in Issue 3449 on the consensus specs repo.

The Merge

TODO

History

TODO

Testing the Merge

TODO

Architecture

TODO

Transition

TODO

Engine API

TODO

 ${\bf Optimistic\ sync}$

Part 5: Future

Introduction

${\bf With drawals}$

Data Availability Sampling

TODO

Proto-Danksharding

TODO

Full Danksharding

Distributed Validator Technology

Introduction

TODO

Multi-party Compute

TODO

Consensus

Light Clients

Introduction

TODO

Syncing

TODO

Protocol

Active Research Topics

Introduction

TODO

Proofs of Custody

TODO

Builder / proposer split

TODO

Consensus changes

TODO

Single slot finality

TODO

References:

- Paths toward single-slot finality
- A simple Single Slot Finality protocol

Verkle trees

TODO

Statelessness

TODO

Single Secret Leader Election

TODO

Verifiable Delay Function

TODO

Post-quantum crypto

TODO

S[NT]ARK-friendly state transitions

Appendices

Staking

Introduction

TODO

Ways to Stake

TODO

Client Diversity

TODO

 $\mathbf{F}\mathbf{A}\mathbf{Q}$

How to become a core dev

So you wanna be a core dev?

TODO

Resources

Reference

TODO

Running the spec

Introduction

Being written in Python, the spec itself is executable. This is wonderful for generating test cases and there is a whole infrastructure in the specs repo for doing just that.

We can also run the spec ourselves to do interesting things. In this exercise we will calculate the minimum and maximum sizes of the various containers defined by the spec. The following code is from Protolambda, lightly modified to simplify and update it.

```
from inspect import getmembers, isclass
from eth2spec.utils.ssz.ssz_typing import Container
from eth2spec.capella import mainnet
def get_spec_ssz_types():
    return [
        value for (_, value) in getmembers(mainnet, isclass)
        if issubclass(value, Container) and value != Container # only the subclasses, not the imported
                                         \hookrightarrow base class
    ]
type_bounds = {
    value. name : ({
        'size': value.type byte length()
    } if value.is_fixed_byte_length() else {
        'min_size': value.min_byte_length(),
        'max_size': value.max_byte_length(),
    }) for value in get_spec_ssz_types()
}
import json
print(json.dumps(type_bounds))
```

Set up

We have a few hoops to jump through to get things installed for the first time. The below works well for me on Linux, but I haven't tested extensive variations. Just use the commands prefixed with >. I've included some output so that you can check whether things are on the right lines.

First, set up a Python virtual environment.

```
> git clone https://github.com/ethereum/consensus-specs.git
Cloning into 'consensus-specs'...
...
> cd consensus-specs/
> python3 -m venv .
> source bin/activate
(consensus-specs) > python --version
Python 3.10.6
```

Now we install and build all the dependencies required for the actual specs.

```
(consensus-specs) > python setup.py install
... tons of output ...
(consensus-specs) > make install_test
... lots more output ...
(consensus-specs) > python setup.py pyspecdev
running pyspecdev
running build_py command
running pyspec
```

. . .

Run

Finally, we can simply run the Python script from above. Copy it into a file called sizes.py and run it as follows.

```
(consensus-specs) > python sizes.py | jq
{
   "AggregateAndProof": {
     "min_size": 337,
     "max_size": 593
},
```

The pipe to jq is optional, you will just get less pretty output without it.

Full output

Values are bytes. Don't be alarmed that the maximum size of BeaconState turns out to be 139 TiB, or that BeaconBlockBody can be enormous. These sizes are based on the notional maximum SSZ list lengths they contain, and are not realistic in practice.

```
"AggregateAndProof": {
  "min_size": 337,
  "max_size": 593
},
"Attestation": {
  "min size": 229,
  "max size": 485
},
"AttestationData": {
  "size": 128
"AttesterSlashing": {
  "min_size": 464,
  "max_size": 33232
},
"BLSToExecutionChange": {
  "size": 76
"BeaconBlock": {
  "min_size": 984,
  "max_size": 1125899911198752
"BeaconBlockBody": {
  "min_size": 900,
  "max_size": 1125899911198668
"BeaconBlockHeader": {
  "size": 112
"BeaconState": {
  "min_size": 2737221,
  "max_size": 152833729758309
"Checkpoint": {
  "size": 40
"ContributionAndProof": {
  "size": 264
"Deposit": {
```

```
"size": 1240
},
"DepositData": {
 "size": 184
},
"DepositMessage": {
 "size": 88
},
"Eth1Block": {
  "size": 48
},
"Eth1Data": {
 "size": 72
"ExecutionPayload": {
 "min_size": 512,
  "max_size": 1125899911038176
\verb"ExecutionPayloadHeader": \{
 "min_size": 568,
  "max_size": 600
},
"Fork": {
  "size": 16
},
"ForkData": {
  "size": 36
"HistoricalBatch": {
  "size": 524288
},
"HistoricalSummary": {
  "size": 64
"IndexedAttestation": {
 "min_size": 228,
 "max_size": 16612
"LightClientBootstrap": {
 "min_size": 25600,
 "max_size": 25632
},
"LightClientFinalityUpdate": {
  "min_size": 1992,
  "max_size": 2056
},
"LightClientHeader": {
 "min_size": 812,
  "max_size": 844
},
"LightClientOptimisticUpdate": {
 "min_size": 984,
  "max_size": 1016
},
"LightClientUpdate": {
 "min_size": 26776,
  "max_size": 26840
"PendingAttestation": {
 "min_size": 149,
  "max_size": 405
},
"PowBlock": {
```

```
"size": 96
  },
  "ProposerSlashing": {
    "size": 416
  "SignedAggregateAndProof": {
    "min_size": 437,
    "max_size": 693
  "SignedBLSToExecutionChange": {
    "size": 172
  "SignedBeaconBlock": {
    "min size": 1084,
    "max_size": 1125899911198852
  "SignedBeaconBlockHeader": \{\\
    "size": 208
  "SignedContributionAndProof": {
    "size": 360
  "SignedVoluntaryExit": {
    "size": 112
  "SigningData": {
    "size": 64
  "SyncAggregate": {
    "size": 160
  "SyncAggregatorSelectionData": {
    "size": 16
  "SyncCommittee": {
    "size": 24624
  "SyncCommitteeContribution": {
    "size": 160
  "SyncCommitteeMessage": {
    "size": 144
  },
  "Validator": {
    "size": 121
  "VoluntaryExit": {
    "size": 16
  "Withdrawal": {
    "size": 44
  }
}
```

See also

Hsiao-Wei Wang gave a Lightning Talk on the consensus Pyspec at Devcon VI. She swiftly covers how it is structured, how to run it, and how to build test cases. The presentation slides are available.

Sizes of containers

${\bf Glossary}$